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Interior Ballistics Modeling: Extensions to the One-Dimensional XKTC Code and Analytical Studies of Pressure Gradient for Lumped Parameter Codes

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Abstract

We describe a number of extensions to the XNOVAKTC (XKTC) Code, a model of interior ballistic phenomena based on a numerical solution of the governing equations for one-dimensional, multi-phase flow. We also present some analytical formulations for the pressure gradient in a gun in a form suitable for incorporation into a lumped parameter interior ballistics model.

In XKTC, the flow resistance formula for stacked granular propellant is extended to account for the increase in drag due to tumbling of the grains as the bed expands. The code is also extended to permit the analysis of the consequences of propellant fracture, with fracture taken to be dependent on the local maximum intergranular stress. An explicit representation of the impact induced granular compaction wave as a surface of discontinuity is encoded to support the fracture analysis.

The analytical formulas for the pressure gradient include the effects of tube geometry and several aspects of the structure of the two-phase flow. The results are in a closed form with the breech and base pressure explicitly related to the spacemean pressure. Results are presented for both granular and stick propelling charges.

Preface

The enclosed report is presented in its original form as received from the contractor and without editorial change.

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1.0 INTRODUCTION

A first objective of this report is to document certain extensions which have been made to the XNOVAKTC (XKTC) Code (Gough, 1990). The XKTC Code is intended to provide digital simulations of the interior ballistics of a wide range of gun propelling charges with particular emphasis on the influence of propellant packaging and distribution on the processes of flamespreading and pressure wave formation. Like all versions of the NOVA Code, (Gough, 1980a) from which it is derived, XKTC is based on a numerical solution of the governing equations for the macroscopic, quasi-one-dimensional flow defined by the solid propellant and its products of combustion. A second objective of this report is to document certain closed form analytical results which describe the effects of tube geometry, and the structure of the two-phase flow, on the pressure gradient in the gun. These results which relate the breech, base and spacemean pressures are intended to be of use in lumped parameter models of interior ballistics.

The analytical results pertaining to the pressure gradient are presented in Section 3.0. The balance of this introduction is concerned with the XKTC Code.

The XKTC Code is based on the balance equations for macroscopically one-dimensional two-phase flow. The state variables are to be thought of as averages of the local values or microproperties. Intractable microflow details such as drag, heat transfer and propellant combustion are assumed to be related to the macroscopic variables by means of empirical correlations. The resulting equations for each of the two phases — the solid propellant and its products of combustion — resemble the equations for unsteady flow through a duct of variable cross-sectional area. The effective cross-section for each phase incorporates the porosity or fraction of a unit volume occupied by the gas-phase. The governing equations are solved by the method of finite differences with an explicit allowance for the discontinuities in the state variables at the internal boundaries defined by the ends of the increments. Appendix A may be consulted for details of the scope of application of the Code.

The XKTC Code is the latest in a series of codes in the NOVA family of which that of Gough (1980a), may be taken as the first generally available version. The XNOVA Code (Gough, 1983) was developed to take advantage of more efficient computational procedures which had been developed in related studies. XNOVA was intended as an express version of NOVA and deleted a number of little-used options. The XNOVAK Code (Gough, 1984) was an extension of XNOVA to include finite-rate chemistry in the gasphase. XNOVAK was itself extended to become first XNOVAT (Gough, 1985), which included various features pertinent to the tank gun, but not linked to the chemistry model, and subsequently XKTC (Gough, 1990), which included additional details pertinent to tank charges and provided a full linkage of the tank gun and chemistry options. The current version of XKTC includes

certain additional features as discussed in Section 2.0. Moreover, it includes features developed under other contracts, namely the modeling of in-bore rockets (Gough, 1988a); the modeling of a traveling liquid charge (Gough, 1988b); the modeling of electrothermal guns (Gough, 1992, 1993); and alternative representations of the thermochemistry of the propellant to model near-field combustion (Gough, 1995).

Reference may be made to Gough (1990) for a statement of the balance equations for XKTC and to other sources for details of revisions to the various code options (Gough, 1998b, 1991, 1992, 1993).

The code description given in Appendix A is comprehensive and includes the contributions of all studies to date.

2.0 REVISIONS TO XRTC GOVERNING EQUATIONS

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Two topics require documentation here. In Section 2.1 we discuss revisions to the analysis of flow resistance in a bed of stacked granular propellant. In Section 2.2 we review the analysis of grain fracture with emphasis on the representation of the compression wave formed by impact on the projectile base as an explicit surface of discontinuity.

2.1 Flow Resistance of Stacked Granular Propellant

Ordinarily, granular propellant is loaded in a randomly packed fashion with the result that the flow resistance is large and the probability of pressure wave anomalies is increased. A stacked granular propellant bed involves a careful arrangement of the grains so that well defined axial flow channels are created. Such an arrangement allows charges of highly progressive multiperforated grains to have the low flow resistance typical of stick propellant while avoiding the possibility of propellant rupture due to overpressurization of the perforations which would occur in long sticks.

It is assumed that the flow resistance for stacked granular propellant is similar to that of stick propellant when the propellant is initially loaded into a configuration which creates well organized axial flow channels. However, as the propellant burns and moves it is expected that the original well ordered configuration will be lost. The grains will tumble and eventually the aggregate will develop the random structure associated with ordinary granular propellant. To capture the variation of the flow resistance with the changing structure of the aggregate, we consider the ratio of the volume per grain to the volume of a sphere in which the grain may freely rotate. dynamics of the rearrangement of the structure of the aggregate are not modeled explicitly. It is assumed that when the ratio has the initial value one or less, the aggregate is well organized due to the confinement imposed on each grain by its neighbors and that the flow resistance is therefore essentially that of a geometrically equivalent stick charge. For generality, as we see below, we admit the possibility that some fraction of the randomly packed bed flow resistance is experienced even when the bed is well ordered. When the volume ratio exceeds one, each grain is free to rotate and we assume that the aggregate becomes randomly structured so that the flow resistance is that of an ordinary granular bed. For intermediate values of the ratio, we simply interpolate between the resistance of the stick charge and that of the granular In practice, the bed is fully ignited prior to any significant expansion. Since the flow resistance of a stick charge is taken to be zero in the XKTC Code, its contribution is neglected in the intermediate regime where interpolation is involved.

The volume per grain is $V_{p_{\bullet}}/(1-\epsilon_{\bullet})$ where $V_{p_{\bullet}}$ is the superficial or exterior volume of the grain and ϵ_{\bullet} is the exterior porosity computed by neglecting the presence of the perforations. We take the volume for free rotation to be $4/3\,\mathrm{nL}^3$ where L is the length of the grain, presumably its

largest dimension. The volume for free rotation is evidently that of a sphere with radius equal to L. This is thought to be a conservative estimate of the volume. One could make a case for the use of L as the diameter of the sphere which would lead to an earlier occurrence of the prediction of randomization of the aggregate. However, the use of the smaller estimate implies a level of retained structure in the sense that the grains would be required to be centered within their respective cells.

The ratio of the volume per grain to the volume for free rotation is evidently

$$\eta = \frac{3}{4\pi L^3} \frac{V_{p_e}}{(1 - \epsilon_e)}$$
 (2.1.1)

We take the initial value of η to be η_o . Until the bed is ignited at a given location the flow resistance is assumed to be that of stick propellant. Following ignition, the flow resistance of a stick charge is assumed to be zero. We admit an input datum t_r such that for values of the time less than t_r the flow resistance of stacked granular propellant is likewise zero. The flow resistance of the stacked granular charge for $t > t_r$ is evaluated on the basis of η according to

$$\frac{f_{s}}{f_{s,NOM}} = \begin{bmatrix} 1 & & \text{if } \eta \ge 1 \\ \\ C_{\eta_{o}} + (1 - C_{\eta_{o}}) \left[\frac{(\eta - \eta_{o})}{(1 - \eta_{o})} \right]^{n_{r}} & \text{if } \eta_{o} < \eta < 1 \\ \\ C_{\eta_{o}} & & \text{if } \eta \le \eta_{o} \end{bmatrix}$$
(2.1.2)

Here C_{η_o} is a dimensionless coefficient whose value is less than one and n_r is a relaxation exponent. The form of (2.1.2) is speculative and the user of the code is required to provide values of C_{η_o} and n_r . It is suggested that values be determined by matching the code to detailed observations of the pressure distributions in instrumented gun firings.

It is emphasized that the analysis of flow resistance is performed locally. Thus the flow resistance can vary strongly from point to point as a consequence of local bed randomization.

The foregoing analysis is only implemented if $\eta_o < 1$. If the stacked granular charge is defined so that η_o is greater than one then it is supposed that special means of regulating the bed geometry have been included and the flow resistance is always evaluated as that of stick propellant.

We conclude this section with a comment on numerical stability. When a stacked granular charge is dispersed there are no intergranular stresses. in addition, the interphase drag is zero due to the choice of t, the only force acting on the grains will be the gas-phase pressure gradient, the buoyancy force. In such a situation instability can occur due to fundamental Consider the situation of steady flow and choose a physical mechanisms. reference frame in which the propellant is at rest. Let there be a local minimum of porosity and let the gas velocity be subsonic. contraction will be associated with a pressure minimum which implies that the pressure gradient will be such as to move the propellant into the compacted region from both sides, further reducing the porosity. Such problems are illposed and cannot be simulated without the use of artificial dissipative terms or fictitious forces. It may be possible to complete solutions, but mesh indifference will not be demonstrable. Accordingly, the use of large values of t_r is not recommended and non-zero values of C_{n_r} may be desirable in some cases when instability is noted in the distribution of porosity.

2.2 Analysis of Grain Fracture

The analysis of grain fracture is predicated on the maximum value of intergranular stress experienced by each local element of the propelling charge. During the calculation we monitor the stress in the bed and update the maximum values as these are established. The effect of fracture is assumed to be embedded in experimentally determined tables of multipliers to the nominal surface area and flow resistance predicated on the values of the maximum stress.

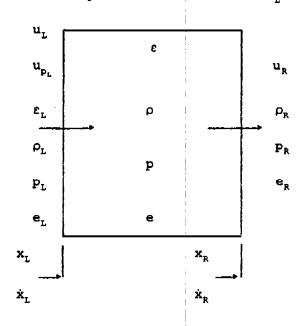
An important aspect of this approach relates to the numerical accuracy with which the stress field is determined. In particular, we are concerned here with the stress levels achieved as a result of impact of the propellant bed against the projectile base. For the sake of numerical fidelity it is desirable to represent the resulting granular shock wave as an explicit surface of discontinuity. The arguments in support of this approach may be found in Gough (1980b). We also include herewith a review of the analysis presented therein and which was encoded into an earlier version of the NOVA Code. That analysis was recoded and made compatible with the current solution algorithm of XKTC.

In keeping with the numerical formulation of XKTC we require a lumped parameter analysis of a two-phase region to model the compacted region shortly after formation when its resolution as a one-dimensional continuum would impose a restrictively low time step. This topic is covered in Section 2.2.1. In Section 2.2.2 we summarize the constitutive relations including boundary

conditions to be used at the internal boundary. Section 2.2.3 notes some aspects of the implementation of the analysis which may help in the interpretation of the solution.

2.2.1 Balance Equations for a Two-Phase Lumped Parameter Region

Consider a lumped parameter region as depicted in the sketch. It is bounded by surfaces located at x_1 and x_2 whose functional dependence on time



will be furnished from independent considerations. The region assumed to have an instantaneous volume V which is available to the two-phase flow and sectional areas of the bounding surfaces available to the flow are taken to be A_r and A_p . We identify x_p with the external boundary, which is at most gas-permeable and x, with granular compaction wave. Accordingly, we consider the flux of both phases across x, and only the gas across x_{g} . We note also that the flux of gas may correspond either to mass addition or mass loss but that only mass addition is expected in regard to the solidphase.

We assume that the igniter or primer condensed phase may have a finite density ρ_{IG} and be characterized by a rate of gasification ψ per unit volume. With this in mind it is easy to see that the volume of the lumped parameter region is governed by the ordinary differential equation.

$$\dot{\mathbf{V}} = \mathbf{A}_{\mathbf{R}}\dot{\mathbf{x}}_{\mathbf{R}} - \mathbf{A}_{\mathbf{L}}\dot{\mathbf{x}}_{\mathbf{L}} + \dot{\mathbf{V}}_{\mathbf{I}\mathbf{G}}^{\dagger} \tag{2.2.1.1}$$

where

$$\dot{V}_{1G} = \frac{1}{\rho_{1G}} \int_{x_1}^{x_R} A(x) \psi(x) dx$$
 (2.2.1.2)

represents the rate of increase in volume due to consumption of the igniter.

The porosity or void fraction is predicated on the available volume V. Hence the balance of mass of the solid-phase may be expressed as

$$\frac{\mathbf{d}}{\mathbf{dt}} \left[(1 - \varepsilon) \mathbf{V} \right] = \mathbf{A}_{L} (1 - \varepsilon_{L}) \left(\mathbf{u}_{\mathbf{p}_{L}} - \dot{\mathbf{x}}_{L} \right) - \frac{\dot{\mathbf{m}}}{\rho_{\mathbf{p}}} \mathbf{V}$$
 (2.2.1.3)

where

$$\dot{m} = (1 - \epsilon) \rho_p \frac{S_p}{V_p} \dot{d}$$
 (2.2.1.4)

describes the rate of gasification of the solid propellant. We have ρ_p , propellant density; S_p , the surface area of a grain; V_p , the volume of a grain; and d, the rate of surface regression. We have, moreover, used the familiar nomenclature for the state variables: ϵ , porosity; , u_p solid-phase velocity. The subscript L refers to values on the boundary of the contiguous continuum region.

In view of (2.2.1.1), we may expand the differential on the left hand side of (2.2.1.3) to get the result

$$\dot{\epsilon} = \frac{1}{V} \left\{ (1 - \epsilon) (A_R \dot{x}_R - A_L \dot{x}_L) - (1 - \epsilon_L) A_L (u_{p_L} - \dot{x}_L) \right\} + (1 - \epsilon) \frac{\dot{V}_{IG}}{V} + \frac{\dot{m}}{\rho_p}$$
(2.2.1.5)

The balance of mass of the gas-phase may be stated in the form

$$\frac{d}{dt} \left[\epsilon \rho V \right] = \epsilon_L \rho_L A_L (u_L - \dot{x}_L) - \epsilon_R \rho_R A_R (u_R - \dot{x}_R) + \dot{m} V + \rho_{IG} \dot{V}_{IG} \qquad (2.2.1.6)$$

where we have ρ , the gas-density and u its velocity. As in the preceding section, the subscripts refer to values on the boundaries of the contiguous regions.

By expanding the left hand side and making use of (2.2.1.1) and (2.2.1.5) we may put (2.2.1.6) into the computational form

$$\dot{\rho} = \frac{1}{\varepsilon V} \left\{ \varepsilon_{L} \rho_{L} A_{L} \left(u_{L} - \dot{x}_{L} \right) - \varepsilon_{R} \rho_{R} A_{R} \left(u_{R} - \dot{x}_{R} \right) - \rho \left(A_{R} \dot{x}_{R} - A_{L} \dot{x}_{L} \right) \right.$$

$$\left. + \rho \left(1 - \varepsilon_{L} \right) A_{L} \left(u_{\rho_{L}} - \dot{x}_{L} \right) \right\} + \frac{\dot{m}}{\varepsilon} \left(1 - \frac{\rho}{\rho_{D}} \right) + \frac{\rho_{IG} V_{IG}}{\varepsilon V} \left(1 - \frac{\rho}{\rho_{IG}} \right)$$

$$(2.2.1.7)$$

Using e to denote internal energy and $h = e + p/\rho + u_{rel}^2/2$ to denote the total enthalpy, we may express the balance of energy of the gas-phase in a frame of reference whose instantaneous velocity is equal to that of the gas in the lumped parameter region in the following form.

$$\frac{d}{dt} \left[\epsilon \rho e V \right] = A_L \epsilon_L \rho_L h_L (u_L - \dot{x}_L) - A_R \epsilon_R \rho_R h_R (u_R - \dot{x}_R)$$

$$+ h_p \dot{m} V + h_{IG} \rho_{IG} \dot{V}_{IG} - p \frac{d}{dt} \left[\epsilon V \right] - q_p$$

$$(2.2.1.8)$$

This equation may be interpreted as the statement: rate of change of energy within the control volume occupied by the gas-phase equals total enthalpy flux into the volume less work to expand the control volume and heat lost to the propellant. The terms h_p and h_{IG} refer to the propellant and igniter products respectively and are assumed to embed the chemical energy. As we discuss further, the mass transfer is assumed to be adiabatic and to be governed by a quasi-steady law in the frame of reference of the gas within the lumped parameter region.

Using Equations (2.2.1.1) and (2.2.1.5) and (2.2.1.6) to simplify (2.2.1.8) we have the result

$$\dot{\mathbf{e}} = \frac{1}{\epsilon \rho V} \left\{ \mathbf{A}_{L} \epsilon_{L} \rho_{L} (\mathbf{u}_{L} - \dot{\mathbf{x}}_{L}) (\mathbf{h}_{L} - \mathbf{e}) - \mathbf{A}_{R} \epsilon_{R} \rho_{R} (\mathbf{u}_{R} - \dot{\mathbf{x}}_{R}) (\mathbf{h}_{R} - \mathbf{e}) - \mathbf{p} (\mathbf{A}_{R} \dot{\mathbf{x}}_{R} - \mathbf{A}_{L} \dot{\mathbf{x}}_{L}) + \mathbf{p} (\mathbf{1} - \mathbf{e}_{L}) \mathbf{A}_{L} (\mathbf{u}_{p_{L}} - \dot{\mathbf{x}}_{L}) + \dot{\mathbf{m}} V (\mathbf{e}_{p} - \mathbf{e}) + \rho_{IG} \dot{V}_{IG} (\mathbf{e}_{IG} - \mathbf{e}) - \mathbf{q}_{p} \right\}$$

$$(2.2.1.9)$$

2.2.2 Constitutive Relations

We first state the conditions which apply in general at a discontinuity in macroscopic two-phase flow (Gough, 1979). Next we note the conditions which apply at a solid-phase contact discontinuity. Then we turn to the case of the compaction wave.

We note that we have given no provision yet for the determination of the intergranular stress in the compacted region. The intergranular stress will be assumed to be equal to the value deduced from an analysis of the jump conditions. Accordingly, the stress is not taken to be a function of the porosity of the compacted region as a whole.

In addition, we note that the preceding equations have referred to such quantities as the interphase heat transfer \mathbf{q}_p and the rate of surface regression. A separate accounting of these quantities is not maintained. The values in a lumped parameter region are assumed to be equal to those on the boundary of the neighboring continuum region.

General Results

Let the speed of the surface of discontinuity be u_s. Denote the properties of the phases on each side of discontinuity by the subscripts 1 and 2. The principles of conservation of mass, momentum and energy lead to the following four jump conditions or conditions of finite compatibility.

$$\varepsilon_1 \rho_1 \left(\mathbf{u}_1 - \mathbf{u}_s \right) = \varepsilon_2 \rho_2 \left(\mathbf{u}_2 - \mathbf{u}_s \right) \tag{2.2.2.1}$$

$$(1 - \epsilon_1) \rho_p (u_{p_1} - u_s) = (1 - \epsilon_2) \rho_p (u_{p_2} - u_s)$$
 (2.2.2.2)

$$p_{1} + \sigma_{1} + \frac{\rho_{1} \varepsilon_{1}}{g_{0}} (u_{1} - u_{s})^{2} + \frac{\rho_{p}}{g_{0}} (1 - \varepsilon_{1}) (u_{p_{1}} - u_{s})^{2}$$

$$= p_{2} + \sigma_{2} + \frac{\rho_{2} \varepsilon_{2}}{g_{2}} (u_{2} - u_{s})^{2} + \frac{\rho_{p}}{g_{0}} (1 - \varepsilon_{2}) (u_{p_{2}} - u_{s})^{2}$$
(2.2.2.3)

$$e_1 + \frac{p_1}{\rho_1} + \frac{(u_1 - u_s)^2}{2g_o} = e_2 + \frac{p_2}{\rho_2} + \frac{(u_2 - u_s)^2}{2g_o}$$
 (2.2.2.4)

Equations (2.2.2.1) and (2.2.2.2) state the principles of conservation of mass for each of the phases. Equation (2.2.2.3) expresses the conservation of momentum of the mixture and introduces o, the intergranular stress (Gough, 1979). Equation (2.2.2.4) expresses conservation of energy for the gas-phase. No energy equation is stated for the solid-phase as it is assumed to be microscopically incompressible.

The fact that the principle of conservation of momentum can only be stated, in general, for the mixture implies that an element of indeterminacy has been introduced which can only be resolved by making some sort of constitutive assumption regarding the exchange of momentum between the phases. Analytically, our inability to state separate, generally valid, relationships to describe the momentum jump for each of the phases stems from the nature of

the mechanical interaction between the phases. The mechanical interaction involves a term of the form $p\nabla\epsilon$ which clearly cannot be assumed a priori to be bounded everywhere within a control volume which envelopes the discontinuity. Only by recognizing the possibility of momentum exchange between the phases can (2.2.2.3) be split.

Solid-Phase Contact Discontinuity

If the discontinuity is such as to admit a jump in porosity as we pass from one mixture region to another then, provided the discontinuity is physically stable, we may assume

$$u_{p_1} = u_{p_2} = u_s$$
 (2.2.2.5)

as is usual in a contact discontinuity.

Moreover, we may postulate, by analogy with the single phase case that the intergranular stress will also be continuous.

$$\sigma_1 = \sigma_2 \tag{2.2.2.6}$$

With the assumption (2.2.2.6), Equations (2.2.2,1), (2.2.2.3) and (2.2.2.4) may be restated as follows

$$\varepsilon_1 \rho_1 (\mathbf{u}_1 - \mathbf{u}_s) = \varepsilon_2 \rho_2 (\mathbf{u}_2 - \mathbf{u}_s) \tag{2.2.2.7}$$

$$p_1 + \frac{\varepsilon_1 \rho_1}{g_0} (u_1 - u_s)^2 = p_2 + \frac{\varepsilon_2 \rho_2}{g_0} (u_2 - u_s)^2$$
 (2.2.2.8)

$$e_1 + \frac{p_1}{\rho_1} + \frac{(u_1 - u_s)^2}{2g_0} = e_2 + \frac{p_2}{\rho_2} + \frac{(u_2 - u_s)^2}{2g_0}$$
 (2.2.2.9)

and are analogous to the Rankine-Hugoniot jump conditions which constrain the state variables on either side of a single phase discontinuity, as for example, a shock.

Granular Compaction Wave

We postulate that (2.2.2.7), (2.2.2.8) and (2.2.2.9) continue to govern the jumps in the properties of the gas-phase. The properties of the solid-phase are therefore governed by the jump condition (2.2.2.2), which is independent of our assumption, and by the following

$$\sigma_1 + (1 - \varepsilon_1) \frac{\rho_p}{g_o} (u_{p_1} - u_s)^2 = \sigma_2 + (1 - \varepsilon_2) \frac{\rho_p}{g_o} (u_{p_2} - u_s)^2$$
 (2.2.2.10)

which, of course, reduces to (2.2.2.6) as u_{p_1} , $u_{p_2} \rightarrow u_s$.

In XKTC we have the following nominal relationship between σ and ϵ under monotonic loading from the settling porosity ϵ_o at which $\sigma=0$ by definition

$$\sigma_{\mathbf{z}}(\varepsilon) = \begin{cases} \rho_{\mathbf{p}} \frac{a_{1}^{2}}{g_{0}} \varepsilon_{0}^{2} \left(\frac{1}{\varepsilon} - \frac{1}{\varepsilon_{0}}\right) & , & \varepsilon \leq \varepsilon_{0} \\ \\ 0 & \text{if } \varepsilon > \varepsilon_{0} \end{cases}$$

$$(2.2.2.11)$$

and we assume that this applies under the condition of shock loading.

In addition we note the following relationship which describes reloading to the nominal curve $\sigma_{\epsilon}(\epsilon)$ from a state (ϵ_1,σ_1) lying below the curve

$$\sigma'(\varepsilon) = \sigma_1 + \frac{\rho_p a_2^2}{\sigma_2} (\varepsilon_1 - \varepsilon)$$
 (2.2.2.12)

and we note that a_2^2 is expected to be an order of magnitude greater than a_1^2 . Then if (ϵ_1,σ_1) are identified as the porosity and stress on the uncompacted side of the granular shock we take

$$\sigma_2(\varepsilon_2) = \min \left(\sigma'(\varepsilon_2), \, \sigma_1(\varepsilon_2) \right) \tag{2.2.2.13}$$

In most cases of interest, the granular bed is dispersed prior to impact. Accordingly, σ_1 = 0 and $\epsilon_1 > \epsilon_0$. It then follows that $\sigma_2(\epsilon_2) = \sigma_*(\epsilon_2)$ and, of course, $\epsilon_2 \leq \epsilon_0$.

Concerning the method of solution, consider first the case when a lumped parameter representation has been made of the compacted region. We therefore assume, from the uniformity of the compacted region, that \mathbf{u}_{p_2} is given as equal to the velocity of the external boundary. Moreover, the values ϵ_1 , σ_1 and \mathbf{u}_{p_1} are known on the uncompacted side from the usual computational procedure, although we shall have to comment a little further on the case when $\sigma_1 \neq 0$. Taking ϵ_1 , σ_1 and \mathbf{u}_{p_1} as given for the moment we recast (2.2.2.2) and (2.2.2.10) to yield

$$\sigma_2 = \sigma_1 + \frac{\rho_p}{g_o} \frac{(1 - \epsilon_1)(1 - \epsilon_2)}{\epsilon_1 - \epsilon_2} (u_{p_2} - u_{p_1})^2$$
 (2.2.2.14)

and

$$u_{s} = \frac{(1 - \varepsilon_{2})u_{p_{2}} - (1 - \varepsilon_{1})u_{p_{1}}}{\varepsilon_{1} - \varepsilon_{2}}$$
 (2.2.2.15)

Equations (2.2.2.13) and (2.2.2.14) may be solved simultaneously, using a midpoint search, to yield the values of ϵ_2 and σ_2 . Then u_s follows from (2.2.2.15) and the gas-phase properties follow from the usual NOVA Code methodology for a solid-phase contact discontinuity.

2.2.3 Coding Considerations

The user specifies the value of the switch NXCW. If this is non-zero, an explicit representation will be made of the granular compaction wave. Because several collisions may occur between the bed and the external boundary, an additional datum is supplied so as to preclude the explicit representation of weak waves. The user supplies a value XIMPV which is the minimum velocity of impact for which the explicit analysis will be conducted. As presently encoded, the explicit analysis can be performed just once per interior ballistic cycle.

To incorporate the explicit analysis, the input program initializes NRG = 2n + 4 regions where n is the number of regions of propellant. We note that this value of NRG is greater by 2 than the normal value. The two additional regions are placed at the leading edge of the forward propellant segment. They are, of course, initially collapsed.

On impact region NRG-3 is given a value of NDTACH = 1 signifying that boundary motion must be computed, but the compacted region is not modeled until it is large enough to be treated as lumped parameter. Eventually, the boundary motion may be sufficient to warrant a continuum representation in accordance with the user-specified value of RZOLV.

At that point, subroutine REG21A is called to transfer the solution to region NRG-2. Region NRG-3 is closed and, except that the boundary motion is that of a shock, the solution technique is now very close to the standard NOVA condition. When the velocity jump across the moving boundary is less than 0.01 times XIMPV or when the compacted region expands and the rate of propagation of intergranular disturbances becomes zero, the shock is considered to have degenerated. The boundary is then frozen as a contact discontinuity.

If the wave degenerates while the compacted region is still lumped parameter, the region representation is maintained until sufficient expansion occurs for it to treated as a continuum. If, on the other hand, the wave is so persistent as to approach the far boundary of the propellant bed, it is transformed to a contact discontinuity at the point at which the uncompacted section would have to be treated as a lumped parameter region according to the value of RZOLV.

Appendix A may be consulted for further details concerning the input data NXCW, RZOLV and XIMPV.

3.0 PRESSURE GRADIENT IN GUN PROPELLING CHARGES

In lumped parameter models of gun interior ballistics it is generally assumed that the modeled value of pressure must represent a spacemean value, On the other hand, the equation of motion of the projectile requires a knowledge of the value of the base pressure, $p_{\rm g}$. Closure of the lumped parameter model therefore requires a specification of the relation between p. and \overline{p} . Moreover, the charge designer needs to know the maximum local pressure in order to assure integrity of the gun tube. This maximum is assumed to occur at the breech and we denote the value by the symbol p_{as} . A traditional approach has been to use the results of Lagrange (Corner, 1950). If the tube is assumed to have uniform area and the mixture of propellant and combustion products is assumed to constitute a homogeneous mixture whose density is independent of position, the continuity equation shows the velocity distribution to be linear and this, in turn, enables one to deduce from the momentum equation that the pressure distribution is quadratic. If C is the charge mass and M is the projectile mass, it emerges that

$$\frac{\overline{p}}{p_B} = 1 + \frac{C}{3M} \qquad (3.1)$$

and

$$\frac{\mathbf{p}_{BR}}{\mathbf{p}_{B}} = 1 + \frac{C}{2M} \qquad (3.2)$$

at all times. These formulae seem to give satisfactory results in simulations of artillery charges in which C/M is typically of the order of 0.2 and the difference between \overline{p} and p_{B} is therefore only a few percent. In tank gun charges for which C/M is of the order of one and the difference between \overline{p} and p_{B} is therefore appreciable, the results are not as satisfactory.

In seeking improvements to Equations (3.1) and (3.2) we may identify the following processes which are omitted from the theory of Lagrange:

- (1) The theory is inherently incapable of representing the occurrence of pressure waves due to the interplay between the ignition train and the packaging of the charge.
- (2) Even for smoothly ignited charges, there is no representation of the propagation of rarefaction waves due to the acceleration of the projectile.

- (3) Gun chambers are generally tapered and the difference between chamber area and tube area can be significant in tank guns. Moreover, the projectile afterbody may intrude significantly into the chamber.
- (4) An examination of two-phase flow simulations shows that the assumption of uniform mixture density is not unreasonable for granular propellant. Although the propellant lags behind the gas with the result that a small region of ullage is created behind the moving projectile, the distributions of each of the two phases are fairly uniform over the length of the tube. However, the velocity lag of the solid-propellant should not be neglected in the momentum equation for the mixture which is used to construct the pressure profile from the velocity distributions.

Of course, all the foregoing processes may be accommodated in a natural way through the use of a fully two-phase analysis such as that embedded in the NOVA Code (Gough, 1980a). However, we may still enquire whether improvements can be made to Equations (3.1) and (3.2) to reflect some of the foregoing processes while at the same time retaining the computational economy and general utility of a lumped parameter approach.

We conclude these introductory remarks with some additional discussion of each of the foregoing processes. In Section 3.1 we show how the Lagrange hypothesis can be extended to account for tubes whose cross-sectional area varies with position. In Section 3.2 we address the effects of the slip velocity between the propellant and the products of combustion. Analytical results are obtained. In Section 3.3 we consider the effects of time dependence of the cross-sectional area. In contrast to the two preceding topics, complete analytical results are not pursued. In Section 3.4 we consider the combined effects of propellant slip velocity and cross-sectional area as a function of position. Again, full analytical results are obtained to describe extended Lagrange relationships between \overline{p} , \overline{p}_{B} and \overline{p}_{BR} .

Ignition Transients

The representation of pressure waves due to ignition transients seems the most difficult process to embed in a lumped parameter model. Possibly, an ensemble of NOVA solutions could be obtained with the objective of expressing the ratios \overline{p}/p_B and p_{BR}/p_B , as functions of time, parametrically with respect to the charge attributes. However, it is not clear that the number of runs required to establish the functional relations would be significantly less than the number of runs required to address specific charge configurations of actual interest. As far as the present study is concerned, we implicitly exclude from consideration those charges for which strong ignition-induced pressure waves are present. We note, however, that the occurrence of such waves may have little ballistic consequence provided that they are not so severe as to be accompanied by grain fractures. For example, NOVA simulations of the 5-inch/54

caliber Navy case charge exhibit strong pressure waves, in accord with experiments. Nevertheless, good agreement between predicted values of maximum pressure and muzzle velocity is found when consistent data are used to run NOVA and a lumped parameter code. This suggests that the ballistic event occurs sufficiently slowly for the effects of the ignition transient to be averaged out.

Rarefaction Waves

Rarefaction due to motion of the projectile is embedded in the Lagrange representation in a manner which assumes all elements of the mixture to be expanding at the same rate, a rate which is determined by the instantaneous velocity of the projectile. In reality, of course, it takes time for the state of motion of the projectile to be impressed throughout the propulsion gas and the pressure gradient may be expected to undulate as the unloading waves travel back and forth between the breech and the base of the projectile.

An analytical solution was obtained by Love and Pidduck (Corner, 1950) for the special case in which the propellant is all burnt and quiescent prior to projectile motion. Their results show the ratio \bar{p}/p_B to undergo a damped oscillation about an asymptotic value which is presumably achieved with infinite projectile displacement. The value of \bar{p}/p_B , initially equal to one, increases as the rarefaction due to projectile motion propagates rearward. When the rarefaction is reflected from the breech, the ratio undergoes a maximum and returns to the value one when the reflected wave reaches the projectile base, after which it begins to rise again.

Pidduck and Kent (Corner, 1950), noting that the initial rarefaction tended to damp rather quickly, sought a similarity solution which would agree asymptotically with the solution of Love and Pidduck although it would differ in the early stages. From their analysis emerges an alternative to Equation (3.1) in the form

$$\frac{\overline{p}}{p_n} = 1 + \frac{C}{\delta M} \qquad (3.3)$$

where δ is the Pidduck-Kent constant, a function of C/M and the ratio of specific heats. Their observation that the oscillations due to the system of rarefaction waves tend to damp out is consistent with our previous comment concerning the averaging out of the ignition transients. The fact that the Pidduck-Kent solution does not accord with the earlier stages of the exact solution is not really of importance, since the initial stages of the exact solution are quite remote from actual propelling charge behavior. Typically, in real charges, the propellant is fifty percent consumed and the projectile has achieved fifty percent of the muzzle velocity at the time when maximum

pressure occurs. On the other hand, the asymptotic agreement between the similarity solution and the exact solution may or may not be of importance. One has to assume that in spite of the highly idealized initial conditions, the exact solution nevertheless tends towards the behavior of a real charge.

An alternative approach is contained in a R.A.R.D.E. paper (Anon, 1964). It is assumed that the tube is straight and attention is focussed on the balance equations for the gas-phase alone. In place of the linear velocity distribution which emerges from the standard Lagrange assumption, it is supposed that the velocity distribution is a quadratic whose coefficients are functions of time. At the same time, it is also assumed that the pressure distribution remains quadratic, as in the standard Lagrange formulation. balance equations are converted to ordinary differential equations at one point, arbitrarily selected to be the breech. Limiting arguments are used, together with the boundary conditions, to determine governing equations for the coefficients in the velocity distribution. A global energy balance is also invoked. The propellant is supposed to be uniformly distributed, although a method of relaxing this assumption is discussed. The propellant is assumed to burn at a finite rate. However, we note that the balance equations for the gas-phase implicitly assume the propellant to be at rest and no consideration is given to interphase drag. Neglect of interphase drag is appropriate only for stick propellant; however, the assumption of uniform distribution is only appropriate for granular charges.

Non-Uniform Flow Area

Non-uniformity can be due not only to variations in the tube cross-sectional area, but also to the intrusion of the projectile afterbody. Variations in tube area are presumably confined to the chamber region and are a function of position only. This problem has been previously addressed by Vinti (1942) who presented results corresponding to a cylindrical chamber connected to a cylindrical tube of smaller diameter. Vinti also considered the effects of gun recoil and wall friction on the pressure gradient. These latter effects, which are omitted from the NOVA Code, are not considered here. Analytical results to express the influence of flow area on the pressure gradient have been obtained more recently by Morrison and Wren (1987). Variations in flow area due to the intrusion of the afterbody are a function of both position and time. We will show that the spacewise variations in flow area can be accommodated in an extended Lagrange formulation.

When the flow area decreases with distance downbore, as is the case in normal situations, and the spacemean pressure is understood to be an area-weighted quantity, one may deduce that the ratio \overline{p}/p_B is reduced relative to the ideal Lagrange value, Equation (3.1). The Lagrange value will be attained asymptotically with infinite projectile displacement, provided that the non-uniformity of area is localized to the chamber and the projectile afterbody.

However, an additional complication to be considered in the case of a projectile afterbody is that the motion of the projectile depends on a spacewise integral of pressure rather than a local value. This consideration is not pursued in the present study.

Propellant Velocity Lag

The analysis of Lagrange implicitly assumes that either the propellant is all burnt at the initial instant, or that the burning propellant moves with the same velocity as the gas-phase. The degree to which the propellant velocity remains in equilibrium with that of the gas-phase is determined primarily by the interphase drag. If there were no drag, or flow resistance, one might expect that Equation (3.1) would apply provided that C were replaced by the total mass of the gas-phase at any time. In such a situation one would expect that the ratio \overline{p}/p_n would initially be nearly equal to one and would gradually increase to the limiting Lagrange value as the propellant was In reality, flow resistance will be present and the pressure gradient will therefore be expected to exceed that which would arise with no Depending on the magnitude of the velocity lag, the flow resistance. contribution of the flow resistance, which is quadratically dependent on the difference between the velocity of the gas and that of the propellant, might be such as to produce instantaneous values of \overline{p}/p , in excess of the Lagrange value given by Equation (3.1). The influence of the propellant velocity lag may therefore be such as to introduce complex structure into the time dependence of the ratio \overline{p}/p_{R} .

3.1 Non-Uniform Bore Area

We consider the continuity and momentum equations for unsteady flow of a homogeneous inviscid substance through a tube with variable area A = A(z).

$$\frac{\partial \rho}{\partial t} + \frac{1}{A} \frac{\partial \rho A u}{\partial z} = 0 \qquad , \tag{3.1.1}$$

$$\rho \frac{\partial u}{\partial t} + \rho u \frac{\partial u}{\partial z} + g_0 \frac{\partial p}{\partial z} = 0 \qquad . \tag{3.1.2}$$

Here we have t, time; z, axial position; ρ , density; u, velocity; p, pressure; and g_0 is a constant used to reconcile dimensions.

We make the Lagrange assumption:

$$\frac{\partial \rho}{\partial z} = 0 . (3.1.3)$$

Equation (3.1.1) becomes

$$\frac{\partial Au}{\partial z} = -\frac{A}{\rho} \frac{\partial \rho}{\partial t} \qquad (3.1.4)$$

From global conservation:

$$\rho = \frac{C}{\int_{0}^{z_{p}} A(z) dz},$$
(3.1.5)

where z_p is the projectile position and C is the total charge mass. Using $V\left(z\right)$ to represent the volume between the breech face and station z this may be written as

$$\rho = \frac{c}{V(z_p)} \qquad (3.1.6)$$

We assume that the variations in A(z) are due only to the shape of the combustion chamber and, possibly, the afterbody of the projectile. The projectile is assumed to have velocity V_p and to move through a tube whose area is fixed and equal to A_p . Differentiating (3.1.6) with respect to time we see that

$$\frac{\partial \rho}{\partial t} = -\frac{A_B C V_p}{V^2(z_p)} = -\frac{\rho A_B V_p}{V(z_p)} , \qquad (3.1.7)$$

which is a function of time alone. Substituting into (3.1.4) and using the boundary condition u=0 at z=0, we have

$$A(z)u(z) = \frac{A_BV_p}{V(z_p)} \int_0^z A(z)dz = \frac{A_BV(z)V_p}{V(z_p)}$$
 (3.1.8)

If $A(z) = A_B$, a constant, this becomes

$$u(z) = V_p \frac{z}{z_p}$$
 (3.1.9)

which is the usual Lagrange result. Note that since

$$\frac{\partial u}{\partial z} = f(t) - \frac{u}{A} \frac{\partial A}{\partial z} ,$$

it follows that for $\partial A/\partial z < 0$, as is expected to be the case, $\partial u/\partial z$ is not constant but increases with z. The distribution of velocity is therefore superlinear or sublinear according as $\partial A/\partial z \stackrel{>}{_{\sim}} 0$.

The pressure distribution follows from the momentum equation (3.1.2)

$$g_0 \frac{\partial p}{\partial z} = -\frac{C}{V(z_p)} \left[\frac{A_B V(z)}{A(z) V(z_p)} \left[\dot{V}_p - \frac{A_B V_p^2}{V(z_p)} \right] + \frac{V_p^2 A_B^2}{A(z)} \frac{V(z)}{V^2(z)_p} \left[1 - \frac{V(z)}{A^2(z)} \frac{\partial A}{\partial z} \right] \right]$$
(3.1.10)

Combining terms, and noting that $\int \frac{V^2}{A^3} \frac{\partial A}{\partial z} dz = \int \frac{V}{A} dz - \frac{V^2}{2A^2}$,

it follows that

$$g_0[p(z) - p(0)] = J_1(z) \frac{CA_B}{V^2(z_p)} \left[\frac{A_B V_p^2}{V(z_p)} - \dot{V}_p \right] - \frac{CV_p^2}{2} \frac{A_B^2 V^2(z)}{A^2(z) V^3(z_p)} , \qquad (3.1.11)$$

where

$$J_1(z) = \int_0^z \frac{V(z)}{A(z)} dz$$

Note that p(z) depends on both V_p and V_p . It should also be noted that (3.1.11) remains unchanged even if $\partial A/\partial z=0$ for part of the flow, as would be expected in a normal gun tube.

In order to define the spacemean pressure, it seems appropriate to use

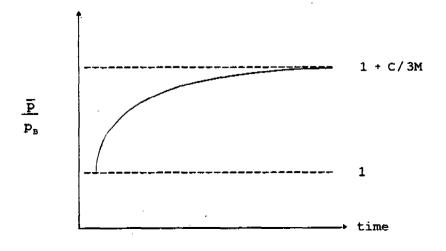
$$\overline{p} = \frac{\int_{0}^{z_{p}} p(x) A(x) dx}{\int_{0}^{z_{p}} A(x) dx} \qquad (3.1.12)$$

While we cannot establish quantitative results at this point, we can draw conclusions concerning the qualitative behavior of the pressure ratio $\overline{p}/p_{\rm g}$. We expect actual gun tubes to have a tapered chamber with area reduction (chambrage) at the entrance to the bore. Consider the limiting case when the bore area is infinitesimal compared with that of the chamber. A condition of stagnation will occur in the chamber and the pressure drop will occur only in the tube. At low projectile velocities (low Mach number) we will have

$$p_B \sim p_{BR} - \frac{\rho_{BR}}{2g_0} V_p^2$$
 (3.1.13)

where p_{BR} and ρ_{BR} are respectively the pressure and density in the breech and where we assume that the amount of gas in the tube is small compared with the projectile mass. This also follows from (3.1.11) if we note that $J(z) \sim \frac{V(z_p)}{A_B} \; (z_p - z_{p_o}) \; \text{ under the stated conditions; only the last term of } (3.1.11) \; \text{ remains.}$

It is easy to see that, if M << 1, then $\overline{p}/p_B \sim 1$ and is much less than the Lagrange value L = 1 + C/3M. We expect the Lagrange number to be established as $z_p \to \infty$ and $V(z_p) >> V(z_{p_o})$. Thus, with chambrage, we expect a gradual increase of \overline{p}/p_B as shown in the following sketch.



We conclude this section by considering the computational implications of the foregoing analysis. We may write Equation (3.1.11) in the form

$$p(z) = p(0) + a(t)J_1(z) + b(t)J_2(z)$$
, (3.1.14)

where

$$a(t) = \frac{CA_{B}}{g_{0}V^{2}(z_{p})} \left[\frac{A_{B}V_{p}^{2}}{V(z_{p})} - \dot{V}_{p} \right] , \qquad (3.1.15)$$

$$b(t) = -\frac{CV_p^2}{2g_0} \frac{A_B^2}{V^3(z_p)} , \qquad (3.1.16)$$

$$J_1(z) = \int_0^z \frac{V(z)}{A(z)} dz$$
, (3.1.17)

$$J_2(z) = \frac{V^2(z)}{A^2(z)}$$
 (3.1.18)

The spacemean pressure, as defined by Equation (3.1.12), becomes

$$\overline{p} = p(0) + \frac{a(t)}{V(z_p)} J_3(z_p) + \frac{b(t)}{V(z_p)} J_4(z_p)$$
 (3.1.19)

where

$$J_{3}(z_{p}) = \int_{0}^{z_{p}} A(z) J_{1}(z) dz , \qquad (3.1.20)$$

$$J_4(z_p) = \int_0^{z_p} A(z) J_2(z) dz \qquad . \tag{3.1.21}$$

We assume that \overline{p} is the value of pressure determined from the lumped parameter model using the equation of state. Then the breech pressure, p_{BR} , and the base pressure, p_{BR} , are evidently given as

$$\mathbf{p}_{BR} = \overline{\mathbf{p}} - \frac{\mathbf{a}(t)}{V(z_p)} J_3(z_p) - \frac{\mathbf{b}(t)}{V(z_p)} J_4(z_p)$$
 (3.1.22)

and

$$p_p = p_{pp} + a(t)J_1(z_p) + b(t)J_2(z_p)$$
 (3.1.23)

Some simplification follows when the variation in area is confined to the chamber. Such a situation is expected when the tube is not tapered and when the projectile has no afterbody. If the initial position of the projectile base is z_p and if $A(z) = A_p$ for $z \ge z_p$ it follows that

$$V(z_p) = V(z_{p_0}) + A_B(z_p - z_{p_0})$$
 (3.1.24)

$$J_{1}(z_{p}) = J_{1}(z_{p_{e}}) + \frac{1}{A_{B}} \left[V(z_{p_{e}}) (z_{p} - z_{p_{e}}) + \frac{A_{B}}{2} (z_{p} - z_{p_{e}})^{2} \right] , \qquad (3.1.25)$$

$$J_2(z) = \frac{1}{A_B^2} \left[V(z_{p_o}) + A_B(z_p - z_{p_o}) \right]^2 , \qquad (3.1.26)$$

$$J_{3}(z_{p}) = J_{3}(z_{p_{o}}) + A_{B}J_{1}(z_{p_{o}}) (z_{p} - z_{p_{o}}) + \frac{V(z_{p_{o}})}{2} (z_{p} - z_{p_{o}})^{2} + \frac{A_{B}}{6} (z_{p} - z_{p_{o}})^{3} , \qquad (3.1.27)$$

$$J_{4}(z_{p}) = J_{4}(z_{p_{o}}) + \frac{1}{3A_{B}^{2}} \left[\left[V(z_{p_{o}}) + A_{B}(z_{p} - z_{p_{o}}) \right]^{3} - V^{3}(z_{p_{o}}) \right] \qquad (3.1.28)$$

Hence the geometric terms $V(z_{p_o})$, $J_1(z_{p_o})$, $J_2(z_{p_o})$, $J_3(z_{p_o})$ and $J_4(z_{p_o})$ need be computed just once at the start of the calculation and the values may then be saved for subsequent use.

In principle, the global energy balance should be revised to a form consistent with the assumptions of the pressure gradient analysis. The kinetic energy of the propellant is found to be ${\rm CV}_{\rm p}^2/6g_0$ when the conventional Lagrange hypothesis is used. From Equation (3.1.8) we see that an expression consistent with the present analysis is

$$KE = \frac{CV_p^2}{2g_0} \frac{A_B^2}{V^3(z_p)} J_4(z_p) \qquad (3.1.29)$$

Finally, we eliminate the implicit dependence of Equations (3.1.22) and (3.1.23) on p_g through a(t) as defined by (3.1.15). The equation of motion of the projectile may be written as

$$\dot{V}_{p} = \frac{g_{0}A_{B}}{M_{0}} [p_{B} - p_{RES}]$$
 (3.1.30)

where \mathbf{M}_{p} is the mass of the projectile and \mathbf{p}_{RES} is the bore resistance. Evidently,

$$a(t) = a_1(t) + a_2(t)p_B$$
 (3.1.31)

where

$$a_{1}(t) = \frac{CA_{B}}{g_{0}V^{2}(z_{p})} \left[\frac{A_{B}V_{p}^{2}}{V(z_{p})} + \frac{g_{0}A_{B}}{M_{p}} p_{RES} \right] , \qquad (3.1.32)$$

$$a_2(t) = -\frac{C}{M_p} \frac{A_B^2}{V^2(z_p)}$$
 (3.1.33)

Substituting (3.1.31) into Equations (3.1.22) and (3.1.23) we find

$$p_{BR} = \alpha p_B + \beta \qquad , \tag{3.1.34}$$

$$\overline{p} = \gamma p_B + \delta \qquad , \tag{3.1.35}$$

where

$$\alpha = 1 - a_2(t) J_1(z_p)$$
 (3.1.36)

$$\beta = -a_1(t) J_1(z_p) - b(t) J_2(z_p) , \qquad (3.1.37)$$

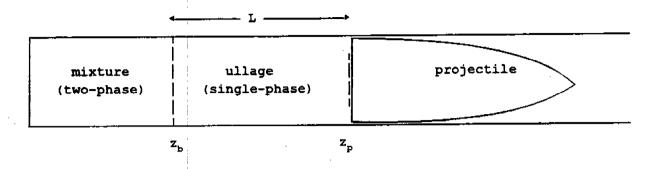
$$Y = \alpha + \frac{J_3(z_p) a_2(t)}{V(z_p)}$$
, (3.1.38)

$$\delta = \beta + \frac{J_3(z_p)a_1(t)}{V(z_p)} + \frac{b(t)J_4(z_p)}{V(z_p)} . \qquad (3.1.39)$$

3.2 Propellant Velocity Lag

In this section we explore the consequences of the inhomogeneity of the mixture. We note that the velocity of the solid-phase differs from that of the gas-phase. We seek to determine the effect on the pressure gradient of the propellant velocity lag as an isolated effect. Thus, in the present section we assume the cross-sectional area of the tube to be uniform, $\partial A/\partial z=0$. Moreover, we retain the basic Lagrange assumption that the density of the gas is uniform throughout the tube. However, since the propellant velocity lags that of the gas, we explicitly consider the consequences of the formation of a region of ullage between the propellant bed and the base of the projectile. The propellant is assumed to be distributed uniformly only over the region between the breech and the leading edge of the bed. Our formulation is intended to be applicable not only to granular propellant, for which the region of ullage is relatively small, but also, with the help of certain additional assumptions, to stick propellant which remains highly localized and for which the region of ullage becomes very large.

The assumed structure of the flow is illustrated in the following sketch which also introduces some nomenclature.



The position of the leading edge of the propellant bed is taken to be at z_b while the base of the projectile is at z_p , both positions relative to the breech face. The length of the ullage is $L = z_p - z_b$.

We may write the continuity equations for each of the phases in the mixture region in the form

$$\frac{\partial \varepsilon \rho}{\partial t} + \frac{\partial \varepsilon \rho u}{\partial z} = \dot{m}(t) \qquad (3.2.1)$$

$$\rho_{p} \frac{\partial \varepsilon}{\partial t} - \frac{\partial}{\partial z} (1 - \varepsilon) \rho_{p} u_{p} = \dot{m}(t) , \qquad (3.2.2)$$

where we have ϵ , porosity; ρ_p , propellant density; u_p , propellant velocity; and m, the rate of combustion of propellant. With respect to the gas-phase we have the traditional Lagrange assumption, which we will assume to apply throughout the tube, namely

$$\frac{\partial \rho}{\partial z} = 0 (3.2.3)$$

With respect to the solid phase we make the analogous assumption but we restrict it to the region occupied by the mixture, namely

$$\frac{\partial \varepsilon}{\partial z} = 0 \qquad . \tag{3.2.4}$$

In addition we assume that, within the mixture region, m is a function only of time even though, due to the pressure gradient, it must vary with position, too.

Evidently,

$$(1 - \varepsilon) \rho_{p} \frac{\partial u_{p}}{\partial z} = \frac{\partial \varepsilon}{\partial t} - \dot{m}(t) \qquad (3.2.5)$$

It therefore follows that $\mathbf{u}_{_{\mathbf{D}}}$ is a linear function of position and evidently

$$u_{p} = U_{p} \left[\frac{z}{z_{b}} \right] \qquad (3.2.6)$$

when the breech boundary condition $u_p(0) = 0$ is taken into account, and where $U_p = u_p(z_p)$ is the solid-phase velocity at the leading edge of the propellant bed.

Moreover:

$$\varepsilon \rho \, \frac{\partial \mathbf{u}}{\partial \mathbf{z}} = - \, \frac{\partial \varepsilon \rho}{\partial \mathbf{t}} + \dot{\mathbf{m}}(\mathbf{t}) \tag{3.2.7}$$

shows that within the mixture region u(z,t) continues to obey the Lagrange distribution

$$u = U_g(t) \left[\frac{z}{z_b} \right] , \qquad (3.2.8)$$

where $U_g = u(z_b)$ is the gas-phase velocity at the leading edge of the bed. The symbol U_g refers to the mixture side of the interface. Due to the discontinuity in porosity the gas velocity jumps discontinuously at the interface, at least from a macroscopic perspective.

The discontinuity in gas velocity is retained in the present formulation. However, we will ignore the concomitant jumps in the thermodynamic properties. The finite mass balance at the interface yields

$$\varepsilon (U_g - U_p) = U_{g_{\bullet}} - U_p \qquad , \tag{3.2.9}$$

where $U_{g_{i}}$ is the gas velocity on the ullage side of the interface. The continuity equation for the region of ullage may be written in the form

$$\frac{\partial \mathbf{u}}{\partial \mathbf{z}} = -\frac{1}{\rho} \frac{\mathbf{D}\rho}{\mathbf{D}\mathbf{t}} \qquad (3.2.10)$$

Since we retain the basic assumption of Lagrange, namely uniform density at all times, it follows that $D\rho/Dt$ is a function of time alone and we may write

$$U_{g+} = V_p + L \frac{D}{Dt} ln\rho$$
 (3.2.11)

where V_p is the projectile velocity and L is the length of the ullage. Combining (3.2.9) and (3.2.11) we have

$$U_g = U_p + \frac{1}{\epsilon} \left[V_p + L \frac{D}{Dt} \ln \rho - U_p \right]$$
 (3.2.12)

We will also require $\dot{\mathbf{U}}_{a}$ which we have as

$$\dot{\mathbf{U}}_{g} = \frac{\dot{\mathbf{V}}_{p}}{\varepsilon} - \frac{1 - \varepsilon}{\varepsilon} \dot{\mathbf{U}}_{p} - \frac{\dot{\varepsilon}}{\varepsilon^{2}} \left[\mathbf{V}_{p} + \mathbf{L} \frac{\mathbf{D}}{\mathbf{D}t} \ln \rho - \mathbf{U}_{p} \right] + \frac{\mathbf{L}}{\varepsilon} \frac{\mathbf{D}^{2}}{\mathbf{D}t^{2}} \ln \rho + \frac{\dot{\mathbf{L}}}{\varepsilon} \frac{\mathbf{D}}{\mathbf{D}t} \ln \rho \quad .$$
(3.2.13)

Equations (3.2.12) and (3.2.13) introduce the first and second time derivatives of the density. It is possible to express these derivatives algebraically and thereby to identify more precisely the dependence of the pressure gradient on the state variables. However, the formulation is made more complicated. For the present, therefore, we will simply assume that these derivatives can be furnished from the lumped parameter solution by means of numerical differentiation. This approximate treatment is expected to be adequate for granular propellant in which the region of ullage is expected to remain small at all times. The more complete analytical approach may prove necessary in the case of stick propellant for which the region of ullage becomes increasingly large as the projectile moves down the bore.

We now consider the momentum equations for the mixture region which we may express as

$$\frac{\partial \mathbf{u}}{\partial \mathbf{t}} + \mathbf{u} \frac{\partial \mathbf{u}}{\partial \mathbf{t}} + \frac{\mathbf{g}_0}{\rho} \frac{\partial \mathbf{p}}{\partial \mathbf{z}} = -\frac{\mathbf{f}_s}{\epsilon \rho} + \frac{\dot{\mathbf{m}}}{\epsilon \rho} (\mathbf{u}_p - \mathbf{u}) \qquad (3.2.14)$$

$$\frac{\partial u_p}{\partial t} + u_p \frac{\partial u_p}{\partial z} + \frac{g_0}{\rho_p} \frac{\partial p}{\partial z} = \frac{f_s}{(1 - \epsilon) \rho_p}$$
(3.2.15)

where f_s is the interphase drag and we assume the granular aggregate to be dispersed so that the intergranular stress σ_p = 0. To get the pressure gradient we need to specify f_s . We assume

$$f_s = \frac{1-\epsilon}{D_p} \rho (u - u_p)^2 \hat{f}_s$$
 (3.2.16)

where D_p is the effective grain diameter and \hat{f}_s is a dimensionless friction factor. In general, \hat{f}_s is a function of Reynolds number and particle shape and therefore of both z and t.

Equations (3.2.14) and (3.2.15) are better posed in divergence form as

$$\frac{\partial \varepsilon \rho u}{\partial t} + \frac{\partial \varepsilon \rho u^2}{\partial z} + \varepsilon g_0 \frac{\partial p}{\partial z} = -f_s + m u_p \qquad (3.2.17)$$

$$\frac{\partial}{\partial t} (1 - \epsilon) \rho_p u_p + \frac{\partial}{\partial z} (1 - \epsilon) \rho_p u_p^2 + (1 - \epsilon) g_0 \frac{\partial p}{\partial z} = f_s - m u_p , \qquad (3.2.18)$$

which can be obtained through the use of the continuity equations.

Adding (3.1.17) and (3.1.18) we see that

$$g_0 \frac{\partial p}{\partial z} = -\frac{\partial \epsilon \rho u}{\partial t} - \frac{\partial}{\partial t} (1 - \epsilon) \rho_p u_p - \frac{\partial \epsilon \rho u^2}{\partial z} - \frac{\partial}{\partial z} (1 - \epsilon) \rho_p u_p^2 \qquad (3.2.19)$$

We introduce the mass fraction burned, ϕ , so that

$$\varepsilon \rho = \frac{\phi C - \rho A_B L}{V(z_b)} = \frac{\phi_* C}{V(z_b)} \qquad (3.2.20)$$

where

$$\phi_{\bullet} = \phi (1 - \rho A_{B} L/C)$$
 (3.2.21)

Also,

$$(1 - \varepsilon) \rho_p = \frac{(1 - \phi)C}{V(z_b)}$$
, (3.2.22)

where C is total charge mass and $V(z_b)$ is the instantaneous volume of the region occupied by the mixture. We also note that

$$\dot{\phi}_{\bullet} = \dot{\phi} \left[1 - \frac{\rho A_B L}{C} \right] - \frac{\rho A_B \Phi}{C} \left[\dot{L} + L \frac{D}{Dt} \ln \rho \right] , \qquad (3.2.23)$$

$$\dot{\varepsilon} = \frac{\dot{\phi}C}{\rho_{p}V(z_{p})} + \frac{(1 - \phi)CA_{p}U_{p}}{\rho_{p}V^{2}(z_{p})} . \qquad (3.2.24)$$

In view of Equations (3.2.6), (3.2.8), (3.2.20) and (3.2.21), Equation (3.2.19) becomes

$$g_0 \frac{\partial p}{\partial z} = -\frac{\partial}{\partial t} \left[\frac{z}{z_b} \frac{C}{V(z_b)} \left[\phi_* U_g + (1 - \phi) U_p \right] \right]$$

$$-\frac{\partial}{\partial z} \left[\frac{z^2}{z_b^2} \frac{C}{V(z_b)} \left[\phi_* U_g^2 + (1 - \phi) U_p^2 \right] \right] \qquad (3.2.25)$$

Following expansion of the derivatives and simplification this becomes

$$g_0 \frac{\partial p}{\partial z} = -\frac{z}{z_b} \frac{C}{V(z_b)} \left[\phi_* \dot{U}_g + (1 - \phi) \dot{U}_p + \dot{\phi}_* U_g - \dot{\phi} U_p + \frac{2\phi_* U_g}{z_b} (U_g - U_p) \right] \qquad (3.2.26)$$

We may eliminate U_g by means of Equation (3.2.13). Also, we may express the solid-phase momentum equation in the form

$$\dot{\mathbf{U}}_{p} = \frac{1}{D_{p}} \frac{\rho}{\rho_{p}} \left[\mathbf{U}_{q} - \mathbf{U}_{p} \right]^{2} \hat{\mathbf{f}}_{s} - \frac{g_{0}}{\rho_{p}} \left[\frac{\partial \mathbf{p}}{\partial \mathbf{z}} \right]_{z} , \qquad (3.2.27)$$

which then allows us to eliminate $\dot{U}_{\rm p}$ from (3.2.26). We get

$$g_0 \frac{\partial p}{\partial z} = -\frac{z}{z_b} \frac{C}{V(z_b)} \left[\psi_1 - \psi_2 \frac{g_0}{\rho_p} \left[\frac{\partial p}{\partial z} \right]_{z_b} \right] , \qquad (3.2.28)$$

where

$$\psi_1 = \psi_1' + \frac{\Phi_*}{F} \dot{V}_P \qquad , \tag{3.2.29}$$

$$\psi_{1}' = \dot{\phi}_{\bullet} U_{g} - \dot{\phi} U_{p} - \dot{\phi}_{\bullet} \frac{\dot{\epsilon}}{\epsilon^{2}} \left[V_{p} + L \frac{D}{Dt} \ln \rho - U_{p} \right]$$

$$+ \frac{\Phi_{\bullet}}{\epsilon} \left[L \frac{D^{2}}{Dt^{2}} \ln \rho + \dot{L} \frac{D}{Dt} \ln \rho \right] + \frac{2 \phi_{\bullet} U_{g}}{z_{b}} \left[U_{g} - U_{p} \right]$$

$$+ \frac{\psi_{2}}{D_{p}} \frac{\rho}{\rho_{p}} \left[U_{g} - U_{p} \right]^{2} \hat{f}_{g} , \qquad (3.2.30)$$

$$\psi_2 = 1 - \phi - \phi_* \frac{(1 - \varepsilon)}{\varepsilon} \qquad . \tag{3.2.31}$$

Evidently,

$$\left[\frac{\partial p}{\partial z}\right]_{z_b} = -\frac{C}{g_0 V(z_b)} \frac{\psi_1}{1 - \frac{\psi_2 C}{\rho_p V(z_b)}}$$
(3.2.32)

Substituting back into (3.2.28) we have the following expression for the pressure gradient in the mixture region

$$\frac{\partial \mathbf{p}}{\partial z} = -\mathbf{k}_1(\mathbf{t})\mathbf{z} \qquad (3.2.33)$$

where

$$k_{1} = \frac{C}{g_{0}z_{b}V(z_{b})} \frac{\psi_{1}}{1 + \frac{\psi_{2}C}{\rho_{p}V(z_{b})}}$$
(3.2.34)

We note that k_1 depends on the base pressure $p_{\rm g}$ = $p(z_{\rm p})$ through the term $\dot{V}_{\rm p}$. We take the equation of motion of the projectile to be

$$\dot{\mathbf{V}}_{\mathbf{p}} = \frac{\mathbf{g}_{0} \mathbf{A}_{\mathbf{B}}}{\mathbf{M}_{\mathbf{p}}} \left[\mathbf{p}_{\mathbf{B}} - \mathbf{p}_{\mathbf{RES}} \right] \qquad (3.2.35)$$

Evidently, from Equations (3.2.29) and (3.2.35),

$$k_1 = k_{11}p_B + k_{12}$$
 (3.2.36)

where

$$\mathbf{k}_{11} = \frac{\mathbf{C}\Phi_{\bullet}\mathbf{A}_{\mathrm{B}}}{\mathbf{V}(\mathbf{z}_{\mathrm{b}})\mathbf{M}_{\mathrm{p}}\mathbf{z}_{\mathrm{b}}} \frac{\mathbf{k}_{2}}{\epsilon} \qquad (3.2.37)$$

$$k_2 = \frac{1}{1 - \frac{\psi_2 C}{\rho_p V(z_b)}},$$
(3.2.38)

$$k_{12} = \frac{C}{g_0 V(z_b)} \frac{k_2}{z_b} \psi_1' - k_{11} p_{RES}$$
 (3.2.39)

Then by integrating (3.2.33) we see that the pressure distribution within the mixture can be expressed in terms of p_{BR} and p_{B} as follows

$$p(z) = p_{BR} - \frac{z^2}{2} [k_{11}p_B + k_{12}]$$
 (3.2.40)

To complete the analysis we must now turn our attention to the pressure distribution in the region of ullage. The momentum equation for the gas in the ullage is

$$\frac{\partial \mathbf{p}}{\partial \mathbf{z}} = -\frac{\rho}{\mathbf{g}_0} \left[\frac{\partial \mathbf{u}}{\partial \mathbf{t}} + \mathbf{u} \frac{\partial \mathbf{u}}{\partial \mathbf{z}} \right] \qquad (3.2.41)$$

We note that the velocity distribution in the ullage varies linearly with distance between the value $U_{\rm g}$ at the mixture boundary and the value $V_{\rm p}$ at the projectile base. Evidently, from Equation (3.2.10),

$$u = V_p + (z_p - z) \frac{D}{Dt} In\rho$$
 (3.2.42)

Substitution into (3.2.41) and integrating yields the pressure distribution in the ullage in the form

$$p(z) = p(z_b) - \frac{\rho}{g_0} \left[\dot{V}_p + z_p \Delta \right] \left[z - z_b \right] - \left[z^2 - z_b^2 \right] \frac{\Delta}{2}$$
, (3.2.43)

where

$$\Delta = \frac{D^2}{Dt^2} \ln \rho - \left[\frac{D}{Dt} \ln \rho \right]^2 \qquad (3.2.44)$$

We note the implicit dependence on $p_{_{B}}$ through the term $\dot{V}_{_{p}}$ in (3.2.43).

From (3.2.40) and (3.2.43) we can now determine the spacemean pressure \widetilde{p} as

$$\overline{p} = p_{BR} \frac{z_b}{z_p} - k_1 \frac{z_b^3}{6z_p} + p(z_b) \frac{L}{z_p} - \frac{\rho}{g_0} \left[\dot{V}_p + \frac{2L\Delta}{3} \right] \frac{L^2}{2z_p} . \qquad (3.2.45)$$

We may eliminate $p(z_p)$ by means of (3.2.40). Also, V_p may be eliminated from (3.2.43) and (3.2.45) by means of (3.2.35). We note the tacit neglect of the pressure jump at the mixture boundary.

Following some straightforward manipulations we find the following relationships between \overline{p} , $p_{\rm RR}$ and $p_{\rm B}$.

$$\mathbf{p}_{BR} = \alpha \mathbf{p}_{B} + \beta \qquad , \tag{3.2.46}$$

$$\overline{p} = \gamma p_{R} + \delta \qquad , \qquad (3.2.47)$$

$$\alpha = 1 + \frac{z_b^2}{2} k_{11} + \frac{\rho L A_B}{M_D} , \qquad (3.2.48)$$

$$\beta = k_{12} \frac{z_b^2}{2} - \frac{\rho L A_B}{M_D} p_{RES} + \frac{\rho L^2 \Delta}{2g_0} \qquad (3.2.49)$$

$$\gamma = \alpha - \frac{k_{11}z_b^2}{2z_p} \left[\frac{z_b}{3} + L \right] - \frac{\rho A_B L^2}{2z_p M_p} , \qquad (3.2.50)$$

$$\delta = \beta - \frac{k_{12}z_b^2}{2z_p} \left[\frac{z_b}{3} + L \right] - \frac{\rho L^2}{2g_0z_p} \left[\frac{2L\Delta}{3} - g_0 \frac{A_B}{M_p} p_{RES} \right] \qquad (3.2.51)$$

We also note the total kinetic energy of the propellant and the combustion products. From Equations (3.2.6), (3.2.8) and (3.2.42) it follows that the kinetic energy is given by

$$KE = \frac{A_{B}z_{b}}{6g_{0}} \left[\epsilon \rho U_{g}^{2} + (1 - \epsilon) \rho_{p} U_{p}^{2} \right] + \frac{A_{B}\rho L}{6g_{0}} \left[3V_{p}^{2} + 3V_{p} L \frac{D}{Dt} ln\rho + L^{2} \left[\frac{D}{Dt} ln\rho \right]^{2} \right]$$
(3.2.52)

The foregoing may be used to make the lumped parameter energy equation consistent with the present two-phase analysis.

As we noted previously, the explicit recognition of the presence of the region of ullage allows the present two-phase analysis to be extended to the case of stick propellant. Two additional considerations are necessary. First, we must recognize that Equation (3.2.27) does not apply to stick charges because it neglects the important influence of the stress transmitted through the stick charge. Because stick propellant normally retains its mechanical

integrity, its length does not change appreciably during combustion. To apply the present analysis to stick charges we retain all the foregoing results with the exception of (3.2.27) as a means of determining the mixture boundary. Equation (3.2.27) is replaced by the assumption that $U_n = 0$ at all times and that the stick charge remains uniformly distributed between the breechface and the mouth of the tube throughout the interior ballistic cycle. NOVA Code simulations show this assumption to be reasonably good for single increment slotted stick charges, the type most commonly used. Since Equation (3.2.27) is equivalent to (3.2.15) it follows that some approximation must also be involved in the use of Equation (3.2.33) which is derived from (3.2.15). It is not difficult to see that (3.2.33) remains valid provided that p is viewed as the total stress, a sum of contributions due to the gas-phase pressure and the intergranular stress. The validating assumption in connection with the use of (3.2.33) for stick propellant is that the partial stress due to the intergranular forces is small by comparison with the pressure of the gas. Again, NOVA solutions show this assumption to be reasonable in cases of practical interest.

The second consideration relates to the burnout of the stick charge. NOVA solutions exhibit a pronounced wave propagation effect in relation to the influence of burnout on the pressure at the base of the projectile. This wave effect stems from two causes. First, the slotted stick has a rather neutral burning characteristic so that the rate of gasification is nearly constant right up to the instant of burnout. The flowfield is therefore required to adjust itself to a nearly instantaneous loss of a strong local source of combustion products. The adjustment is transient in nature and takes some time to propagate from the combustion chamber to the base of the projectile. Until the burnout wave reaches the base of the projectile the base pressure is relatively elevated and some performance enhancement can result if muzzle exit occurs prior to arrival of the wave.

We address this topic in an approximate manner. We assume that after burnout occurs for a stick charge the velocity distribution becomes bilinear. A hingepoint propagates from the mouth of the tube towards the base of the projectile at the local acoustic wavespeed. At the hingepoint the velocity distribution suffers a discontinuity of slope. We assume that this bilinear distribution can capture the effects of the primary burnout wave. We do not consider the implications of reflection of the wave from the base of the projectile. After the wave overtakes the projectile the velocity distribution is assumed to remain linear in accordance with the basic Lagrange assumption. Thus the approach taken here is intended to address stick charges for which overtaking of the projectile by the burnout wave either does not occur or else occurs shortly before muzzle exit.

Let t_b be the time at which burnout occurs and let $\dot{\varphi}_b$ be the fractional rate of consumption of the propellant at burnout. Let z_a and u_a respectively denote the position of the hingepoint and the local gas velocity. Evidently we will have to integrate the ordinary differential equation

$$\frac{dz}{dt} = u + c \qquad (3.2.53)$$

where c is the isentropic sound speed which we may approximate in terms of spacemean properties as

$$c = \sqrt{\frac{g_0 \overline{\gamma} \overline{p}}{(1 - bp)}} . \tag{3.2.54}$$

Here we have used $\overline{\gamma}$ as the ratio of specific heats, the overbar being used to avoid confusion with the term defined by Equation (3.2.50). We have used b to denote the covolume.

The initial condition for Equation (3.2.53) is taken to be

$$z_{\bullet}(t_{b}) = z_{p_{o}}$$
 (3.2.55)

Then the bilinear velocity distribution is given by

$$u(z) = \begin{cases} u_{*}z/z_{*} & , & 0 \le z \le z_{*} & , \\ \\ u_{*} + \frac{(V_{p} - u_{*})(z - z_{*})}{(z_{p} - z_{*})} & , & z_{*} \le z \le z_{p} & . \end{cases}$$
(3.2.56)

Following burnout, Equations (3.2.10) and (3.2.41) apply throughout the chamber and tube and may be used to construct the velocity and pressure distributions. However, we note a fundamental inconsistency between the Lagrange assumption of uniform density and the assumption of a bilinear velocity distribution after burnout. The bilinear distribution implies different values of $\partial u/\partial x$ and hence of $Dln\rho/Dt$ on each side of the hingepoint. After burnout the global mass balance, expressed in terms of the spacemean density, is

$$\frac{1}{\rho} \frac{D\rho}{Dt} = -\frac{A_B V_p}{V(z_p)} \qquad (3.2.57)$$

While we will use this equation to resolve values of density and rate of change of density in the subsequent analysis, we assume implicitly that the densities on each side of the hingepoint may differ from the spacemean value.

In front of the hingepoint the flow is adapting to the motion of the projectile but is still under the impression that the propellant is burning. Thus we have

$$\frac{1}{\rho} \frac{D\rho}{Dt} = -\frac{A_B V_p}{V(z_p)} + \dot{\phi}_b C \left[\frac{1}{\rho} - \frac{1}{\rho_p} \right] \qquad , \quad z_s \le z \le z_p \qquad . \quad (3.2.58)$$

From Equation (3.2.10) we may now identify the gas velocity at the hingepoint

$$u_* = V_p - (z_p - z_*) \left[\frac{A_b V_p}{V(z_p)} - \dot{\phi}_b c \left[\frac{1}{\rho} - \frac{1}{\rho_p} \right] \right] \qquad (3.2.59)$$

We may now construct the pressure distribution from the momentum equation, (3.2.41). We use (3.2.56), (3.2.59) and (3.2.35). We find

$$p(z) = \begin{bmatrix} p_{BR} - z^{2}(k_{34}p_{B} + k_{35}) & 0 \le z \le z_{*} \\ \\ p_{*} - (k_{51} + k_{52}p_{B})(z - z_{*}) - k_{53}(z^{2} - z_{*}^{2}) & z_{*} \le z \le z_{p} \end{bmatrix}$$

(3.2.60)

where p_{\bullet} is the pressure at the hingepoint. We also have introduced the following terms

$$k_{31} = 1 - (z_p - z_e) \frac{A_B}{V(z_p)}$$
 (3.2.61)

$$k_{32} = \frac{A_{B}V_{p}}{V^{2}(z_{p})} \left[A_{B}V_{p} + \frac{\phi_{b}C}{\rho_{p}} \right] , \qquad (3.2.62)$$

$$k_{33} = -\frac{(V_p - z_s)}{V(z_p)} \left[A_B V_p - \phi_b C \left[\frac{1}{\rho} - \frac{1}{\rho_p} \right] \right] , \qquad (3.2.63)$$

$$k_{34} = \frac{\rho A_B}{2M_p} \frac{k_{31}}{z_*} \qquad (3.2.64)$$

$$k_{35} = \frac{\rho}{2g_0 z_*^2} \left[\left[k_{32} (z_p - z_*) + k_{33} \right] z_* - u_* \dot{z}_* + u_*^2 \right] - k_{34} p_{RES} , \qquad (3.2.65)$$

$$k_{41} = 1 - \frac{(z_p - z)A_p}{V(z_p)}$$
 (3.2.66)

$$k_{42} = k_{32}$$
 (3.2.67)

$$k_{43} = -\frac{V_p}{V(z_p)} \left[A_B V_p - \dot{\phi}_b C \left[\frac{1}{\rho} - \frac{1}{\rho_p} \right] \right]$$
 (3.2.68)

$$\lambda = (V_p - u_*) / (z_p - z_*)$$
 (3.2.69)

$$k_{51} = \frac{\rho}{g_0} \left[k_{42} z_p + k_{43} + \lambda (u_{\bullet} - \lambda z_{\bullet}) \right] - k_{52} p_{RES} , \qquad (3.2.70)$$

$$k_{52} = \frac{\rho A_B}{M_p} k_{41}$$
 (3.2.71)

$$k_{53} = \frac{\rho}{2g_0} (\lambda^2 - k_{42})$$
 (3.2.72)

From Equation (3.2.60) we may eliminate p, and deduce

$$p_{BR} = \alpha p_B + \beta \qquad , \tag{3.2.73}$$

where

$$\alpha = 1 + z_{\bullet}^{2} k_{24} + k_{52} (z_{p} - z_{\bullet}) \qquad (3.2.74)$$

$$\beta = z_{\bullet}^{2} k_{35} + k_{51} (z_{p} - z_{\bullet}) + k_{53} (z_{p}^{2} - z_{\bullet}^{2}) \qquad (3.2.75)$$

Furthermore, integration of (3.2.60) and elimination of p_{a} and p_{BR} yields

$$\overline{p} = \gamma p_{R} + \delta \qquad , \tag{3.2.76}$$

where

$$\gamma = \alpha - \frac{z_{\bullet}^{3}}{3z_{p}} k_{34} - (z_{p} - z_{\bullet}) \frac{z_{\bullet}^{2}}{z_{p}} k_{34} - \frac{(z_{p} - z_{\bullet})^{2}}{2z_{p}} k_{52} , \qquad (3.2.77)$$

$$\delta = \beta - \frac{z_{\bullet}^{3}}{3z_{p}} k_{35} - \frac{(z_{p} - z_{\bullet})}{z_{p}} (k_{35} - k_{53}) z_{\bullet}^{2} - \frac{k_{51}}{2z_{p}} (z_{p} - z_{\bullet})^{2} - \frac{k_{53}}{3z_{p}} (z_{p}^{3} - z_{\bullet}^{3}) \qquad (3.2.78)$$

A similar approach has been used by Morrison and Coffee (1990) in an application to Regenerative Liquid Propellant Guns.

3.3 Area a Function of Position and Time

We now consider the continuity and momentum equations for unsteady flow of a homogeneous inviscid fluid through a tube with variable area A = A(z,t)

$$\frac{\partial A\rho}{\partial t} + \frac{\partial \rho Au}{\partial z} = 0 \qquad , \tag{3.3.1}$$

$$\rho \frac{\partial u}{\partial t} + \rho u \frac{\partial u}{\partial z} + g_0 \frac{\partial p}{\partial z} = 0 \qquad (3.3.2)$$

We assume that

$$A = A_e - A_i \qquad , \tag{3.3.3}$$

where $A_{\rm e}$ is the area of the tube, a function of z only, and $A_{\rm i}$ is the area defined by the local intrusion of the afterbody, a function of both z and t. We note that

$$\frac{\partial A}{\partial t} = -\frac{\partial A_i}{\partial t} \qquad (3.3.4)$$

and since A_i is constant in a frame moving with the projectile velocity $V_{_{\! D}}$

$$\frac{\partial \mathbf{A}}{\partial \mathbf{t}} = \mathbf{V}_{\mathbf{p}} \frac{\partial \mathbf{A}_{\mathbf{i}}}{\partial \mathbf{z}} \qquad . \tag{3.3.5}$$

We make the Lagrange assumption

$$\frac{\partial \rho}{\partial z} = 0 \qquad , \tag{3.3.6}$$

so that (3.3.1) becomes

$$\frac{\partial Au}{\partial z} = -\frac{A}{\rho} \frac{\partial \rho}{\partial t} - \frac{\partial A}{\partial t} \qquad (3.3.7)$$

As before, we note that

$$\rho V(z_p) = C ,$$

so that

$$\frac{1}{\rho} \frac{\partial \rho}{\partial t} = - \frac{1}{V(z_p)} \frac{\partial}{\partial t} V(z_p)$$

Also, we have

$$\frac{\partial}{\partial t} V(z_p) = \frac{\partial}{\partial t} \int_0^{z_p} A(z,t) dz$$

or,

$$\frac{\partial}{\partial t} V(z_p) = \int_0^{z_p} \frac{\partial A}{\partial t} dz + V_p A_B ,$$

where A_B is understood to be $A(z_p,t)$ and will not, in general, be the area of the tube. Equation (3.3.7) may be integrated with respect to z. Using the boundary condition u(0,t)=0 it follows that

$$A(z,t)u(z,t) = \frac{V(z,t)}{V(z_p,t)} \left[V_p A_p + \int_0^{z_p} \frac{\partial A}{\partial t} dz \right] - \int_0^{z} \frac{\partial A}{\partial t} \partial z \qquad (3.3.8)$$

Equation (3.3.8) may be compared with Equation (3.1.8). We note that (3.3.8) satisfies the boundary condition $u(z_p,t)=V_p$, as it must for consistency, independently of the form of $\partial A/\partial t$. No further progress or simplification can be made unless $\partial A/\partial t$ is specified. For the particular case of interest here we may make use of Equation (3.3.5) to deduce the result

$$A(z,t)u(z,t) = \frac{V(z,t)}{V(z_{p},t)} \left[A_{B} + A_{i}(z_{p},t) - A_{i}(0,t) \right] V_{p}$$

$$- \left[A_{i}(z,t) - A_{i}(0,t) \right] V_{p} \qquad (3.3.9)$$

If, moreover, $A_i(0,t) = 0$, as might be expected for this case, then

$$u(z,t) = \frac{V_p}{A(z,t)V(z_p,t)} \left[V(z,t)A_e(z_p,t) - V(z_p,t)A_i(z,t) \right] . \qquad (3.3.10)$$

As in Section 3.1 we could now proceed to determine the pressure distribution from the momentum equation. The formulism will, however, be complicated by the presence of the integrals of $A_i(z,t)$. Moreover, the equation of motion (3.1.32) will be complicated by the introduction of an integral of pressure over the intruding afterbody. Accordingly, further analytical results are not pursued.

3.4 Combined Effects of Area and Propellant Lag

We now attempt to combine the influence of variable area with that of propellant velocity lag. We assume that the variation in area is confined to the propellant chamber and that the propellant initially fills the chamber. Subsequently, a region of ullage may develop between the mixture and the base of the projectile. However, the cross-sectional area within the ullage is assumed to be constant and equal to $A_{\rm B}$ at all points. Attention is focussed principally on granular propellant although we comment on the applicability of the results to stick propellant at the end of the section. Nomenclature is as in the previous sections.

We have the continuity equations for each of the phases within the mixture region in the forms

$$\frac{\partial \varepsilon \rho}{\partial t} + \frac{1}{A} \frac{\partial \varepsilon \rho u A}{\partial z} = \dot{m}(t) \qquad (3.4.1)$$

$$\rho_{p} \frac{\partial \varepsilon}{\partial t} - \frac{1}{A} \frac{\partial}{\partial z} (1 - \varepsilon) \rho_{p} u_{p} A = \dot{m}(t) \qquad (3.4.2)$$

As in Section 3.2 we assume that within the mixture region

$$\frac{\partial \rho}{\partial z} = \frac{\partial \varepsilon}{\partial z} = 0 \qquad . \tag{3.4.3}$$

Moreover, the uniformity of the gas-phase density is assumed to extend throughout the tube and to apply in the region of ullage as well as in the mixture. Let the mixture boundary be at z_b and let the boundary values of the gas- and solid-phases be U_g and U_p respectively. Moreover, since $A(z_b) = A_B$ it follows from (3.4.1) and (3.4.2) that

$$u_{p}(z) = U_{p}\left[\frac{A_{p}}{A(z)}\right]\left[\frac{V(z)}{V(z_{b})}\right] \qquad (3.4.4)$$

$$u(z) = U_g \left[\frac{A_B}{A(z)} \right] \left[\frac{V(z)}{V(z_b)} \right] , \qquad (3.4.5)$$

The conditions in the region of ullage are unchanged from Section 3.2. Accordingly, Equations (3.2.9) through (3.2.13) are applicable here. To construct the pressure gradient in the mixture region we require the momentum equations which we may express in divergence form as

$$\frac{1}{A} \left[\frac{\partial}{\partial t} A \epsilon \rho u + \frac{\partial}{\partial z} A \epsilon \rho u^2 \right] + \epsilon g_0 \frac{\partial p}{\partial z} = -f_s + m u_p , \qquad (3.4.6)$$

$$\frac{1}{A} \left[\frac{\partial}{\partial t} A(1-\epsilon) \rho_p u_p + \frac{\partial}{\partial z} A(1-\epsilon) \rho_p u_p^2 \right] + (1-\epsilon) g_0 \frac{\partial p}{\partial z} = f_s - m u_p \qquad (3.4.7)$$

As in Section 3.2 we assume that intergranular stresses can be neglected. By adding (3.4.6) and (3.4.7) we get

$$g_{0} \frac{\partial p}{\partial z} = -\frac{1}{A(z)} \frac{\partial}{\partial t} \left[A(z) \varepsilon \rho u + A(z) (1 - \varepsilon) \rho_{p} u_{p} \right]$$

$$-\frac{1}{A(z)} \frac{\partial}{\partial z} \left[A(z) \varepsilon \rho u^{2} + A(z) (1 - \varepsilon) \rho_{p} u_{p}^{2} \right] .$$
(3.4.8)

If we now introduce ϕ , the mass fraction burned, we see that the previous relations (3.2.20) through (3.2.24) are applicable here. Thus we may substitute (3.2.20) and (3.2.22) together with (3.4.4) and (3.4.5) into (3.4.8) to get the result

$$g_{0} \frac{\partial p}{\partial z} = -\frac{CA_{B}V(z)}{A(z)} \frac{\partial}{\partial t} \left[\frac{\phi_{\bullet}U_{g}}{V^{2}(z_{b})} + \frac{(1-\phi)U_{p}}{V^{2}(z_{b})} \right]$$

$$-\frac{CA_{B}^{2}}{A(z)V^{3}(z_{b})} \left[\phi_{\bullet}U_{g}^{2} + (1-\phi)U_{p}^{2} \right] \frac{\partial}{\partial z} \frac{V^{2}(z)}{A(z)}$$

$$(3.4.9)$$

Following expansion of the derivatives and simplification we get

$$g_{0} \frac{\partial p}{\partial z} = -\frac{CA_{B}V(z)}{A(z)V^{2}(z_{b})} \left[\phi_{a}\dot{U}_{g} + (1 - \phi)\dot{U}_{p} + \dot{\phi}_{a}U_{g} - \dot{\phi}U_{p} + \frac{2A_{B}}{V(z_{b})} \phi_{a}U_{g} \left[U_{g} - U_{p} \right] - \frac{A_{B}V(z)}{V(z_{b})A^{2}(z)} \frac{\partial A}{\partial z} \left[\phi_{a}U_{g}^{2} + (1 - \phi)U_{p}^{2} \right] \right]$$
(3.4.10)

It is easy to verify that when $A(z) = A_B$ so that $V(z) = A_B z$, then (3.4.10) reduces to (3.2.26) as it should. On the other hand, when $\phi = \phi = 1$, $z_b = z_p$, L = 0, $U_q = U_p = V_p$, then (3.4.10) reduces to (3.1.10).

As in Section 3.2 we proceed to eliminate \dot{U}_g from (3.4.10) using (3.2.13). Similarly, we use (3.2.27) to eliminate \dot{U}_p . We find

$$g_0 \frac{\partial p}{\partial z} = -\frac{V(z)}{A(z)} \frac{CA_B}{V^2(z_b)} \left[\psi_1 - \psi_2 \frac{g_0}{\rho_p} \left[\frac{\partial p}{\partial z} \right]_{z_b} - \psi_3 \frac{A_B}{V(z_b)} \frac{V(z)}{A^2(z)} \frac{\partial A}{\partial z} \right] , \quad (3.4.11)$$

where

$$\psi_1 = \psi_1' + \frac{\Phi_*}{F} V_p$$
 (3.4.12)

$$\begin{split} \psi_{1}' &= \dot{\phi}_{\bullet} U_{g} - \dot{\phi} U_{p} - \phi_{\bullet} \frac{\dot{\epsilon}}{\epsilon^{2}} \left[V_{p} + L \frac{D}{Dt} \ln \rho - U_{p} \right] + \frac{\dot{\phi}_{\bullet}}{\epsilon} \left[L \frac{D^{2}}{Dt^{2}} \ln \rho + \dot{L} \frac{D}{Dt} \ln \rho \right] \\ &+ 2 \dot{\phi}_{\bullet} U_{g} \frac{A_{B}}{V(\dot{z}_{b})} \left[U_{g} - U_{p} \right] + \frac{\psi_{2}}{D_{p}} \frac{\rho}{\rho_{p}} \left[U_{g} - U_{p} \right]^{2} \hat{f}_{s} \end{split}$$

$$(3.4.13)$$

$$\psi_2 = 1 - \phi - \phi_* \frac{(1 - \epsilon)}{\epsilon}$$
 (3.4.14)

$$\psi_3 = \phi_* U_g^2 + (1 - \phi) U_p^2 \qquad . \tag{3.4.15}$$

It should be noted that (3.4.12) through (3.4.14) are identical with (3.2.29) through (3.2.31) except for the penultimate term of (3.4.13). By setting $z = z_b$ in (3.4.11) we may solve for $(\partial p/\partial z)_{z_b}$. Recalling that $(\partial A/\partial z)_{z_b} = 0$ we find

$$\left[\frac{\partial \mathbf{p}}{\partial z}\right]_{z_{b}} = -\frac{C}{g_{0}V(z_{b})} \frac{\psi_{1}}{1 - \frac{\psi_{2}C}{\rho_{p}V(z_{b})}},$$
(3.4.16)

which is identical to (3.2.32). We may substitute (3.4.16) into (3.4.11), integrate with respect to z, and use (3.2.25) to eliminate \dot{V}_p from ψ_1 to get the following relation for the pressure in the mixture

$$p(z) = p_{BR} + \left[a_1(t) + a_2(t)p_B \right] J_1(z) + b(t)J_2(z) , \qquad (3.4.17)$$

where $J_1(z)$ and $J_2(z)$ are defined by Equations (3.1.17) and (3.1.18) and we have

$$a_{1}(t) = \frac{CA_{B}}{g_{0}V^{2}(z_{b})} \left[\frac{\psi_{3}A_{B}}{V(z_{b})} - \frac{\psi_{1}' - \frac{g_{0}A_{B}}{M_{p}} \frac{\phi_{*}}{\varepsilon} p_{RES}}{1 - \frac{\psi_{2}C}{\rho_{p}V(z_{b})}} \right], \qquad (3.4.18)$$

$$a_2(t) = -\frac{CA_B^2}{M_p V^2(z_b)} \frac{\phi_*}{\epsilon} \left[1 - \frac{\psi_2 C}{p_p V(z_b)} \right]^{-1}$$
, (3.4.19)

$$b(t) = -\frac{C\psi_3}{2g_0} \frac{A_B^2}{V^3(z_b)} \qquad (3.4.20)$$

In the ullage the pressure distribution is unchanged from the form deduced in Section 3.2; thus Equation (3.2.43) applies. The procedure outlined in Sections 3.1 and 3.2 may be followed here. The spacemean pressure is assumed to be area-weighted as in Section 3.1 We deduce

$$p_{BR} = \alpha p_B + \beta \qquad , \tag{3.4.21}$$

where

$$\alpha = 1 - a_2(t) J_1(z_b) + \frac{\rho A_B L}{M_o}$$
, (3.4.22)

$$\beta = -a_1(t) J_1(z_b) - b(t) J_2(z_b) - \frac{\rho A_B L}{M_D} p_{RES} + \frac{\rho L^2 \Delta}{2g_0} , \qquad (3.4.23)$$

and,

$$\overline{p} = \gamma p_B + \delta \qquad , \tag{3.4.24}$$

where

$$Y = \alpha + \frac{a_2(t)}{V(z_p)} \left[J_3(z_b) + A_B L J_1(z_b) \right] - \frac{\rho A_B^2 L^2}{2M_p V(z_p)} , \qquad (3.4.25)$$

$$\delta = \beta + \frac{a_1(t)}{V(z_p)} \left[J_3(z_b) + A_B L J_1(z_b) \right] + \frac{b(t)}{V(z_p)} \left[J_4(z_b) + A_B L J_2(z_b) \right] - \frac{\rho A_B L^2}{2 g_0 V(z_p)} \left[\frac{2 L \Delta}{3} - \frac{g_0 A_B P_{RES}}{M_p} \right] , \qquad (3.4.26)$$

We have introduced $J_3(z)$ and $J_4(z)$ as defined by Equations (3.1.20) and (3.1.21). Under the stated assumptions of the present section it follows that $V(z_p)$ and $J_1(z_p)$, $J_2(z_p)$, $J_3(z_p)$, $J_4(z_p)$ may be evaluated according to Equations (3.1.24) through (3.1.28) with z_b replacing z_p in the evaluation of the J_1 terms, $i=1,\ldots,4$.

We have tacitly assumed that we were dealing with granular propellant. As in Section 3.2, however, the present analysis is applicable to stick charges provided that the same approximations can be made. Moreover, the analysis of the pressure gradient subsequent to burnout of the stick charge can be treated as in Section 3.2. The only modification is the replacement of a linear velocity distribution behind the hingepoint by the form expressed in Equation (3.4.5). Further results may be found in a report by Robbins et al (1990).

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Appendix A:

XNOVAKTC (XKTC)—Structure and Use

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INTRODUCTION

Our intention in this Appendix is to provide the user of the code with some understanding of its macrostructure and full details of the specification of input data. We do not attempt to document the code in such detail as to permit revisions by the user. XKTC is an extension of NOVATC, XNOVAT and XNOVAK which are, in turn, extensions of the express version of the NOVA Code known as XNOVA. XNOVA is a subset of the NOVA Code and certain of the details of the original versions of the NOVA Code which were deleted in the preparation of XNOVA are also absent from its successors XNOVAK and XNOVAT. Discussions of the structure of NOVA, NOVATC, XNOVA, XNOVAK and XNOVAT may be found in earlier reports (Gough, 1980a,1981,1983a,1983b,1984,1985). Although we provide a complete tabulation of the present set of code subroutines and functions, our general discussion is confined to the differences between the current version of XKTC and its predecessors, including the previous version (Gough, 1986a).

The discussion of structure and of input is contained in the two following Sections. Before proceeding, however, we wish to draw the user's attention to certain general restrictions on the use of the code.

First, it should be noted that existing NOVA, XNOVA and NOVATC data bases cannot always be read by XNOVAK, XNOVAT or XKTC. Although we always attempt to maintain data base compatibility between the various code versions, XNOVAK, XNOVAT and XKTC do require a minor change to pre-existing data bases. File [M4], described in Table A.6, always consists of two cards in XNOVAK/XNOVAT/XKTC data sets. Pre-existing NOVA, XNOVA and NOVATC data sets in which File [M4] consisted of just one card may be made compatible with XNOVAK/XNOVAT/XKTC by the incorporation of a single blank card following the pre-existing File [M4]. No change is required to pre-existing data bases for which [M4] already consisted of two cards. A corresponding revision to XNOVAK/XNOVAT/XKTC data bases is required if they are to be run on NOVATC, XNOVA or NOVA. However, all XNOVAK data bases can be read by XNOVAT and XKTC.

Second, in regard to the summarized solution histories given at the conclusion of each run, it should be noted that the energy defect calculation does not presently support the full chemistry option. If intermediate combustion products are present, the tabulated energy defect may become quite large. Only the mass defect can be depended upon to gage the accuracy of the numerical solution in such cases. The single exception to this statement is that of the traveling charge with a finite flame thickness. In this special case, where there is just one intermediate species, the energy defect calculation reflects the chemical energy stored in the intermediates. Moreover, in this special case, the mass fraction calculation for propellant type three in the summary table is used to tabulate the ratio of the mass of the unburned intermediates to that of the original traveling charge increment.

STRUCTURE AND LINKAGES

A complete summary of the routines and their linkages is given in Table A.1. The overall macrostructure is unchanged from that of XNOVA as documented by Gough (1983b). The following brief comments provide a summary of the routines which were added to XNOVA to produce XNOVAK, the revisions which subsequently transformed XNOVAK into XNOVAT, the amalgam of XNOVAT and BRLTC (Gough, 1980b) to produce the previous version of XKTC, and the amalgam of XKTC and RLPTC (Gough, 1988) to produce the current version. We note that the current version is intended for use on 32-bit word machines and is therefore written in double precision.

Routines Added in Preparation of XNOVAK

XNOVAK was developed as an extension of XNOVA. Accordingly, XNOVA is a subset of both XNOVAK and NOVA. Moreover, in developing XNOVAK it was found necessary to restore certain capabilities which had been removed from NOVA during the preparation of XNOVA. Specifically, we restored the invariant embedding solution for the thermal response of the solid propellant. Thus, in addition to the capabilities of XNOVA, XNOVAK and NOVA also share a transient combustion modeling capability.

The NOVA routines restored to XNOVAK were CMBUST, FEAK, IMBED and ROOT together with necessary I/O linkages. The routines were then modified to support the XNOVAK features of subsurface reactivity and the evaporative boundary condition. New routines added to support the kinetics option included CHEMR, CHEMRS, CONLOS, COVC and GAMMOL. The new routine FILLBR implements the analysis of the rear filler elements and was created by making appropriate editing changes to the pre-existing routine FILLER. One additional routine, AVN, was included for the purpose of documenting Code revisions and printing the version number on each run.

Routines Added in Preparation of XNOVAT

Several routines were required to produce XNOVAT. Subroutine INTRPC determines the rate of combustion of the reactive layers ascribed to the tube wall, the centerline, and the projectile afterbody. To support the new form functions we have added the routines BLSL, HEX19, and SLIVER. To treat the reactivity and flow resistance of the endwalls of the bundles of propellant we added the routines CALFLO, CALPRM, FLUX, FLUXDR and TDBCAL, all of which were adapted from the TDNOVA Code (Gough, 1983c). The routine TDBUF acts as a link between the existing boundary value solver BCAL and the routine TDBCAL. In addition we added the routines JCON, SETSUB and RCASE which perform various utility functions.

Structure of NOVATC

XKTC was essentially formed by substituting XNOVAT in place of XNOVA in the previously developed NOVATC Code (Gough, 1983a). As we have previously discussed, NOVATC is an amalgam of XNOVA and BRLTC (Gough, 1980b, 1983b).

In forming the amalgam care was taken to minimize cross-contamination of the coding. The approach was to take BRLTC and delete all references to the flow behind the base of the traveling charge while retaining the storage, data reads and processing pertinent to the regression of the surface, the traveling charge and the projectile. This stripped down code was linked to a complete version of XNOVA (Gough, 1983b) in which a minimal number of linking subroutine calls were placed. Although a more tightly written code could have been developed it would have been more difficult to maintain such a code in a form compatible with future versions of XNOVA and BRLTC. Also, it is the case that XNOVA and BRLTC have many variables whose Fortran names are identical, but whose meanings differ and, conversely, some variables with different names but identical meanings.

It will be noted in Table A.1 that all routines pertinent to the traveling charge have the prefix TC. A single routine, TCLINK, has the function of reconciling the storage conventions of the two codes and of passing data between them. Processing follows the usual NOVA conventions with the traveling charge logic activated at a number of places. NOVSUB calls TCDATA and TCLINK to read and initialize data. INTEG calls TCLINK, TCOUT to print the solutions and TCBR4 to determine the traveling charge time step constraint. INTAL calls TCLINK and TCXC, the main integration executive for the traveling charge. TABLES calls TCLINK. It was also necessary to restructure slightly the routines BCAL and BDMOV.

Routines Added in Preparation of Previous Version of XKTC

The approach followed in the development of NOVATC made the replacement of XNOVA by XNOVAT fairly straightforward. It should be noted, however, that the present effort involved substantial exercising of the algorithm and several revisions were made to the analysis of the boundary values at the base of the burning traveling charge. Accordingly, the versions of TCLINK and TCBASE used here differ from those in earlier versions of NOVATC.

Apart from linking the kinetics, tank gun and traveling charge options in a physically complete fashion, it was necessary to add several new routines in the development of XKTC. Subroutine GETLS computes the values of L' for the intermediate products of combustion of the traveling charge. ATACH enforces the attachment of a propellant type to the tube or to the projectile.

Routines Added in Preparation of Present Version of XKTC

The revisions described in the main body of the present report have not entailed the addition of many new subroutines. Subroutines EXCW, FRACT and REG21A have been added to support the explicit analysis of an intergranular shock wave and the effects of grain fracture. The bulk of the new routines have been required in order to effect the amalgam with the RLPTC Code to support the modeling of charges with a traveling liquid propellant component. The approach to the amalgam with RLPTC was perfectly analogous to that described above in connection with BRLTC. The RLPTC routines added to XKTC are all prefaced with the letters TLC. Gough (1988) may be consulted for a table indicating the precise correspondence between the TLC - routines and their RLPTC counterparts. A new routine TLCLNK performs the task of linking the TLC storage with that of XKTC.

Finally, we note that the present version of XKTC includes those revisions made for the Navy to permit the modeling of inbore rockets (Gough, 1986b) and a linkage to the plasma model of Powell and Zielinsky (1992).

DESCRIPTION OF INPUT FILES

We preface the detailed description of the input file structure with some general observations. We note, in particular, the nomenclature for the definition of the geometry of the propelling charge.

Figure A.1 illustrates a charge configuration with does not make use of the tank gun option (MODET = 0). We illustrate the base of the projectile, an arbitrary number of filler elements -- some at the rear and some at the front of the charge -- and two types of propellant, the first of which is in two increments, the latter increment overlapping that of the second propellant. The figure also illustrates the significance of the input data ZGR, XEL, XBL and ZBPR.

Figure A.2 illustrates a charge configuration which does make use of the tank gun option (MODET = 1). We illustrate the intrusion of the projectile afterbody into the combustion chamber, the reactive layers on the tube wall, the centerline and the projectile afterbody, and three types of propellant, the first of which is present as two increments. To the rear of the afterbody we represent the three types of propellant as being parallel packaged and we illustrate the significance of the input data RGRI and RGRO.

Figures A.1 and A.2 both assume that the propellant is of the conventional type. Figure A.3 illustrates a charge configuration in which a solid propellant traveling charge is present. We note that the traveling charge may consist of several increments, each having distinct mechanical and thermochemical properties. The simulation of the traveling charge may be performed

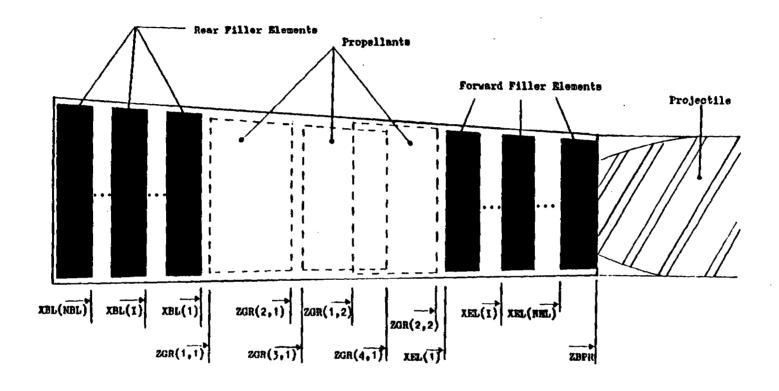
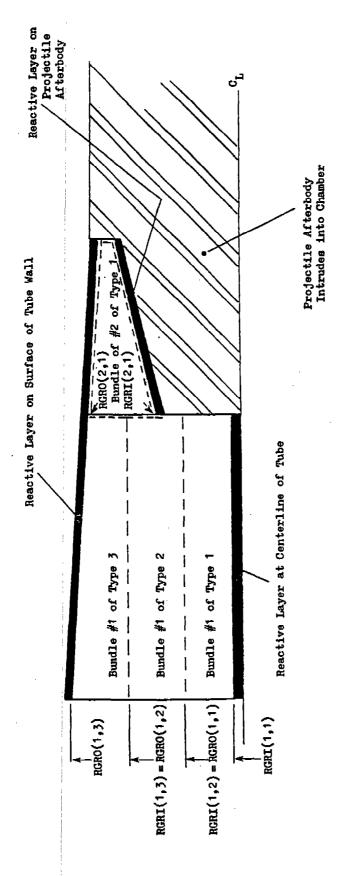


Figure A.1 Nomenclature for Definition of Charge Configuration in XKTC with MODET = 0.



Nomenclature for Definition of Charge Configuration in XNOVAT with MODET = 1. Figure A.2

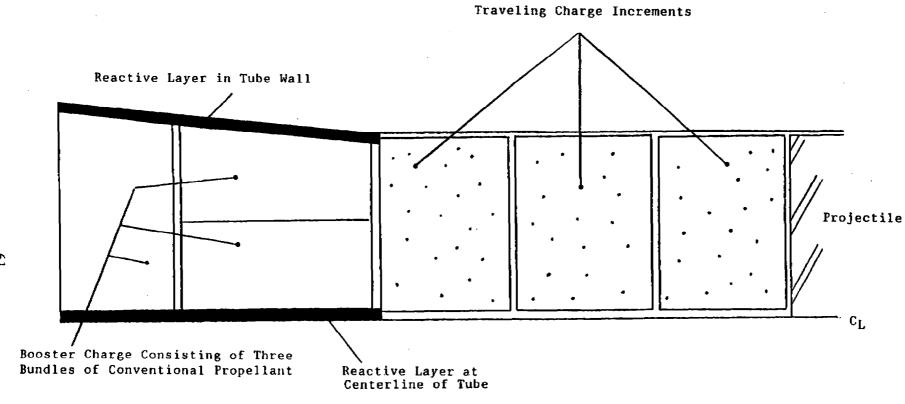


Figure A.3 Example of a Hybrid Charge Consisting of Conventional and Traveling Charge Increments.

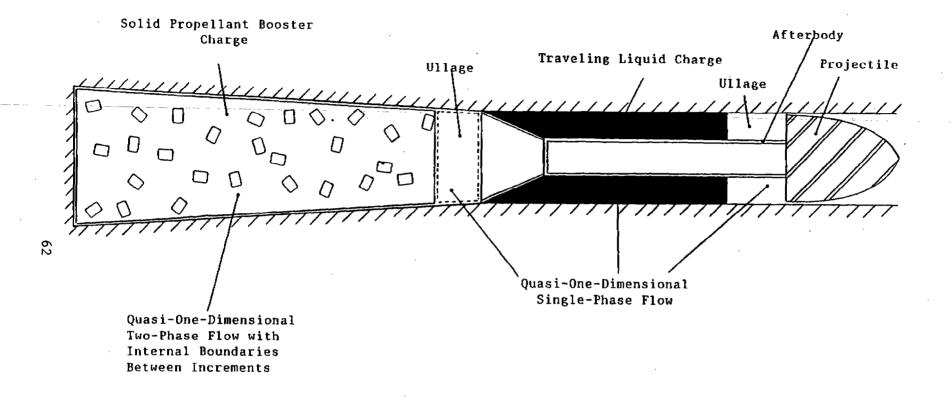


Figure A.4 Example of Hybrid Charge Consisting of Traveling Liquid Propellant and Solid Propellant Booster.

in conjunction with an arbitrarily configured conventional charge. It is assumed, however, that when the traveling charge is present there are no compactible filler materials at the front of the chamber, as in Figure A.1, and that the projectile does not have an afterbody as in Figure A.2. Reactive sidewalls may nevertheless be present, as shown in Figure A.3.

Figure A.4 illustrates a charge configuration in which a liquid propellant traveling charge is present. The solid propellant booster is permitted to take any of the configurations compatible with the solid propellant traveling charge. Figure A.4 shows a projectile with an afterbody which stabilizes the traveling liquid charge and allows the propellant to vent at the rear face. In the representation of Figure A.4 it is tacitly assumed that the discharged liquid propellant is fully burned within a negligibly short time so that the mass transferred to the booster region consists of final products of combustion. Gough (1988) may be consulted for further details.

Input to XKTC consists of XNOVAT data followed by a subset of the BRLTC data base when the solid propellant traveling charge option is selected in the control data field of XKTC and by a subset of the RLPTC data base when the liquid propellant traveling charge option is exercised. Tables A.2, A.3, A.4 and A.5 enumerate the "Mandatory", Contingent, Traveling Charge and Traveling Liquid Charge data files. The files prefixed with an M are always mandatory in XNOVAT. Here, File [M13] is optional. We have retained the file labels of XNOVAT, in spite of this minor inconsistency, to promote commonality among the various codes.

The enumeration of the M and C files follows that for the NOVA code. We have attempted to maximize the compatibility of XKTC, XNOVAT, XNOVAK, XNOVATC, XNOVA and NOVA data bases. As noted in the introduction to this appendix, compatibility is complete with the possible exception of File [M4]. In XKTC, XNOVAT and XNOVAK, File [M4] always consists of two cards. In XNOVATC, XNOVA and NOVA it may consist of either one or two cards. Existing NOVATC, XNOVA and NOVA data sets for which File [M4] consists of only one card may be made compatible with XKTC, XNOVAT and XNOVAK by the insertion of a single blank card after the existing [M4] data card. NOVA files not supported by XKTC, XNOVAT and XNOVAK are read and subsequently ignored. The tabulation of data by XKTC only includes those elements which are supported.

All mandatory files, Table A.2, are common to all codes. However, not all the members of every file are supported by XKTC, XNOVAT and XNOVAK. The detailed definition of the input files given in Table A.6 describes all the elements which are supported and simply denotes the others as "Inactive." Those contingent files, Table A.3, which are supported are defined while the others are denoted as "not supported." Only those contingent files which are supported by XKTC appear in the detailed discussion of Table A.6.

The program input files are structured to permit the running of only one problem at a time. A problem may be restarted from disc, provided suitable options have been selected in a prior run. Each problem may be terminated according to a criterion of number of integration steps, projectile displacement or problem time. Termination occurs at whichever of the three criteria is first satisfied. However, if the blowdown option is exercised the projectile displacement criterion does not serve to terminate the calculation. The muzzle is assumed to be open when the specified displacement is reached and termination is subsequently based on number of integration steps, problem time, or breech pressure, whichever is satisfied first.

It should be noted that file counters are edited by subroutine NOVSUB to establish their conformality with internal storage dimensions. However, other data are not edited, and it is recommended that the program user perform a first run on a new problem with termination set to follow initial set-up, so that all data may be validated.

The following notes (1) - (10) apply whether or not the traveling charge option is exercised. Subsequent notes (11) - (16) pertain to the traveling charge option. Note (17) applies to the inbore rocket motor option. Notes 18 and 19 apply to the traveling liquid charge option.

- (1) For problems involving only granular propellant, the representations of the grain distributions are arbitrary. The granular propellants may doubly or triply overlap. However, a region occupied by stick propellant may not be shared by any other type unless MODET = 1. If MODET = 1, it is permissible to have an increment of stick propellant parallel packaged with another increment of stick or granular propellant. The monolithic charge is not permitted to share a cross-section of the tube with any other type. If a given type is specified as bonded to the tube or projectile, the bonding will be presumed to apply to any other propellant which shares a region with the given type.
- (2) The mode of representation of one type of propellant is independent of the mode of representation of any other. If tables of volume fractions are used, it should be recalled that the volume fraction is the complement of the porosity, being zero when no propellant is present and increasing to unity as the pore volume vanishes. The volume fraction defaults to zero outside the range of positions defined by the tables.
- (3) An internal boundary is identified at any location in which any volume fraction is discontinuous. Thus an internal boundary may be established at a point at which the porosity is continuous.

- (4) Absolutely no restrictions, other than that on note (1), are placed on the relative positions of the bags of propellant. After the data are read, they are all converted internally to volume fraction tables. These are all then scanned to create a list of internal boundary positions. This list is then sorted to put them into order and to define the computational regions.
- (5) The right-hand boundary is always set equal to XEL(1). If NEL = 0, XEL(1) defaults to ZBPR. Similarly, the left-hand boundary is always set equal to XBL(1). If NBL = 0, XBL(1) defaults to zero. It should be noted that the configuration of the forward elements is specified by reference to the position of the left-hand or rear boundary of each element. Conversely, the configuration of the rear elements is specified by reference to the position of the right-hand or forward boundary of each element. In both cases the elements are ordered so that the first is closest to the propelling charge.
- (6) Although filler elements may be included if MODET = 1, the coding does not consider the influence of the afterbody on the behavior of the filler elements.
- (7) It is emphasized that every case closure element must be accounted for, including spaces. Any element, other than the first, may be entered as a space by setting its mass equal to zero.
- (8) It is noted that one may use a single element to represent more than one physical component and that conversely, one may use several elements to characterize a single component.
- (9) The present storage allocation in the code imposes certain restrictions on the modeling of subsurface reactions in the propellant. It is assumed that only one type of propellant is present if an invariant embedding solution of the thermal response is desired (KMODE = 2 in File [M2]). At most 21 stations are permitted for the analysis of the thermal response. At most two chemical species can be associated with the subsurface chemistry. While these limits are thought to be adequate for present needs, they may readily be relaxed by means of changes in certain dimension statements.
- (10) It will be noted that the data required when KMODE # 0 Files [C23.1] [C23.6] are to some extent already provided by the data of Files [M7] -[C7]. The latter data are superseded in such a case and consistency between the two sets of data is not essential. However, inconsistencies may yield an apparent energy defect in the summarized interior ballistics table.
- (11) Unit 9 is reserved for storage of the traveling charge data if disk logout is specified.

- (12) The code does not support the traveling charge option simultaneously with the compactible case closure option. It is also assumed that the projectile has no afterbody if the traveling charge option is exercised.
- (13) The code termination data are always specified according to the NOVA format. The projectile data follow the NOVA format only if the traveling charge option is not in effect.
- (14) Due to the cross-linking of the codes, no more than KQ-2 mesh points and no more than 9 increments can be specified for the booster region when the traveling charge option is in effect. Here KQ is the dimension of the XKTC storage arrays, currently set equal to 999 by a PARAMETER statement.
- (15) A composition dependent covolume is not considered. The covolume for the calculation is presently based on the booster charge data according to the NOVA convention.
- (16) The gun tube is assumed to have a constant area in the region occupied by the unreacted traveling charge.
- (17) If an inbore rocket motor is present it is assumed that there are no forward filler elements, that the projectile has no afterbody and that no booster increments are attached to the projectile.
- (18) The base of the traveling liquid charge is assumed to be permeable to the gas-phase if a cavity is present, but impermeable to the solid propellant booster charge.
- (19) A region of ullage is assumed to exist at all times between the booster charge and the base of the traveling liquid charge. It is therefore recommended that the input datum RZOLV be less than or equal to 0.01. See the discussion of File [M3] in Table A.6.

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TABLE A.1 SUMMARY OF ROUTINES AND LINKAGES

XKTC Purpose XKTC is a dummy main routine which immediately

transfers control to NOVSUB.

Calls: NOVSUB.

Called by: None.

AFTSET Purpose: Subroutine AFTSET performs region management in the

case when the base of the afterbody of the projectile

is represented as an explicit discontinuity.

Calls: OUTPUT.

Called by: MESH, NOVSET.

ATACH Purpose: Subroutine ATACH enforces the attachment of a charge

increment to either the tube or the projectile.

Calls: None.

Called by: INTAL.

AVN Purpose: Subroutine AVN is used to document code revisions

and print the version number.

Calls: None.

Called by: NOVSUB.

BCAL Purpose: Subroutine BCAL accepts trial boundary values for

the gas- and solid-phases and adjusts them so as to satisfy simultaneously the physical and character-

istic boundary conditions.

Calls: COVC, EPTOR, EXCW, GAMMOL, GRLOAD, LUMPS, OUTPUT,

PRTOC, PRTOE, RHEO, TABLES, TDBUF.

Called by: INTAL.

BDMOV Purpose: Subroutine BDMOV updates the position of the region

boundaries. It also updates the projectile

displacement and velocity, making use of FILLER

and/or FILLBR when case closure elements are present.

Calls: EXCW, FILLBR, FILLER, FRATE, GMOVE, RCASE, RESFUN,

RHEO.

Called by: INTAL, OUTPUT, TABLES.

BLKDAT Purpose: BLKDAT performs block data initialization.

Calls: None.

Called by: None.

BLSL Subroutine BLSL computes the volume and surface Purpose:

area for the blind slit form function during the

slivering phase.

Calls:

None.

Called by:

FORM.

BRNOUT

Subroutine BRNOUT detects the instant when all the Purpose:

propellant has been consumed and then consolidates

all the computational regions into a single region

with uniform mesh spacing.

Calls:

FITSP, REG21.

Called by:

None.

CALEOS

Subroutine CALEOS calculates specific heats and Purpose:

enthalpy according to formulation of NASA SP-273.

Calls:

None.

EPTOR, ERTOP, FRICT, HEATP, HEATW, INTAL, INTRPC, Called by:

LUMPS, NOVSET, NOVSUB, PRTOE.

CALFLO Purpose: Subroutine CALFLO computes the rate of reaction of

the surface fluxes associated with the endwalls of

the charge increments.

Calls:

None.

Called by:

TDBUF.

CALPRM

Purpose:

Subroutine CALPRM computes the flow resistance co-

efficient for the endwalls of the charge increments.

Calls:

None.

Called by:

TDBUF.

CHEMR

Purpose:

Subroutine CHEMR computes the effects of chemical

reactions on the species mass fractions in the

combustion product mixture and returns the value of

the heat liberated by chemical reaction.

Calls:

None.

Called by:

INTAL, LUMPS.

CHEMRS

Purpose:

Subroutine CHEMRS performs a function similar to

that of CHEMR; however it addresses the reactions

within the solid propellant.

Calls:

None.

Called by:

IMBED.

Subroutine CMBUST interfaces the invariant embedding CMBUST Purpose: solution of the solid propellant thermal response with the macroscopic two-phase flow. Calls: FBAK, IMBED. INTEG, NOVSET. Called by: Subroutine CONLOS computes the rate of transfer of CONLOS Purpose: condensed species from the combustion product mixture to the surface of the solid propellant. Calls: None. HEATP. Called by: Purpose: Function COVC computes the covolume of the combustion COVC product mixture. Calls: None. BCAL, FRICT, HEATP, HEATW, INTAL, INTEG, INTRPC, Called by: LUMPS, REG12, REG32, STATES, TCLINK, TDBCAL, TDBUF. Function DPDER computes the partial derivative DPDER Purpose: $(\partial p/\partial e)_{0}$ for the covolume equation of state. Calls: None. LUMPS. Called by: Function DPDRE computes the partial derivative DPDRE Purpose: $(\partial p/\partial \rho)_{p}$ for the covolume equation of state. None. Calls: LUMPS. Called by: Function EPTOR evaluates the density as a function **EPTOR** Purpose: of internal energy and pressure for the covolume equation of state. Calls: CALEOS. BCAL, FRICT, HEATP, HEATW, INTRPC, NOVSET, TDBCAL, Called by: TLCBCL, TLCBCX, TLCINT, TLCLPV. Function ERTOP evaluates the pressure as a function **ERTOP** Purpose:

of internal energy and density for the covolume equation of state.

> CALEOS. Calls:

INTAL, LPVB, LUMPS, NOVSET, REG12, REG32, TLCLPV. Called by:

Subroutine EXCW computes the state of the solid-**EXCW** Purpose: phase after passing through a granular shock wave.

GRLOAD. Calls:

BCAL, BDMOV. Called by:

FRAK Purpose: Function FRAK computes the temperature gradient at

the surface of the solid propellant taking into account heat transfer from the igniter and heat

feedback from the flame.

Calls: None.

Called by: CMBUST, NOVSET.

FILLBR Purpose: Subroutine FILLBR updates the motion of the rear case

closure elements.

Calls: OUTPUT, TABLES.

Called by: BDMOV, NOVSET.

FILLER Purpose: Subroutine FILLER updates the motion of the forward

case closure elements and the projectile.

<u>Calls</u>: OUTPUT, TABLES. Called by: BDMOV, NOVSET.

FITSP Purpose: Subroutine FITSP sets values of the state variables,

following re-allocation of the mesh, by means of a

cubic spline interpolation scheme.

Calls: None.

Called by: BRNOUT, MESH, NOVSET.

FLUX <u>Purpose</u>: Subroutine FLUX computes the state of gas at the

boundaries of the reactive endwalls.

Calls: None.

Called by: FLUXDR, TDBCAL.

FLUXDR Purpose: Subroutine FLUXDR computes the derivatives of the

state variables in a lumped parameter region with

respect to the fluxes to that region from the

contiguous continuum regions.

<u>Calls</u>: FLUX. Called by: TDBUF.

FORM Purpose: Subroutine FORM computes the surface area and volume

of the propellant grains. It is supported by PERF19

which treats the slivering phase of nineteen

perforation propellant.

Calls: BLSL, HEX19, PERF19.

Called by: INTEG, NOVSET.

FORMCR Purpose: Subroutine FORMCR is effectively a subset of FORM

and is used to support subroutine LPVB as a modular

package.

Calls:

None.

Called by:

LPVB, TLCLPV.

FRACT

Purpose:

Subroutine FRACT determines the effects of grain

fracture.

Calls:

None.

Called by:

INTEG, NOVSET.

FRATE

Purpose:

Function FRATE computes the steady flow through a

nozzle using the covolume equation of state.

Calls:

None.

Called by:

BDMOV, LPVB.

FRICT

Purpose:

Subroutine FRICT computes the interphase drag for

granular propellant.

Calls:

CALEOS, COVC, EPTOR, VIS.

Called by:

INTEG.

GAMMOL

Purpose:

Subroutine GAMMOL computes the ratio of specific

heats and the molecular weight of the combustion

product mixture.

Calls:

None.

Called by:

BCAL, LUMPS, STATES, TCLINK, TDBCAL, TDBUF.

GETLS

Purpose:

Subroutine GETLS computes L values for the

intermediate combustion products of the traveling

charge.

Calls:

None.

Called by:

INTAL, INTEG.

GMOVE

Purpose:

Subroutine GMOVE updates the motion of the gun tube

when the recoil option is exercised.

Calls:

None.

Called by:

BDMOV.

GRLOAD

Purpose:

Subroutine GRLOAD computes the nominal loading curve

for granular propellant.

Calls:

None

Called by:

BCAL, EXCW, INTAL, RHEO.

HEATP Purpose: Subroutine HEATP determines the interphase heat

transfer, updates the surface temperature of the solid-phase prior to ignition, and also determines

the interphase drag in stick propellant.

Calls: CALEOS, CONLOS, COVC, EPTOR, VIS.

Called by: INTEG.

HEATW Purpose: Subroutine HEATW determines the rate of heat transfer

to the tube wall and updates the tube surface

temperature.

Calls: CALEOS, COVC, EPTOR, VIS.

Called by: INTEG, NOVSET.

HEX19 Purpose: Subroutine HEX19 computes the volume and surface

area of nineteen-perforation hexagonal grains.

Calls: SLIVER.

Called by: FORM.

IGNITE <u>Purpose</u>: Subroutine IGNITE determines the time of ignition

of the propellant.

Calls: None.

Called by: INTEG.

IMBED Purpose: Subroutine IMBED integrates the thermal profile in

the solid propellant by means of the method of

invariant embedding.

Calls: CHEMRS, FBAK, ROOT, ROOTR.

Called by: CMBUST, NOVSET.

INTAL Purpose: Subroutine INTAL updates the principal state

variables, p, ρ , u, ϵ , u_p, σ at all interior mesh points. It also determines trial update boundary values together with characteristic coefficients which are transmitted to BCAL for imposition of the

physical boundary conditions.

Calls: ATACH, BCAL, BDMOV, CALEOS, CHEMR, COVC, ERTOP,

GETLS, GRLOAD, INTRP1, LPVB, PRTOC, PRTOE, RCASE,

RDEDPR, RHEO, TCLINK, TCXC, TLCLNK, TLCXC.

Called by: INTEG.

Subroutine INTEG is the principal integration Purpose: INTEG executive. It is cycled twice per time step, once for the predictor level and once for the corrector level. It establishes the constitutive data by calls to individual subroutines and effects the update of the principal state variables by a call to INTAL. INTEG itself updates the surface regression and thermal parameter H for the solid-phase and, if KMODE = 0 (File [M2] of Table A.4), it also updates the molecular weight and ratio of specific heats for the gas phase. CMBUST, COVC, FORM, FRACT, FRICT, GETLS, HEATP, Calls: HEATW, IGNITE, INTAL, INTRP1, INTRP2, INTRPC, JCON, MESH, OUTPUT, PRTOC, REGRES, STATES, TABLES, TCBR4, TCLINK, TCOUT, TERMIN, TLCGDT, TLCLNK, TLCMSH, TLCOUT, VOIDS, WALTEM. NOVSET. Called by: Subroutine INTRP1 determines the cross-sectional INTRP1 Purpose: area of the tube at each mesh point, including an allowance for the unburned portion of the primer. Calls: JCON. INTAL, INTEG, MESH, NOVSET, TABLES. Called by: Subroutine INTRP2 computes the rate of discharge of INTRP2 Purpose: the igniter at each mesh point. PLASMA. Calls: INTEG, MESH, NOVSET. Called by: Subroutine INTRPC computes the local mass addition INTRPC Purpose: due to combustion of the reactive sidewalls. CALEOS, COVC, EPTOR, JCON, RCASE, VIS. Calls: Called by: INTEG, MESH, NOVSET. Function JCON locates the nearest continuum mesh JCON Purpose: point. None. Calls: INTEG, INTRP1, INTRPC, LUMPS. Called by: Subroutine LPDATA converts the XNOVA data base into LPDATA Purpose: an equivalent data base for a lumped parameter

interior ballistic model.

None.

NOVSET.

Calls: Called by: LPVB Purpose: Subroutine LPVB provides a lumped parameter analysis

of a control volume which undergoes mass transfer

with some external ambient.

Calls: ERTOP, FORMCR, FRATE.

Called by: INTAL, NOVSET.

LUMPS <u>Purpose</u>: Subroutine LUMPS provides a trial update of the

state of all lumped parameter regions. It also computes derivatives of the state variables with respect to the mass fluxes to the lumped parameter region. These are used by BCAL to enforce the

physical boundary conditions.

Calls: CALEOS, CHEMR, COVC, DPDER, DPDRE, ERTOP, GAMMOL,

JCON, RCASE.

Called by: BCAL, TDBUF.

MESH Purpose: Subroutine MESH determines the level of modeling of

each region and assigns mesh points to the continuum

regions on the basis of their relative sizes.

Calls: AFTSET, FITSP, INTRP1, INTRP2, INTRPC, OUTPUT, REG12,

REG21, REG21A, REG32, SETSUB, STATES.

Called by: INTEG, NOVSET.

NOVSET Purpose: Subroutine NOVSET performs the initialization of

variables which are not set by BLKDAT.

Calls: AFTSET, CALEOS, CMBUST, EPTOR, ERTOP, FBAK, FILLBR,

FILLER, FITSP, FORM, FRACT, HEATW, IMBED, INTEG, INTRP1, INTRP2, INTRPC, LPDATA, LPVB, MESH, REGRES, SETSUB, TABLES, TCDATA, TCINIT, TCLINK, TLCINP,

TLCINT, TLCLNK.

Called by: NOVSUB.

NOVSUB Purpose: Subroutine NOVSUB reads and prints the input data

used to define the problem.

Calls: AVN, CALEOS, NOVSET.

Called by: XKTC.

OUTPUT Purpose: Subroutine OUTPUT is responsible for logout of the

solution to the printer and/or direct access device

unit 8.

Calls: BDMOV, REGRES, TABLES, VIS.

Called by: AFTSET, BCAL, FILLBR, FILLER, INTEG, MESH.

PERF19 Purpose: Subroutine PERF19 computes the surface area and

covolume of nineteen-perforation propellant during

the slivering phase.

Calls:

None.

Called by:

FORM.

PGINT

Purpose:

Function PGINT performs truncation of a floating

point variable to a fixed point variable.

Calls:

None.

Called by:

TABLES.

PLASMA

Purpose:

Subroutine PLASMA computes the fluxes from a capillary

given the history of current. It is supported by block data "atomic" and two subroutines "mixture"

and "zjawja" which are not described here. See Powell

and Zielinsky (1992).

Calls:

mixture, zjawja

Called by:

INTRP2

PRTOC

Purpose:

Function PRTOC computes the square of the speed of

sound according to the covolume equation of state.

Calls: N

Called by:

BCAL, INTAL, INTEG, TDBUF.

PRTOE

Purpose:

Function PRTOE computes the internal energy from the

pressure and density according to the covolume

equation of state.

Calls:

None.

Called by:

BCAL, CALEOS, INTAL, STATES, TCLINK, TDBCAL, TDBUF,

TLCBCL, TCLMSH, TLCXC.

RCASE

Purpose:

Subroutine RCASE determines the density of the case

as a function of pressure.

Calls:

None.

Called by:

BDMOV, INTAL, INTRPC, LUMPS.

RDEDPR

Purpose:

Function RDEDPR computes the quantity $\rho(\partial e/\partial p)_{\rho}$

according to the covolume equation of state.

Calls:

None.

Called by:

INTAL, TLCFDR.

REG12

Purpose:

Subroutine REG12 transforms data for a region of

continuum ullage into data for a region of lumped

parameter ullage.

Calls:

COVC, ERTOP.

Called by:

MESH.

REG21 Purpose: Subroutine REG21 transforms data for a region of

lumped parameter ullage into data for a region of

continuum ullage.

Calls:

None.

Called by: BRNOUT, MESH.

REG21A Purpose:

Subroutine REG21A transforms data for a region of

lumped parameter two-phase flow into data for a

region of continuous two-phase flow.

Calls:

None.

Called by: MESH.

REG32 Purpose:

Subroutine REG32 sets initial data for a lumped

parameter region of ullage which is newly opened.

Calls:

COVC, ERTOP.

Called by: MESH.

REGRES Purpose:

Subroutine REGRES computes the rate of regression

of the surface of the propellant.

Calls:

VIS.

Called by: INTEG, NOVSET, OUTPUT.

RESFUN

Purpose:

Function RESFUN computes the resistance to projectile

motion due to interference of the rotating band with

the gun tube.

Calls:

None.

Called by: BDMOV.

RHEO

Purpose:

Subroutine RHEO computes the rate of propagation of

intergranular disturbances.

Calls:

GRLOAD.

Called by:

BCAL, BDMOV, INTAL.

ROOT

Purpose:

Subroutine ROOT selects a new value for the solution

of an arbitrary equation by the method of regula

falsi.

Calls:

None.

Called by:

IMBED.

ROOTR

Purpose:

Subroutine ROOTR is similar to ROOT, but contains

additional logic for the situation in which the

slope of the test function vanishes.

<u>Calls</u>:

None.

Called by:

IMBED.

Subroutine SETSUB sets the reactivity and perme-SETSUB Purpose: ability pointers. None. Calls: Called by: MESH, NOVSET. Subroutine SLIVER computes the volume and surface SLIVER Purpose: area of nineteen-perforation hexagonal grains during the slivering process. None. Calls: HEX19. Called by: Subroutine STATES computes certain of the dependent STATES Purpose: state variables from the principal storage arrays for the gas-phase. COVC, GAMMOL, PRTOE. Calls: INTEG, MESH, TERMIN. Called by: Subroutine TABLES compiles the summary data which TABLES Purpose: describe the conventional interior ballistic quantities such as histories of breech and base pressure and of the projectile trajectory. BDMOV, INTRP1, PGINT, TCLINK, TLCLNK. Calls: BCAL, FILLER, FILLER, INTEG, NOVSET, OUTPUT. Called by: Subroutine TCARAC defines characteristic data in TCARAC Purpose: conjunction with the determination of boundary values for the traveling charge when modeled as a continuum. TCBR2, TCDSDR. Calls: TCBASE, TCBPR, TCONTC. Called by: Subroutine TCBASE determines the regression rate of TCBASE Purpose: the traveling charge and provides trial boundary values for the unreacted side.

TCARAC, TCBURN, TCDSDR, TCIG, TCLINK, TCPROP, Calls: TCRESP, TCRNOM.

TCXC. Called by:

Subroutine TCBMDC computes mechanical properties of TCBMDC Purpose: the traveling charge when its rheology is specified

in tabular format.

ISCICU (An IMSL routine). Calls:

TCDATA, TCDSDR, TCRNOM, TCSNOM. Called by:

TCBPR Purpose: Subroutine TCBPR updates the boundary values of the

traveling charge at the base of the projectile.

Calls: TCARAC, TCDSDR, TCRNOM.

Called by: TCXC.

TCBR1 Purpose: Subroutine TCBR1 initializes the computational

arrays associated with the traveling charge.

Calls: TCRFIT, TCRNOM.

Called by: TCINIT.

TCBR2 Purpose: Subroutine TCBR2 moves the traveling charge

computational arrays into working arrays. This routine performs a trivial function in the present

code but it is retained in order to maintain structural commonality with BRLTC where its

function is non-trivial.

Calls: None.

Called by: TCARAC, TCBR3, TCBR4, TCOUT.

TCBR3 Purpose: Subroutine TCBR3 updates the state variables for

the traveling charge at all internal mesh points.

Calls: TCBR2, TCDSDR, TCWFR.

Called by: TCXC.

TCBR4 Purpose: Subroutine TCBR4 determines the CFL time step

restriction for the traveling charge.

Calls: TCBR2, TCDSDR, TCLINK.

Called by: INTEG.

TCBURN Purpose: Subroutine TCBURN calculates the regression rate of

the traveling charge when specified as an empirical function of pressure (on the reacted side) or stress

(on the unreacted side).

Calls: TCDVDI.

Called by: TCBASE.

TCDATA Purpose: Subroutine TCDATA reads and prints the input data

associated with the traveling charge.

Calls: TCBMDC, TCINIT.

Called by: NOVSET.

TCDSDR Purpose: Function TCDSDR calculates the speed of sound in

the traveling charge.

Calls: TCBMDC, TCSNOM.

Called by: TCARAC, TCBASE, TCBPR, TCBR3, TCBR4, TCONTC.

TCDVDI <u>Purpose</u>: Subroutine TCDVDI performs interpolation by the

method of divided differences.

Calls:

None.

Called by:

TCBURN.

TCGETK

Purpose:

Subroutine TCGETK updates the ordinary differential

equations associated with the traveling charge.

Calls:

TCRESP.

Called by:

TCXC.

TCIG

Purpose:

Subroutine TCIG determines the time at which

ignition occurs for the traveling charge.

Calls:

None.

Called by:

TCBASE.

TCINIT

Purpose:

Subroutine TCINIT performs the initialization of

constants and pointers for the traveling charge.

Calls:

TCBR1, TCRFIT, TCVUPD.

Called by:

NOVSET, TCDATA.

TCLINK

Purpose:

Subroutine TCLINK transfers data between the NOVA

routines and the BRLTC routines.

Calls:

COVC, GAMMOL, PRTOE, TCPROP.

Called by:

INTAL, INTEG, NOVSET, TABLES, TCBASE, TCBR4, TCOUT,

TCXC.

TCONTC

Purpose:

Subroutine TCONTC updates the boundary values for

the traveling charge at the interfaces between

increments.

<u>Calls</u>:

TCARAC, TCDSDR, TCRNOM.

Called by:

TCXC.

TCOUT

Purpose:

Subroutine TCOUT performs the logout of the

traveling charge state variables.

Calls:

TCBR2, TCLINK.

Called by:

INTEG.

TCPROP

Purpose:

Subroutine TCPROP moves the traveling charge

property data from vector into scalar storage.

Calls:

None.

Called by:

TCBASE, TCLINK.

TCRESP Purpose: Subroutine TCRESP computes the resistance on the

projectile when the traveling charge option is in

effect.

Calls:

None.

Called by: TCBASE, TCGETK.

TCRFIT Purpose: Subroutine TCRFIT performs the mesh allocation for

the traveling charge and the interpolation of data

associated with revisions to the number of points.

Calls:

None.

Called by: TCBR1, TCINIT, TCXC.

TCRNOM Purpose: Function TCRNOM computes the density of the

traveling charge as a function of pressure on

the nominal loading curve.

Calls: TCBMDC.

Called by: TCBASE, TCBPR, TCBR1, TCONTC.

TCSCHK Purpose: Subroutine TCSCHK enforces the requirement that the

pressure in the traveling charge not exceed the nominal loading value for the current value of

density.

Calls: TCSNOM.

Called by: TCXC.

TCSNOM Purpose: Function TCSNOM computes the pressure in the

traveling charge as a function of density on the

nominal loading curve.

Calls: TCBMDC.

Called by: TCDSDR, TCSCHK.

TCVCHK Purpose: Subroutine TCVCHK checks that the velocity in the

traveling charge has not been reversed as a

consequence of the friction term.

Calls: None.

Called by: TCXC.

TCVUPD Purpose: Subroutine TCVUPD updates the continuum boundary

velocities for the traveling charge.

Calls: None.

Called by: TCINIT, TCXC.

TCWFR Purpose: Subroutine TCWFR computes the friction between the

traveling charge and the tube wall.

Calls: None.

Called by: TCBR3.

TCXC

Purpose:

Subroutine TCXC is the integration executive for

the traveling charge state variables.

Calls:

TCBASE, TCBPR, TCBR3, TCGETK, TCLINK, TCONTC,

TCRFIT, TCSCHK, TCVCHK, TCVUPD, TCZUPD.

Called by:

INTAL.

TCZUPD

Purpose:

Subroutine TCZUPD updates the positions of the

continuum boundaries associated with the traveling

charge.

Calls:

None.

Called by:

TCXC.

TDBCAL

Purpose:

Subroutine TDBCAL uses the physical boundary

conditions and the characteristic forms to

determine the boundary values at each time step.

Calls:

COVC, EPTOR, FLUX, GAMMOL, PRTOE.

Called by:

TDBUF.

TDBUF

Purpose:

Subroutine TDBUF acts as an interface from the NOVA

storage conventions to those of the solver TDBCAL.

Calls:

CALFLO, CALPRM, COVC, FLUXDR, GAMMOL, LUMPS, PRTOC,

PRTOE, TDBCAL.

Called by:

BCAL.

TERMIN

Purpose:

Subroutine TERMIN tests for the termination of the

calculation.

Calls:

STATES.

Called by:

INTEG.

TLCBCL

Purpose:

Subroutine TLCBCL enforces the physical boundary

conditions associated with the traveling liquid

charge.

Calls:

EPTOR, PRTOE, TLCOUT, TLCPTR, TLCSMQ.

Called by:

TLCBCX.

TLCBCX

Purpose:

Subroutine TLCBCX organizes data for TLCBCL.

Calls:

EPTOR, TLCBCL, TLCFDR, TLCMIX, TLCPTR.

Called by:

TLCXC.

TLCFDR

Purpose:

Subroutine TLCFDR evaluates the effect of a mass

flux on a lumped parameter region for the traveling

liquid charge.

Calls:

RDEDPR, TLCMIX, TLCPTR.

Called by:

TLCBCX.

TLCGAC Purpose: Subroutine TLCGAC computes flow areas associated

with the traveling liquid charge.

Calls: None.

Called by: TLCINT, TLCMSH, TLCXC.

TLCGAS Purpose: Function TLCGAS computes the speed of sound in the

gas-phase for the traveling liquid charge.

Calls: None.

Called by: TLCMIX.

TLCGBL Purpose: Subroutine TLCGBL computes the total mass and

energy in the regions defined by the traveling

liquid charge.

Calls: TLCPTR.

Called by: TLCINT, TLCLNK.

TLCGDT Purpose: Subroutine TLCGDT computes the time step constraint

associated with the traveling liquid charge.

Calls: TLCMIX.

Called by: INTEG.

TLCINP Purpose: Subroutine TLCINP reads the input data for the

traveling liquid charge.

Calls: None.

Called by: NOVSET.

TLCINT Purpose: Subroutine TLCINT performs initialization

associated with the traveling liquid charge.

Calls: EPTOR, TLCGAC, TLCGBL, TLCLPV, TLCMSH, TLCPTR.

Called by: NOVSET.

TLCLIQ Purpose: Function TLCLIQ computes the speed of sound in the

liquid phase for the traveling liquid charge.

Calls: TLCPTR.

Called by: TLCMIX.

TLCLNK Purpose: Subroutine TLCLNK interfaces the traveling liquid

charge data storage with the conventional XKTC

storage arrays.

Calls: TLCGBL.

Called by: INTAL, INTEG, NOVSET, TABLES, TLCUPD.

TLCLPV Purpose: Subroutine TLCLPV models a two-phase lumped

parameter region for the traveling liquid charge.

Calls: EPTOR, ERTOP, FORMCR.

Called by: TLCINT, TLCXC.

TLCLUB Purpose: Subroutine TLCLUB is used to perform matrix

inversion for the traveling liquid charge.

Calls: None.

Called by: TLCSMQ.

TLCLUD Purpose: Subroutine TLCLUD is used to perform matrix

inversion for the traveling liquid charge.

Calls: None.

Called by: TLCSMQ.

TLCMIX Purpose: Function TLCMIX computes the speed of sound in the

two-phase mixture for the traveling liquid charge.

Calls: TLCGAS, TLCLIQ, TLCPTR.

Called by: TLCBCX, TLCFDR, TLCGDT, TLCUPD.

TLCMSH Purpose: Subroutine TLCMSH allocates mesh storage for the

traveling liquid charge.

Calls: PRTOE, TLCGAC.

Called by: INTEG, TLCINT.

TLCOUT Purpose: Subroutine TLCOUT prints the solution in regions

occupied by the traveling liquid charge.

Calls: TLCSTR.

Called by: | INTEG, TLCBCL.

TLCPTR Purpose: Function TLCPTR computes the density of the liquid

phase as a function of pressure in the traveling

liquid charge.

Calls: None.

Called by: TLCBCL, TLCBCX, TLCFDR, TLCGBL, TLCINT, TLCLIQ,

TLCMIX, TLCUPD.

TLCRSP Purpose: Function TLCRSP computes the resistive pressure

acting on the projectile when a traveling liquid

charge is modeled.

Calls: None.

Called by: TLCUPD.

TLCRTP Purpose: Function TLCRTP computes the pressure of the liquid

phase as a function of density in the traveling

charge.

Calls:

None.

Called by:

None.

TLCSMQ

Purpose:

Subroutine TLCSMQ determines the solution of a

system of linear equations.

<u>Calls</u>:

TLCLUB, TLCLUD.

Called by:

TLCBCL.

TLCSTR

Purpose:

Subroutine TLCSTR computes the stresses in the

afterbody of a projectile carrying a traveling

liquid charge.

Calls:

None.

Called by:

TLCOUT, TLCUPD.

TLCUPD

Purpose:

Subroutine TLCUPD performs the integration of the

governing equations associated with the traveling

liquid charge.

<u>Calls</u>:

TLCLNK, TLCMIX, TLCPTR, TLCRSP, TLCSTR.

Called by:

TLCXC.

TLCXC

Purpose:

Subroutine TLCXC is the executive routine for the

data associated with the traveling liquid charge.

Calls:

PRTOE, TLCBCX, TLCGAC, TLCLPV, TLCUPD.

Called by:

INTAL.

VIS

Purpose:

Function VIS computes the viscosity of the gas-phase

as a function of temperature.

Calls:

None.

Called by:

FRICT, HEATP, HEATW, INTRPC, OUTPUT, REGRES.

VOIDS

Purpose:

Subroutine VOIDS updates the volume fractions of

each of the constituent solid-phase species from

the history of the porosity.

Calls:

None.

Called by:

INTEG.

WALTEM

Purpose:

Subroutine WALTEM updates the thermal equation for

the tube wall temperature determined according to a

cubic profile approximation.

Calls:

None.

Called by:

INTEG.

TABLE A.2 SUMMARY OF XRTC "MANDATORY" INPUT FILES

| FILE NUMBER | FILE NAME |
|-------------|---|
| M1 | Problem Name |
| M2 | Control Data |
| мз | Integration Parameters |
| M4 | File Counters |
| M5 | Properties of Ambient Gas |
| M6 | General Properties of Propellant Bed |
| M7 | I-th Propellant Type, Location and Mass |
| M8 | I-th Propellant Form Function Data |
| M 9 | I-th Propellant Rheology |
| M10 | I-th Propellant Solid-Phase Thermochemistry |
| M 11 | I-th Propellant Gas-Phase Thermochemistry |
| M12 | Tube Geometry |
| *M13 | Projectile and Rifling Characteristics |

File M13 is not mandatory in XKTC. It is required only if neither the traveling charge option nor the liquid traveling charge option is exercised.

TABLE A.3 SUMMARY OF KRTC CONTINGENT INPUT FILES

| FILE NUMBER | FILE NAME |
|-------------|--|
| Cl | Logout Counters |
| C2 | Erosive Burn Rate Parameters |
| C3 | Not Supported. |
| C4 | Position and Mass of Additional Bags of I-th Propellant |
| C5 | Distribution of Volume Fraction of I-th Propellant |
| C5.05 | I-th Propellant Drag Relaxation Data |
| C5.1 | I-th Propellant Port Diameter File Counter |
| C5.2 | I-th Propellant Port Diameter |
| C5.3 | I-th Arbitrary Form Function File Counter |
| C5.4 | I-th Arbitrary Form Function Description |
| C5.5 | I-th Propellant Fracture Data Counter |
| C5.6 | I-th Propellant Fracture Characteristics |
| C6 | Not Supported. |
| C7 | I-th Propellant Deterred Layer Properties |
| C8 | Igniter Thermochemistry |
| C9 | Igniter Discharge Times |
| C10 | Igniter Discharge Positions |
| C11 ' | Igniter Rate of Discharge |
| C12 | Bore Resistance |
| C12.1 | Air Shock Data |
| C12.2 | Projectile Setback Resistance Data |
| C13 | Tube Thermal Properties |
| C14 | Tube Initial Temperature Profile |
| C15 | Not Supported. |
| C16 | Not Supported. |
| C17 | Not Supported. |
| C17.5 | Blowdown Parameters |
| C18 | I-th Forward Compactible Filler Element Properties |
| C19 | Constitutive Data for I-th Forward Element |

TABLE A.3 continued

| FILE NUMBER | FILE NAME |
|-------------|---|
| C19.1 | I-th Rear Compactible Filler Element Properties |
| C19.2 | Constitutive Data for I-th Rear Element |
| C20 | Not Supported. |
| C21 | Not Supported. |
| C22 | Not Supported. |
| C23 | Positions for Pressure Table Storage |
| C23.01 | Projectile Afterbody Pressure History Option |
| C23.1 | Kinetics Option Counters |
| C23.2 | Properties of Species |
| C23.21 | Properties of Species in NASA SP-273 Formulation |
| C23.3 | Composition of Propellant Near Field Combustion Products |
| C23.31 | Pressure Dependent Composition of Propellant Near Field Combustion Products |
| C23.4 | Composition of Igniter Discharge Combustion Products |
| C23.41 | Pressure Dependent Composition of Igniter Discharge Combustion Products |
| C23.5 | Composition of Initial Ambient Gas |
| C23.6 | Initial Composition of Solid Propellant |
| C23.61 | Composition of Traveling Charge Near Field Combustion Products |
| C23.62 | Types of Reactions in Mixture of Combustion Products |
| C23.63 | Species Thermal Equilibration Switches |
| C23.7 | Description of Arrhenius Reactions in Mixture of Combustion Products |
| C23.71 | Description of Pressure-Dependent Reactions in Mixture of Combustion Products |
| C23.8 | Description of Reactions in Solid Propellant |
| C23.9 | Solid Propellant Thermal Response Parameters |
| C24 | Parameters to Define Mesh in Invariant Embedding Analysis |
| C25 | Tank Gun Option Control Data |
| C25.1 | Geometry of Projectile Afterbody |
| C25.11 | Spatial Resolution Factor for Analysis of Base of Afterbody as Surface of Area Discontinuity |
| C25.2 | Thickness and Density Counters for Reactive Layer I |

TABLE A.3 continued

| FILE NUMBER | FILE NAME |
|-------------|--|
| C25.3 | Thickness of Reactive Layer I |
| C25.31 | Segment Pointers for Reactive Layer I |
| C25.4 | Density of Reactive Layer I |
| C25.5 | Counter to Describe Discharge of Reactive Layer I |
| C25.6 | Times to Describe Discharge of Reactive Layer I |
| C25.7 | Positions to Describe Discharge of Reactive Layer I |
| C25.8 | Rate of Discharge of Reactive Layer I |
| C25.9 | Burn Rate Counters for Reactive Layer I |
| C26 | Burn Rate Data for Reactive Layer I |
| C26.1 | Ignition Data for Reactive Layer I |
| C26.2 | Thermochemical Data for Reactive Layer I |
| C26.21 | Composition of Reactive Layer Near Field Combustion Products |
| C26.3 | Properties of Deterred Layer of Reactive Layer I |
| C26.31 | Surface Area Multiplier for Reactive Layer I |
| C26.4 | Endwall Property Pointers |
| C26.5 | Permeability Model Data |
| C26.6 | File Counters for I-th Reactivity Model |
| C26.7 | Thermochemical Data for I-th Reactivity Model |
| C26.71 | Composition of Near Field Combustion Products of I-th Reactivity Model |
| C26.8 | Ignition Value for I-th Reactivity Model |
| C26.9 | Burn Rate Data for I-th Reactivity Model |
| C27 | Tabular Description of I-th Reactivity Model |
| C28 | Internal Properties of Control Charge Combustion Chamber |
| C28.1 | External Properties of Control Charge Combustion Chamber |
| C28.2 | Control Charge Type |
| C28.3 | Control Charge Form Function |

TABLE A.3 continued

| FILE NUMBER | FILE NAME |
|-------------|--|
| C28.4 | Control Charge Burn Rate Counter |
| C28.5 | Control Charge Burn Rate Description |
| C28.6 | Control Charge Thermochemistry |
| C28.7 | Properties of Deterred Layer |
| C29 | Forward Boundary Discharge Data |
| C30 | Inbore Rocket Motor Data |
| C30.1 | Composition of Rocket Motor Combustion Products |
| C31 | ETG Control Switches |
| C31.1 | I-th Propellant Helmholtz Wiping Coefficient |
| C31.2 | I-th Propellant Tabular Regression Rate Counter |
| C31.3 | I-th Propellant Tabular Regression Rate Data |
| C31.4 | I-th Plasma Jet File Counters |
| C31.5 | Global Properties of I-th Plasma Jet |
| C31.6 | Composition of I-th Plasma Jet |
| C31.7 | I-th Plasma Jet Mixing Length Parameters in Integrated Format |
| C31.71 | Plasma Capillary Data |
| C31.72 | Stoichiometry Coefficients for Plasma Model |
| C31.73 | Current History |
| C31.8 | I-th Plasma Jet Integrated Data |
| C31.9 | I-th Plasma Jet Mixing Length Parameters in Detailed Format |
| C32 | I-th Plasma Jet Detailed Data |

TABLE A. 4 SUMMARY OF XKTC TRAVELING CHARGE INPUT FILES

| | k. |
|-------------|--|
| FILE NUMBER | FILE NAME |
| TC1 | Traveling Charge Control Data |
| TC2 | Mesh Parameters |
| TC3 | General Properties |
| TC4 | Propellant Thermochemical Properties |
| TC5 | Burn Rate Switches |
| TC6 | Tabular Burn Rate Data |
| TC7 | Tabular Burn Rate Data (con't) |
| TC7.1 | Plasma Guided End Burner |
| TC7.2 | Plasma Guided End Burner (Cont'd) |
| TC8 | Exponential Burn Rate Data |
| TC9 | Propellant Analytical Rheology Data |
| TC10 | Propellant Tabular Rheology Data |
| TC11 | Propellant Tabular Rheology Data (con't) |
| TC12 | Ablative Film Data |
| TC13 | Propellant Friction Data |
| TC14 | Tabular Bore Resistance Data |
| TC15 | Barrel Shock Resistance Data |
| TC16 | Obturator Setback Resistance Data |
| TC17 | Obturator Friction Data |

TABLE A.5 SUMMARY OF KRTC TRAVELING LIQUID CHARGE INPUT FILES

| FILE NUMBER | FILE NAME |
|-------------|--|
| TLC2 | Option Switches |
| TLC5 | Integration Parameters |
| TLC6 | Tube Properties |
| TLC6.1 | Obturator Resistance |
| TLC6.2 | Air Shock Resistance Data |
| TLC7 | Projectile Properties |
| TLC7.1 | Chamber Length |
| TLC9 | Properties of Liquid Propellant |
| TLC9.1 | Propellant Droplet Formation Data |
| TLC9.2 | Droplet Burn Rate Data |
| TLC10 | Initial Conditions |
| TLC11 | Initial Cavity Parameters |
| TLC11.1 | Initial Cavity Geometry |
| TLC22.1 | Properties of TLC Expulsion Charge Combustion Chamber |
| TLC22.2 | TLC Expulsion Charge Type |
| TLC22.3 | TLC Expulsion Charge Form Function |
| TLC22.4 | TLC Expulsion Charge Burn Rate Counter |
| TLC22.5 | TLC Expulsion Charge Burn Rate Description |
| TLC22.6 | TLC Expulsion Charge Thermochemistry |
| TLC22.7 | Properties of Deterred Layer |

TABLE A.6 DESCRIPTION OF INPUT FILES

| File [M1] | "Problem Name" (15A4) One Card |
|-----------|---|
| TITLE | Problem name. May be up to 60 alphanumeric characters. |
| File [M2] | "Control Data" (7L1,33I1) One Card |
| NPRINT | T if print on logout, F otherwise. |
| NGRAPH | Inactive. |
| NDISK | T if disc write on logout, F otherwise. |
| DSKRD | T if disc start, F otherwise. |
| IBTABL | T if summarized interior ballistic data are required, F otherwise. |
| nflam | T if summary of ignition delay data required, F otherwise. |
| NPTABL | T if summarized pressure, pressure difference data are required, F otherwise. |
| NEROS | <pre>1 if erosive effect to be included in propellant combustion, 0 otherwise. If NEROS = 1, File [C2] is required.</pre> |
| NDYN | Inactive. |
| NHTW | <pre>0 if wall temperature is not updated. 1 if cubic profile update is used.</pre> |
| NBC(1) | Inactive. |
| NBC(2) | Inactive. |
| NRES (1) | Inactive. |
| NRES (2) | Inactive. |
| LDBED | <pre>0 if propellant beds initially uncompacted, 1 otherwise. See comment in File [M9].</pre> |

JHTW

0 if heat loss to tube is neglected.

1 if heat loss is calculated by empirical correlation for fully developed turbulent flow. File [C13] is required.

LYER

Inactive.

IBRES

- 1 if linear interpolation of tabular data from File [C12] is used to define bore resistance. No velocity dependence is considered.
- 2 if the interpolated value is multiplied by $7.2V^{-0.6}$, where V is the projectile velocity (ft/sec), provided V \geq 27 fps.

3 if the interpolated value is multiplied by

- (1 + 0.0004414V)/(1 + 0.005046V) where V is the projectile velocity (in/sec).
- 4 if the resistance is that for 1 plus resistance due to the air shock in front of the projectile. File [C12.1] is required.
- 5 if the resistance is that for 1 plus resistance due to Poisson deformation of the projectile. File [C12.2] is required.
- 6 if the resistance is that for 1 plus resistance due to the air shock plus resistance due to Poisson deformation. Files [C12.1] and [C12.2] are required.

If any other value is used, IBRES will default to the value 2.

NTC -

- 0 if traveling charge option not required.
 1 if traveling charge option is in effect.
 When NTC = 1, NUNIN and NUNOUT (File [M3]) must not be entered as nine (default values are eight); NEL (File [M4]) must be entered as zero; NDIM (File [M3]) must not exceed KQ 2 for a granular booster or KQ/2 1 for a stick booster. KQ is presently 999. Files [TC1] through [TC17] are required.
- 2 if end burning plasma guided charge is located in breech of chamber. Files [TC1] through [TC17] are required. In File [TC3] XIB must be entered as zero.

INHIB(1)

0 if propellant type 1 does not have a deterred layer. 1 if propellant type 1 does have a deterred layer. File [C7] is required in this case.

INHIB(2)

As per INHIB(1), but for second propellant type.

INHIB(3)

As per INHIB(1), but for third propellant type.

NXCW

0 if explicit analysis of impact-induced compaction wave not required. 1 if explicit analysis is required. In this case, the value

of XIMPV (File [M6]) must be set.

NBLDWN

0 if tube blowdown analysis is not required. 1 if blowdown analysis is required. File [C17.5] is

required in this case.

2 if end burning plasma guided charge is located in breech of chamber. Files [TC1] through [TC17] are required. In File [TC3] XIB must be entered as zero.

NSWSOL

0 if non-conservative form of solid-phase continuity

equation is to be used.

1 if conservative form is to be used. It is recommended that this option be selected only if excessive mass defects result from the use of the non-conservative form.

KMODE

0 if kinetics option not desired.

1 if gas-phase is to be treated as a reacting, homogeneous

mixture. See Files [C23.1] through [C23.9].

2 if, in addition to treatment of gas-phase as a mixture, subsurface reactivity and/or finite difference solution of

solid-phase thermal response is desired.

See Files [C23.1] through [C23.9].

MODET

0 if tank gun option not desired.

1 if tank gun is desired. See Files [C25.1] through [C27].

NECHO

0 if interpretation of input and normal run desired. 1 if input data not interpreted but normal run desired. 2 if interpretation of input data with no subsequent run desired.

Note: Independently of the value of NECHO, the Code prints an image of the card input file.

INBCX

0 if forward boundary is impermeable.

1 if forward boundary is permeable to mixture of combustion

products. File [C29] is required.

2 if forward boundary is an inbore rocket motor.

Files [C30] and [C30.1] are required.

NTLC

0 if traveling liquid charge option not required. 1 if traveling liquid charge option is required. Files [TLC2] - [TLC22.7] are required.

NFRACT

0 if analysis of propellant fracture is not required. 1 if analysis of propellant fracture is required. Files [C5.5] and [C5.6] are required.

INTRIN

O if values of intergranular stress in File [C5.6] are non-intrinsic (dilute) averages.

1 if values are intrinsic averages.

NETG

0 if electrothermal gun option is not required.
1 if electrothermal gun option is required.
Files [C31] - [C32] are required.

NFILT

0 if no solid-phase smoothing is required.

1 if porosity is smoothed

2 if solid-phase velocity is smoothed.

3 if both porosity and solid-phase velocity are smoothed.

| File [M3] | "Integration Parameters" (615,F10.0/8F10.0) Two Cards |
|-----------|---|
| NDIM | Number of grid points to be used in calculation. In general, NDIM must not exceed the value of KQ, currently set by a PARAMETER statement equal to 999. If perforated stick propellant is present, NDIM must not exceed KQ/2 or 499 in the current version. |
| NSTEP | Number of integration steps before logout. (Each step consists of a predictor followed by a corrector.) If NSTEP = 0, logout follows every predictor as well as every corrector. If NSTEP < 0, File [C1] is required with NSTEP pairs of data. NSTEP > -10. |
| ndtst | Step number for disc start. |
| NSTOP* | Number of steps for termination. |
| NUNIN | Unit number for disc read. If NUNIN = 0, it is defaulted to 8. |
| NUNOUT | Unit number for disc logout. If NUNOUT = 0, it is defaulted to 8. |
| DTPRT | Time interval before logout (sec). If entered as zero, it is defaulted to $10^{10}\mathrm{c}$ |
| TSTOP* | Time for termination (sec). |
| ZSTOP* | Projectile travel for termination (in). |
| TINT | Maximum time step (sec). |
| SAFE | Stability safety factor. Recommended value is 1.1 although larger values may sometimes be required. |
| CRIT | Stability safety factor for source terms. Recommended value is 0.05. |
| RZOLV | Spatial resolution factor. Recommended range of values is $0.01 \le RZOLV \le 0.05$. If RZOLV is entered as zero, it will default internally to $1/(NDIM - 1)$. |
| TABLIB* | Time interval for storage of summarized interior ballistic data (sec). |
| TABLP** | Time interval for pressure table storage (sec). |

Termination occurs at whichever of NSTOP, TSTOP or ZSTOP is first satisfied, except when NBLDWN = 1. (See File [M2]). In the latter case the projectile motion is terminated at ZSTOP and the solution is continued until whichever of NSTOP, TSTOP or PBRF (see File [C17.5]) is first satisfied.

Table sizes are dimensioned to 500. When overflow is imminent, tables are condensed by deleting every second datum. Subsequently, storage time is doubled.

| File [Cl] "Log | out Counters" (1615) One or Two Cards |
|-----------------|---|
| N.B. File requ | ired if and only if NSTEP < 0. (See File [M3].) |
| NDTEP(1) | Maximum value of integration step number for which MSTEP(1) is to be used. |
| MSTEP(1) | Number of integration steps (predictor plus corrector count as one unit) between logout cycles. |
| NDTEP(NSTEP)* | Maximum value of integration step number for which MSTEP(NSTEP) is to be used. |
| mstep (nstep) | Corresponding value of number of steps between logout cycles. |

If NDTEP(|NSTEP|) is exceeded during the calculation, the value MSTEP(|NSTEP|) will be used as a default quantity.

| File [M4] "File Counters" (1615) Two Cards | | |
|--|--|--|
| NSTA | Number of entries in tube geometry table. $2 \le NSTA \le 10$. | |
| JJ | Number of times at which primer discharge is specified. $0 \le JJ \le 40$. If II and $JJ \ge 2$, Files [C8] - [C11] are required. | |
| II | Number of positions at which primer discharge is specified. 0 \leq II \leq 40. | |
| NBRES | Number of entries in bore resistance table. $0 \le NBRES \le 20$. If NBRES ≥ 2 , File [C12] is required. | |
| NTEM | Number of entries in tube initial temperature profile. If NTEM = 0, tube temperature defaults to TEMST (see File [M5].) If NTEM \neq 0, File [C14] is required. 0 \leq NTEM \leq 10. | |
| NEL | Number of elements to characterize compactible filler between bed and projectile. If NEL = 0, projectile base is taken as right-hand boundary for computational domain. If NEL \neq 0, File [C18] is required. $0 \le \text{NEL} \le 10$. | |
| NPROP | Number of types of propellant grains. $1 \le NPROP \le 3$. | |
| NBRDS | Number of burn rate data sets to describe pressure dependence of exponent and pre-exponential factors. (See File [M10].) Note that the same value is assumed for all propellant species, if more than one are defined. | |

| NEPS(1) | Number of entries in initial distribution of volume fraction of propellant type 1. If NEPS = 0, porosity is calculated from mass and position data given in File [M7]. If NEPS \neq 0, File [C5] is required. Propellant types may be entered in either mode, independently of the representation of other types. $0 \leq \text{NEPS}(1) \leq 10$. | |
|----------|---|--|
| NEPS(2) | Number of entries for type 2. | |
| NEPS (3) | Number of entries for type 3. | |
| NZPT | Number of entries in table of positions for summarized pressure data. If NZPT \neq 0, File [C23] is required. 0 \leq NZPT \leq 8. | |
| NMS (1) | Inactive. | |
| NMS (2) | Inactive. | |
| NWIB | Inactive. | |
| MORE (1) | Number of additional bags of propellant of type 1. If MORE(1) > 0, File [C4] is required. $0 \le MORE(1) \le 9$. | |
| MORE (2) | Number of additional bags of propellant of type 2. Only required if NPROP \geq 2. Starts a new card. | |
| MORE (3) | Number of additional bags of propellant of type 3. Only required if NPROP = 3. | |
| NBL | Number of elements to characterize compactible filler between bed and breech. If NBL • 0, File [C19.1] is required. 0 < NBL < 10. | |

| File [M5] | "Properties of Ambient Gas" (8F10.0) One Card |
|-----------|--|
| | Tropological of Transcent Case (Circle) one Case |
| TEMST | Initial temperature (R). |
| PST | Initial pressure (psi). |
| GMST | Molecular weight (lbm/lbmol). |
| GAMST | Ratio of specific heats (-). |
| | |
| File [M6] | "General Properties of Propellant Bed" (8F10.0) One Card |
| TPO | Initial temperature (R). |
| BETA | Inactive. |
| BETAB | Inactive. |
| | |

CE(2) Inactive.

CE(3) Inactive.

XIMPV Minimum impact velocity for initiation of explicit analysis of intergranular compaction wave (in/sec). Note that if XIMPV is entered as zero it will default to 108, effectively precluding the explicit analysis.

File [C2] "Erosive Burn Rate Parameters" (8F10.0) One Card

N.B. File required if and only if NEROS = 1. (See File [M2].)

CEROS Erosive burning pre-exponential factor (in² R/lbf).

BEROS Erosive burning exponential factor (-).

Note: The subsequent Files [M7], [C4], [C5], [M8], [M9], [M10], [C6], [M11] and [C7] are repeated, as a group for each of the NPROP (see File [M4]) types of propellant which constitute the solid-phase.

| File [M7] | 'I-th Propellant Type, Location and Mass" (5A4,6F10.0) One Card |
|------------|--|
| GRNAM(I) | Name of propellant. Up to 20 alphanumeric characters. |
| ZGR (1, I) | Left-hand boundary of first bag of propellant of type I (in). |
| ZGR(2,I) | Right-hand boundary of first bag of propellant of type I (in). |
| WTGRA(1,I) | Mass of first bag of propellant of type I (lbm). A negative value of WTGRA may be entered. In such a case, the absolute value is used to define the mass. The negative sign is used to set an internal switch which causes the computation of initial porosity for a granular charge to reflect the assumption that the propellant is packaged as a cylinder rather than filling uniformly each cross-section of the tube. Conversely, a stick charge will be given a uniform initial distribution of porosity rather than one which varies with cross-sectional area. |
| RHOP(I) | Density of propellant type I (lbm/in3). |
| RGRI(1,I) | Inner radius of rear of bag (in). Only required if MODET = 1. (See File [M4].) If RGRI(1,I) is input as zero it is assumed to coincide with the inner radius of the available flow cross-section. |
| RGRO(1,I) | Outer radius of rear of bag (in). Only required if MODET = 1. (See File [M4].) If RGRO(1,I) is input as zero it is assumed to coincide with the outer radius of the available flow cross-section. |

```
"Position and Mass of Additional Bags of I-th Propellant"
File [C4]
             (8F10.0)
                      More(I) Cards
      File required if and only if MORE(I) # 0. (See File [M4].)
ZGR (3, I)
                 Left-hand boundary of second bag of propellant of type I
                 (in) .:
ZGR (4, I)
                 Right-hand boundary of second bag of propellant of type I
                 (in).
WTGRA(2, I)
                 Mass of second bag of type I (1bm).
RGRI (2, I)
                 Inner radius of second bag (in).
RGRO(2,I)
                 Outer radius of second bag (in).
ZGR (5, I) *
                 Left-hand boundary of third bag.
ZGR(2*MORE(I)+2,I)
                       Right-hand boundary of bag MORE(I)+1 (last bag).
WTGRA (MORE (I)+1)
                       Mass of last bag.
RGRI (MORE (I)+1)
                       Inner radius of last bag (in).
RGRO (MORE (I)+1)
                       Outer radius of last bag (in).
```

File [C5] "Distribution of Volume Fraction of I-th Propellant" (8F10.0) One to Three Cards

N.B. File required if and only if NEPS(I) = 0. (See File [M4].)

- ZEPS(1,I) First position relative to breech (in).
- EPSO(1,I) Corresponding volume fraction of propellant type I.

ZEPS(NEPS(I),I) Last position.

EPSO(NEPS(I), I) Corresponding volume fraction.

Begin new card for each bag.

| File [M8] | "I-th Propellant Form Function Data" (I5,5F10.0,I5,F10.0,I5) One Card |
|-----------|--|
| NFORM(I) | Form function indicator. $1 \le NFORM(I) \le 17$. NFORM may be entered as a negative number. In such a case, the absolute value is used to determine the form function, but the grains are taken to be stacked. This option allows granular propellant to respond as though it had the flow resistance of stick propellant. |
| OD(I) | Grain dimension (in). (See table below.) If OD < 0 for NFORM = 7 or 9, the grains will be treated as inhibited on the outer cylindrical surfaces up to the point of slivering. |
| DPERF(I) | Grain dimension (in). (See table below.) |
| GLEN(I) | Grain length (in). If NFORM = 14, setting GLEN = 0 will cause this granulation to be modeled as a stick. |
| NPERF(I) | Number of perforations (-) except for NFORM = 14 in which case NPERF is the number of slots. |
| SLW(I) | Grain dimension (in). (See table below.) |
| NFIX(I) | If 0, grains are assumed to be free to move. If 1, grains are assumed to be attached to the tube. If 2, grains are assumed to be attached to the projectile. |
| BONDX(I) | Strength of bond to tube or projectile (lbf). If BONDX(I) is entered as zero, it is taken to be infinite. Separation from tube or projectile occurs when absolute value of force required to maintain attachment exceeds BONDX(I). |
| NDUM | If NDUM = 1, File [C5.05] is required to define non-default values of drag relaxation parameters for stacked granular bed. |

FORM FUNCTION PARAMETERS

| NFORM | GRAIN TYPE | <u>od</u> | DPERF | slw |
|-------|--|-------------------------------|------------------------------|--------------------------------------|
| 1 | Sphere | Diameter (in) | _ | _ |
| 2 | Cylinder | Diameter (in) | _ | _ |
| 3 | Stick* | Diameter (in) | Perforation Diameter (in) | _ |
| 4 | Strip* | Width (in) | Thickness (in) | - |
| 5 | Monoperforated | Diameter (in) | Perforation Diameter (in) | - |
| 6 | Monoperforated with outside inhibition | Diameter (in) | Perforation Diameter (in) | - |
| 7 | Seven Perforations | Diameter (in) | Perforation Diameter (in) | |
| 9 | Nineteen Perforations | Diameter (in) | Perforation Diameter (in) | - |
| 10 | Hexagonal Seven- Perforation Stick* | Distance between flats (in) | Perforation Diameter (in) | - |
| 11 | Slotted stick* (single-voidage) | Diameter (in) | Perforation Diameter (in) | Slot Width (in) |
| 12 | Scroll* (single-voidage) | Width (in) | Thickness (in) | - |
| 13 | Scroll* (dual-voidage) | Width (in) | Thickness (in) | External Diameter o Scroll (in |
| 14 | Blind slit | Diameter (in) | Diameter of slotted core (in | _) |
| 15 | Hexagonal Nineteen- Perforation | Diameter (in) ** | Perforation Diameter (in) | - |
| 16 | Monolithic Grain with central port*** | Port diameter at rear (in) | Port diameter at front (in) | - |
| 17 | Arbitrary Tabular**** | - | | - |

End burning is neglected for these forms. Hence GLEN (File [M8]) may be entered arbitrarily.

Grains assumed to have rounded corners. Diameter is between opposite corners.

Burning is assumed to take place only on the surfaces of the internal port. Projectile afterbody may intrude into port. NFIX(I) and BONDX(I) default to 1 and 0 respectively. If OD(I) = 0, or DPERF(I) = 0, then Files [C5.1], [C5.2] are required to define the diameter of the port as a function of position.

^{****} Files [C5.3], [C5.4] required if NFORM = 17.

| | "I-th Propellant Drag Relaxation Data" (8F10.0) One Card |
|--|---|
| N.B. This file | e is required if and only if NDUM = 1 (See File [M8]). |
| RLXF(I) | Exponent used to control rate of relaxation of drag of stacked granular propellant from that for stick to that for granular propellant. Default value is 1.0. |
| RVOLF(I) | Fraction of granular flow resistance experienced by stacked granular bed in settled or loaded condition (-). Default i zero. |
| TUMBLE (I) | Time delay for inset of tumbling of stacked granular bed (msec). Default is zero. |
| TSPLIT(I) | Time delay for breakup of stacked granular propellant (msec). |
| TUMINT(I) | Time interval to complete tumbling (msec). |
| SPLINT(I) | Time interval to complete breakup. (msec). |
| | |
| File [C5.1] ": | I-th Propellant Port Diameter File Counter" (I5) One Card |
| | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) |
| MNOP(I) | Number of entries in file to define diameter of port of monolithic grain. $2 \le MNOP(I) \le 8$. |
| | |
| | |
| File [C5.2] " | I-th Propellant Port Diameter" (8F10.0) One to Two Cards |
| N.B. File requ | I-th Propellant Port Diameter" (8F10.0) One to Two Cards uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) |
| N.B. File requirements of the present of the presen | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or |
| N.B. File requ DPERF(I) | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) |
| N.B. File requ DPERF(I) | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) First axial position relative to rear surface of grain (in) |
| N.B. File requirements of the property of the | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) First axial position relative to rear surface of grain (in) Corresponding diameter of port (in). |
| N.B. File requirements of the property of the | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) First axial position relative to rear surface of grain (in) Corresponding diameter of port (in). |
| N.B. File requirements of the property of the | uired if and only if NFORM(I) = 16 and either OD(I) = 0 or = 0. (See File [M8].) First axial position relative to rear surface of grain (in) Corresponding diameter of port (in). |

NARBF(I)

Number of sets of data in tabular description given in File [C5.4]. $2 \le NARBF(I) \le 20$.

| File [C5.4] | "I-th Arbitrary Form Function Description" (3F10.0) NARBF(I) Cards |
|-------------|--|
| ARBR(1,I) | First value of surface regression (in). |
| ARBS(1,I) | First value of surface area of grain (in2). |
| AREV(1,I) | First value of volume of grain (in3). |
| ARBR (2, I) | Second value of regression. Starts a new card. |
| ARBS(2,I) | Second value of area. |
| ARBV(2,I) | Second value of volume. If ARBV(2,1) $< 10^{-10}$, the volume will be calculated automatically from the values of area versus regression. |

ARBV(NARBV(I),I) Last value of volume.

| File [M9] | "I-th Propellant Rheology" (6F10.0) One Card |
|-----------|---|
| GAP(I) | Rate of propagation of intergranular stress in settled, loading granular bed of type I (in/sec). If propellant I consists of stick then GAP(I) is independent of the settling porosity. |
| GEPO(I) | Porosity of settled bed for type I propellant. If LDBED = 0 (see File [M2]) and the porosity of the bed is less than GEPO(I) at any point where type I is present, GEPO(I) is automatically defaulted to the smallest value of porosity which occurs in the initial distribution. This property may be used to avoid calculating GEPO(I). |
| GCAP(I) | Rate of propagation of intergranular stress during unloading and reloading of propellant type I (in/sec). Not required for stick propellant. If GCAP(I) $< 10^{-10}$, a reversible law will be used for granular propellant. |
| PRPYLD | Inactive. |
| ANU(I) | Poisson ratio of propellant (-). Must be specified for stick propellant. ANU(I) defaults to 0.5 internally if propellant I is granular or if ANU(I) is entered as zero. |

| File [C5.5] | "I-th Propellant | Fracture I | Data Counter" | (I5) | One Card |
|-------------|------------------|------------|---------------|------|----------|
| | | | | | |

- N.B. This file is required if and only if NFRACT = 1. (See File [M2].)
- NSTRV(I) Number of sets of data in fracture characterization of File [C5.6]. $2 \le NSTRV(I) \le 20$.

File [C5.6] "I-th Propellant Fracture Characteristics" (3F10.0) NSTRV(I) Cards

- N.B. This file is required if and only if NFRACT = 1. (See File [M2].)
- STRV(1,I) First value of maximum intergranular stress experienced by propellant (psi). If INTRIN = 0 (File [M2]), the stress is non-intrinsic and if INTRIN = 1, the stress is understood to be an intrinsic average.
- BRF(1,I) Multiplier to be applied to mass burning rate based on nominal form function when maximum stress equals STRV(1,I) (-).
- RAXF(1,I) Multiplier to be applied to interphase drag and heat transfer based on nominal form function when maximum stress equals STRV(1,I) (-). If RAXF = 0, it will default to BRF.
- STRV(2,I) Second value of maximum intergranular stress. Starts a new card.
- RAXF(NTSRV(I),I) Last value of multiplier for interphase drag and heat transfer.
- N.B. This table is linearly interpolated.

| File [M10] "I-th Propellant Solid-Phase Thermochemistry" (8F10.0) One to Three Cards | | | | | | |
|--|--|--|--|--|--|--|
| UPPR(1,I) | Maximum value of pressure for corresponding values of burn rate pre-exponential and exponential factors (psi). | | | | | |
| B22(1,I) | Burning rate pre-exponential factor (in/sec-psi*). | | | | | |
| BNN (1, I) | Burning rate exponent (-). | | | | | |
| UPPR(NBRDS,I)* | Maximum value for last set of burn rate data. | | | | | |
| B22 (NBRDS, I) | Corresponding pre-exponential factor. | | | | | |
| BNN (NBRDS, I) | Corresponding exponent. | | | | | |
| B1(I) | Burning rate additive constant (in/sec). | | | | | |
| TEMPIG(I) | Ignition temperature (R). | | | | | |
| KP(I) | Thermal conductivity (lbf/sec/R). | | | | | |
| ALPHAP(I) | Thermal diffusivity (in2/sec). | | | | | |
| ALPHA(I) | Emissivity factor (-). | | | | | |

If pressure exceeds UPPR(NBRDS,I), the corresponding values of preexponential and exponential factors are used as default values.

| File [M11] | "I-th Propellant Gas-Phase Thermochemistry" (4F10.0) One Card |
|------------|---|
| ECHEM(I) | Internal energy released in combustion (lbf-in/lbm). |
| GMW (I) | Molecular weight (lbm/lbmol). |
| GAMMA(I) | Ratio of specific heat (-). |
| BV(I) | Covolume (in ³ /lbm). |

| File [C7] | "I-th Propellant Deterred Layer Properties" (5F10.0) One Card |
|-----------|---|
| N.B. File | required if and only if INHIB(I) # 0. (See File [M2].) |
| ECHIB(I)* | Internal energy released in combustion at start of deterred layer (lbf-in/lbm). |
| ECHIB2(I) | Internal energy released in combustion at end of deterred layer (lbf-in/lbm). |
| RGFAC(I)* | Factor by which burn rate is multiplied at start of deterred layer (-). |
| RGFAC2(I) | Factor by which burn rate is multiplied at end of deterred layer (-). |
| HIBX(I) | Depth of inhibited layer (-). |

Values within deterred layer deduced by linear spacewise interpolation. Final values need not be the same as those of the undeterred propellant.

| File | [C8] | "Igniter | Thermochemistry" | (8F10.0) | One Card |
|-------|------|----------|--------------------|------------|-----------------------|
| N.B. | File | required | if and only if II | , JJ ≥ 2. | (See File [M4].) |
| EIG | | Int | ernal energy relea | sed in com | bustion (lbf-in/lbm). |
| GMIG | | Mol | ecular weight (1bm | /lbmol). | |
| GAMIG | ; | Rat: | io of specific hea | ts (-). | |
| VIG | | Spe | cific volume of ig | niter soli | .d-phase (in³/lbm). |
| | | | | | |

| File | [C9] | "Igniter | Dischar | ge Tim | es" | (8F1 | 0.0) | One to Five Cards |
|------|------|--------------|---------|--------|-------|------|-------|-----------------------------|
| N.B. | File | required | if and | only i | f II, | JJ | ≥ 2. | (See File [M4].) |
| TPHI | (1) | Firs (sec | | in tab | ular | repr | esent | tation of igniter discharge |
| • | | | | | | | | |
| | | | | | | | | |

TPHI (JJ)

Last time.

| File [C10] | "Igniter Discharge Positions" (8F10.0) One to Five Cards |
|------------|--|
| N.B. File | required if and only if II, $JJ \ge 2$. (See File [M4].) |
| ZPHI(1) | First position in tabular representation of igniter discharge (in). |
| • | |
| ZPHI(II) | Last position. |
| File [Cl1] | "Igniter Rate of Discharge" (8F10.0) Two to Two Hundred Cards |
| N.B. File | required if and only if II, JJ ≥ 2. (See File [M4].) |
| PHI (1,1) | Igniter discharge per unit length per unit time at first position and first time (lbm/in/sec). |
| PHI (2,1) | Discharge at second position and first time. |
| • | |
| PHI(II,1) | Discharge at last position and first time. |
| PHI(1,2)* | Discharge at first position and second time. |
| • | |
| PHI(II,JJ) | Discharge at last position and last time. |
| * PHI(1,J) | begins a new card, $J = 1, \ldots, JJ$. |
| File [M12] | "Tube Geometry" (8F10.0) One to Three Cards |
| ZA(1) | First axial location relative to breech (in). |
| RA(1) | Corresponding radius of bore (in). |
| • | |
| Za (nsta) | Last axial location |
| ra (nsta) | Corresponding radius |

File [C12] "Bore Resistance" (8F10.0) One to Five Cards File required if and only if NBRES ≥ 2. (See File [M4].) First axial location. If BRZ(1) > 0, it is understood to be BRZ(1) relative to breech (in). If BRZ(1) is entered as zero, however, all values of BRZ are understood to be relative to the initial position of the projectile. Corresponding resistance exerted on projectile when base is BR (1) at BRZ(1) (psi). BRZ (NBRES) Last location. BR (NBRES) Corresponding resistance. "Air Shock Data" (4F10.0) One Card File [C12.1] This file is required if and only if IBRES = 4 or 6. (See File [M2].) Ratio of specific heats of gas in front of projectile (-). **AIRGAM** Initial pressure of gas in front of projectile (psi). AIRP0 AIRT0 Initial temperature of gas in front of projectile (R). Molecular weight of gas in front of projectile (lbm/lbmol). **AIRMW** "Projectile Setback Resistance Data" (4F10.0)One Card File [C12.2] The file is required if and only if IBRES = 5 or 6. (See File [M2].) PRMU Coefficient of friction between projectile body and tube wall (-). Poisson ratio of projectile material (-). PRNU Length of projectile (in). PRLEN Length of projectile in contact with wall (in). PRLENC

If < 10-10, PRLENC defaults to PRLEN.

File [C13] "Tube Thermal Properties" (3F10.0) One Card

N.B. File required if and only if JHTW # 0. (See File [M2].)

KW

Thermal conductivity (lbf/sec/R).

ALPHAW

Thermal diffusivity (in2/sec).

ALFAW

Emissivity factor (-).

File [C14] "Tube Initial Temperature Profile" (8F10.0) One to Three Cards

N.B. File required if and only if NTEM # 0. (See File [M4].)

ZW (1) First axial location relative to breech (in).

TEMW(1) Corresponding wall temperature (R).

ZW (NTEM)

Last location.

TEMW (NTEM)

Corresponding temperature.

File [C17.5] "Blowdown Parameters" (8F10.0) One Card

File required if and only if NBLWDN = 1. (See File [M2].) N.B.

PBRF

Value to which breech pressure must drop for termination of blowdown calculation (psi).

PBRFZ

Distance from breech at which PBRF is determined (in).

UBRF

Value to which velocity must drop for termination of

blowdown calculation (in/sec).

UBRFZ

Distance from breech at which UBRF is determined (in).

CDMUZ

Discharge coefficient for muzzle discharge (-).

If CDMUZ $< 10^{-10}$, it defaults to 1.0.

File [M13] "Projectile and Rifling Characteristics" (4F10.0) One Card This file is not required if NTC or NTLC = 1. (See File [M2].) N.B. **ZBPR** Initial axial location of base of projectile relative to breech (in). Mass of projectile (lbm). WTPR Polar moment of inertia of projectile (1bm-in2). PRIN Angle of rifling(°). RIF Base area of projectile (in^2) . If ABPROJ > 10^{-10} it will be used as the propulsion area for the projectile whenever **ABPROJ** it is less than the bore area at the base. TUBEM Mass of recoiling parts of gun (lbm). If TUBEM is zero, recoil of the tube is not considered. "I-th Forward Compactible Filler Element Properties" File [C18] (3F10.0),2I5) One Card File required if and only if NEL # 0. (See File [M4].) File is N.B. repeated NEL times. XEL(I) Position of left-hand boundary of I-th element (in). The array must be well ordered with respect to I. We require $XEL(I) \ge XEL(I-1)$. Forward elements are ordered so that the first is to the left. Mass of I-th element (lbm). If $< 10^{-10}$ element is MEL(I) interpreted as a space. MEL(I) must be greater than 10-10. Initial resistance to motion of I-th element (lbf). FEL(I) If NTYPE(I) = 0, element is treated as perfectly plastic NTYPE (I) (deformation under loading only). If NTYPE(I) = 1, element is treated as elastic. If NTYPE(I) = 2, element is treated as rigid. If NTYPE(I) = 3, element is treated as incompressible. $0 \le NTYPE(I) \le 3.$

element. $0 \le NDATA(I) \le 10$.

NDATA(I)

Number of pairs of entries in stress-strain table of I-th

- File [C19] "Constitutive Data for I-th Forward Element" (8F10.0)
 One to Three Cards
- N.B. File required if and only if MEL(I) > 10⁻¹⁰ and NTYPE(I) < 2. (See File [C18].) File is repeated for each element for which NDATA > 0. Files [C19], as a group, follow Files [C18], as a group.
- YEL(I,1)* First engineering strain taken positive in compression (dimensionless). Must be zero.
- RESEL(I,1) ** Corresponding stress taken positive in compression (psi).
- RESEL(I,NDATA(I)) Last engineering stress. Should exceed maximum pressure in qun.
- * The array YEL must be well ordered. All entries must be in the interval [0,1].
- The array RESEL must have non-zero entries and must be non-decreasing for each element.
- File [C19.1] "I-th Rear Compactible Filler Element Properties" (3F10.0,2I5)
 One Card
- N.B. File required if and only if NBL # 0. (See File [M4].) File is repeated NBL times.
- XBL(I) Position of right-hand boundary of I-th element (in). The array must be well ordered with respect to I. XBL(I) observes the opposite convention from that of XEL(I), that is $XBL(I) \leq XBL(I-1)$ for all I. Rear elements are tabulated so that the first is to the right.
- MBL(I) Mass of I-th element (1bm). If $< 10^{-10}$ element is interpreted as a space. MBL(I) must be greater than 10^{-10} .
- NTYPB(I) If NTYPB(I) = 0, element is treated as perfectly plastic (deformation under loading only).

 If NTYPB(I) = 1, element is treated as elastic

 If NTYPB(I) = 2, element is treated as rigid.

 If NTYPB(I) = 3, element is treated as incompressible.

 0 \le NTYPB(I) \le 3.
- NDATB(I) Number of pairs of entries is stress-strain table of I-th element. 0 ≤ NDATB(I) ≤ 10.

File [C19.2] "Constitutive Data for I-th Rear Element" (8F10.0)
One to Three Cards

N.B. File required if and only if MEL(I) > 10^{-10} and NTYPE(I) < 2. (See File [C19.1].) File is repeated for each element for which NDATB > 0. Files [C19.2], as a group, follow Files [C19.1], as a group.

YBL(I,1) * First engineering strain taken positive in compression (dimensionless). Must be zero.

RESBL $(I,1)^{**}$ Corresponding stress taken positive in compression (psi).

RESBL(I,NDATB(I)) Last engineering stress. Should exceed maximum pressure in gun.

File [C23] "Positions for Pressure Table Storage" (8F10.0) One Card

N.B. File required if and only if NZPT # 0. (See File [M4].)

ZPT(1) First position, relative to breech (in).

ZPT(NZPT) Last position.

^{*} The array YBL must be well ordered. All entries must be in the interval [0,1].

^{**} The array RESBL must have non-zero entries and must be non-decreasing for each element.

^{*} Output consists of tables of pressure at each of the NZPT positions together with value less that at the NZPTth position.

```
File [C23.01] "Projectile Afterbody Pressure History Option" (1615)
One Card
```

N.B. File required if and only if NZPT = 0 and MODET = 1. (See File [M4].)

IZPT(1)

0 if ZPT(1) is fixed in the tube reference frame.
1 if ZPT(1) is fixed in the projectile afterbody

reference frame.

IZPT (NZPT)

MODZPT

0 if gas pressure is tabulated.

1 if intergranular stress is tabulated.

2 if sum of pressure and intergranular stress is tabulated.

File [C23.1] "Kinetics Option Counters" (315) One Card

N.B. File required if and only if KMODE # 0. (See File [M2].)

NSPEC Number of species. $1 \le NSPEC \le 10$.

NGASR Number of reactions occurring in the mixture of combustion

products. $0 \le NGASR \le 10$. If NGASR > 0, File [C23.7] is

required.

NSOLR Number of reactions occurring in the solid-propellant.

 $0 \le NSOLR \le 10$. If NSOLR > 0, File [C23.8] is required.

KEOS 0 if thermal energy formulation is used.

1 if total energy formulation is used.

Data as per NASA SP-273 and the present File [C23.2] is replaced by File [C23.21]. Values of ECHO are to be entered as heat of formation and not as heat

released in near field combustion zone, see Files

[C23.3], [C23.31], [C23.4] and [C23.41].

This option is presently confined to gas-phase species.

ECHO for chemical energy not required.

NPVAR(1) Number of data to specify composition of local products

of first propellant. NPVAR may be zero, in which case the present file [C23.3] is used or it may be between

2 and 20, in which case new file [C23.31] is required.

NPVAR (NPROP) Data for last propellant.

NPVAR (NPROP+1) Data for igniter composition. Note that if NPROP

is 1, this item goes in the sixth field. If it is 0, present File [C23.4] is required, otherwise

we require [C23.41].

| File [C23.2] | "Properties of Species" (2A4,1X,A1,6F10.0) NSPEC Cards |
|---------------|---|
| | puired if and only if KMODE \neq 0 (See File [M2]) and KEOS = 0 e [C23.1]). |
| SPCNAM(I) | Name of species, up to 8 alphanumeric characters. |
| FAZE(I) | Phase of species: $G = gas$ or vapor; $L = liquid$; $S = solid$. One alphanumeric character. |
| SPCV(I) | Specific heat at constant volume (lbf-in/lbm-R). |
| SPCP(I) | Specific heat at constant pressure (lbf-in/lbm-R). |
| SPBV(I) | Covolume (in^3/lbm) . Only required if FAZE = G. |
| SPMOL(I) | Molecular weight (lbm/lbmol). Only required if FAZE = G. |
| SPDEN(I) | Density (lbm/in^3). Only required if FAZE = L or S. |
| CLOS(I) | Transfer coefficient in correlation for rate of deposition of condensed species on surface of solid propellant (sec/in²). Only required if FAZE = L or S. If CLOS = 0, the rate of deposition is zero. |
| | |
| File [C23.21] | "Properties of Species in NASA SP-273 Formulation" (Al0,5F10.0/5E15.8/5E15.8/5E15.8) 4*NSPEC cards |
| N.B. The data | consist of 4 cards for each of the NSPEC species. |
| SPCNAM(I) | Name of species I. Up to 10 characters. |
| TLO(I) | Lower limit of data (K). |
| TSW(I) | Switching point of data (K). |
| THI(I) | Upper limit of data (K). |
| SPBV(I) | Covolume (in**3/lbm). |
| SPMOL(I) | Molecular weight (lbm/lbmol). |
| A(1,I) | First NASA SP datum for specific heat. New card. |
| • | |
| A(5,I) | |
| A(6,I) | Sixth datum. New card. |
| | |
| • | |

A(11,I) Eleventh datum. New card.

A(15,I)

N.B. TLO and THI are not presently checked when subroutine CALEOS is called. The user may want to include an appropriate test and subsequent message/action. This file is actually read by CALEOS rather than NOVSUB in order to make it easier for the user to make revisions.

N.B. The following File [C23.3] is repeated NPROP times, once for each type of solid propellant.

File [C23.3] "Composition of Propellant Near Field Combustion Products" (8F10.0) NPROP to 2*NPROP Cards

N.B. File required if and only if KMODE # 0 (See File [M2])
and NPVAR(I) = 0 (See File [C23.1]).

ECHO(I) Chemical energy released in near field combustion (lbf-in/lbm).

YO(I,1) Mass fraction of near field combustion products corresponding to species type 1 (-).

YO(I,NSPEC) Mass fraction of near field combustion products corresponding to species type NSPEC (-).

File [C23.31] "Pressure Dependent Composition of Propellant Near Field Combustion Products" (F10.0/(8F10.0))
1+NPROP to 1+2*NPROP cards.

N.B. File required if and only if KMODE \neq 0 (See File [M2]) and NPVAR(I) \neq 0 (See File [C23.1]).

ECHO(I) Chemical energy released in near field combustion (KEOS=0) or heat of formation of propellant (KEOS=1) (lbf-in/lbm).

PVAR(I,1) First value of pressure. (psi). New card.

YOVAR(I,1,1) Corresponding mass fraction of first species in near field combustion (-).

YOVAR (I, 1NSPEC) Mass fraction of last species.

```
Second value of pressure. New card.
PVAR(I,2)
YOVAR (I, NPVAR (I), NSPEC)
      Inside the table range YOVAR is linearly interpolated.
N.B.
      Outside, the first or last set of values are used.
              "Composition of Igniter Discharge Combustion Products"
File [C23.4]
               (8F10.0) One to Two Cards
      File required if and only if KMODE \neq 0 (See File [M2]) and
N.B.
      NPVAR(I) = 0. (See File [C23.1].)
                Chemical energy released by combustion of igniter material
ECHO(I)
                prior to injection (lbf-in/lbm).
                Mass fraction of igniter products corresponding to species
YO(I,1)
                type 1 (-).
                Mass fraction of igniter products corresponding to species
YO(I, NSPEC)
                type NSPEC (-).
               "Pressure Dependent Composition of Igniter Discharge
FILE [C23.41]
                Combustion Products" (F10.0/(8F10.0))
                1 + NPROP to 1 + 2*NPROP cards
      File required if and only if KMODE \neq 0 (See File [M2]) and
N.B.
                    (See File [C23.1].)
      NPVAR(I) \neq 0.
               Chemical energy released in near field
ECHO(I)
               combustion (KEOS=0) or heat of formation
               of igniter products (KEOS=1) (lbf-in/lbm).
               First value of pressure. (psi). New card.
PVAR(I,1)
               Corresponding mass fraction of first species
YOVAR (I, 1, 1)
               in near field combustion (-).
YOVAR (I, 1NSPEC) Mass fraction of last species.
               Second value of pressure. New card.
PVAR (1,2)
YOVAR (I, NPVAR (I), NSPEC)
```

```
File [C23.5]
              "Composition of Initial Ambient Gas"
                                                      (8F10.0)
               One to Two Cards
      File required if and only if KMODE # 0. (See File [M2].)
ECHO(I)
                 Internal energy (thermal component) of ambient gas (or
                mixture if condensed species are initially present)
                 (lbf-in/lbm).
YO(I,1)
                Mass fraction of species 1 (-).
YO(I, NSPEC)
                Mass fraction of species NSPEC (-).
      The following File is repeated NPROP times, once for each type of
N.B.
      solid propellant. Present storage limits only support the case
      NPROP = 1 with KMODE = 2.
File [C23.6]
              "Initial Composition of Solid Propellant"
                                                          (8F10.0)
               NPROP to 2*NPROP Cards
      File required if and only if KMODE = 2.
N.B.
                                                (See File [M2].)
ECHO(I)
                Inactive.
                Mass fraction of solid propellant corresponding to species 1
Y0(I,1)
                 (-).
                Mass fraction of solid propellant corresponding to species
 YO(I, NSPEC)
                NSPEC (-).
               "Composition of Traveling Charge Near Field Combustion
File [C23.61]
                           (8F10.0) One to Two Cards
                Products"
N.B.
      File required if and only if KMODE \neq 0 and NTC = 1.
                                                            (See File [M2].)
ECHTC0
                Chemical energy released in near field combustion of
                traveling charge (lbf-in/lbm).
YTC0(1)
                Mass fraction of species 1 (-).
                Mass fraction of species NSPEC (-).
YTC0 (NSPEC)
```

```
"Types of Reactions in Mixture of Combustion Prooducts"
File [C23.62]
                (10I5) One Card
      File required if and only if KMODE \neq 0, NGASR \neq 0 and NTC = 1.
N.B.
      Files [M2] and [C23.1].)
                If 0, reaction 1 is of the Arrhenius type and is described
KRCTYP(1)
                by File [C23.7].
                If 1, reaction 1 is of the pressure dependent type and is
                described by File [C23.71].
                If NTC = 0, KRCTYP(I) defaults to zero for all I.
              Type of reaction NGASR.
KRCTYP (NGASR)
              "Species Thermal Equilibrium Switches" (1015) One Card
File [C23.63]
      File required if and only if KMODE \neq 0, NGASR \neq 0 and NTC = 1.
      (See Files [M2] and [C23.1].)
                If 0, species 1 is assumed to be in constant thermal
KTEOL(1)
                equilibrium with mixture of combustion products.
                If 1, species 1 is assumed to be thermally insulated from
                mixture of combustion products. If NTC = 0, KTEQL(I)
                defaults to zero for all I.
                Thermal equilibration switch for species NSPEC.
KTEOL (NSPEC)
              "Description of Arrhenius Reactions in Mixture of Combustion
File [C23.7]
               Products" (815/8F10.0/F10.0,D10.4,F10.0,D10.4,4F10.0/F10.0)
               Four Cards For Each Such Reaction
      File required if and only if KMODE \neq 0, NGASR \neq 0 and KRCTYP(I) = 0.
N.B.
      (See Files [M2], [C23.1] and [C23.62].)
KRCNTB(1,I)*
                Pointer to first species acting as a reactant in reaction I.
                0 ≤ KRCNTB ≤ NSPEC.
                Pointer to fourth species acting as a reactant in
KRCNTB(4,I)
                reaction I.
                Pointer to first species acting as a product in reaction I.
KPRODB(1,I)
                0 ≤ KPRODB ≤ NSPEC.
               Pointer to fourth species acting as a product in reaction I.
KPRODB(4,I)
```

| STOIB(1,I) | Stoichiometric coefficient corresponding to first reactant species (-). Starts a new card. |
|------------|--|
| • | |
| STOIB(4,I) | Stoichiometric coefficient corresponding to fourth reactant species (-). |
| STOIB(5,1) | Stoichiometric coefficient corresponding to first product species (-). |
| STOIB(8,I) | Stoichiometric coefficient corresponding to fourth product species (-). |
| ECHB(I) | Chemical energy released by reaction (lbf-in/lbm). Starts a new card. |
| ARCB(I) | Pre-exponential factor in Arrhenius rate law (units yield lbmol/in3-sec). |
| ARXB(I) | Temperature exponent in Arrhenius rate law (-). |
| AREB(I) | Activation energy in Arrhenius rate law (lbf-in/lbmol). |
| AROB(1,I) | Order of reaction with respect to concentration of first reactant species (-). |
| • | |
| AROB(4,I) | Order of reaction with respect to concentration of fourth reactant species (-). |
| AROB(5,I) | Order of reaction with respect to concentration of gasphase (-). Starts a new card. |

^{*} The most general reaction supported involves four reactant and four product species. At least one reactant pointer and one product pointer must be different from zero. A zero entry simply implies a reduction in generality of the reaction.

File [C23.71] "Description of Pressure-Dependent Reactions in Mixture of Combustion Products" (815/8F10.0/8F10.0) Three Cards For Each Such Reaction File required if and only if KMODE \neq 0, NGASR \neq 0 and KRCTYP(I) = 1. N.B. (See Files [M2], [C23.1] and [C23.62].) Pointer to first species acting as a reactant in reaction I. KRCNTB(1,I) 0 ≤ KRCNTB ≤ NSPEC. Pointer to fourth species acting as a reactant in KRCNTB(4,I) reaction I. Pointer to first species acting as a product in reaction I. KPRODB(1,I)* $0 \le KPRODB \le NSPEC.$ Pointer to fourth species acting as a product in reaction I. KPRODB(4,I) Stoichiometric coefficient corresponding to first reactant STOIB(1,I) species (-). Starts a new card. Stoichiometric coefficient corresponding to fourth reactant STOIB(4,I) species (-). Stoichiometric coefficient corresponding to first product STOIB(5,I) species (-). Stoichiometric coefficient corresponding to fourth product STOIB(8, I) species (-). Chemical energy released by reaction (lbf-in/lbm). Starts a ECHB(I) new card. Particle diameter, assumed constant (in). DIAB(I) Burn rate additive constant (in/sec). B1B(I) Burn rate pre-exponential factor (in/sec-psi^{BNB}). B2B(I) Burn rate exponent (-). BNB(I)

The most general reaction supported involves four reactant and four product species. At least one reactant pointer and one product pointer must be different from zero. A zero entry simply implies a reduction in generality of the reaction.

| File [C23.8] | "Description of Reactions in Solid Propellant" (815/8F10.0/F10.0,D10.4,F10.0,D10.4,4F10.0) 3*NSOLR Cards |
|-------------------------|--|
| N.B. File re and [C2 | equired if and only if KMODE # 0, NSOLR # 0. (See Files [M2] 23.1].) |
| KRCNTS(1,1)* | Pointer to first species acting as a reactant in reaction I. $0 \le \text{KRCNTS} \le \text{NSPEC}$. |
| KRCNTS(4,I) | Pointer to fourth species acting as a reactant in reaction |
| KPRODS(1,I)* | Pointer to first species acting as a product in reaction I. $0 \le \text{KPRODS} \le \text{NSPEC}$. |
| . KPRODS (4, I) | Pointer to fourth species acting as a product in reaction I. |
| STOIS(1,I) | Stoichiometric coefficient corresponding to first reactant species (-). Starts a new card. |
| STOIS (4, I) | Stoichiometric coefficient corresponding to fourth reactant species (-). |
| STOIS(5,I) | Stoichiometric coefficient corresponding to first product species (-). |
| STOIS(8,I) | Stoichiometric coefficient corresponding to fourth product species (-). |
| ECHS(I) | Chemical energy released by reaction (lbf-in/lbm). Starts a new card. |
| ARCS(I) | Pre-exponential factor in Arrhenius rate law (units yield lbm/in3-sec). |
| ARXS(I) | Temperature exponent in Arrhenius rate law (-). |
| ARES(I) | Activation energy in Arrhenius rate law (lbf-in/lbmol). |

AROS(1,I) Order of reaction with respect to concentration of first reactant species (-).

AROS(4,I) Order of reaction with respect to concentration of fourth reactant species (-).

The most general reaction supported involves four reactant and four product species. At least one reactant pointer and one product pointer must be different from zero. A zero entry simply implies a reduction in generality of the reaction.

| File | [C23.9] | "Solid Propel | lant Thermal | Response | Parameters" |
|------|---------|---------------|--------------|----------|-------------|
| | - | (315,2D10.4,3 | F10.0) One | Card | |

N.B. File required if and only if KMODE = 2. (See File [M2].)

| NZC | Number of stations for analysis of thermal response of solid |
|-----|--|
| | propellant. 0 ≤ NZC ≤ 21. It is presently assumed that |
| | only one propellant region is present. |

NZCBC If 0, pyrolysis law is assumed to govern regression of surface of solid propellant.

If 1, evaporative (Clausius Clapeyron) law is assumed to govern regression of surface of solid propellant.

NOFLAM

If 0, heat feedback from the gas-phase is considered according to Zel'dovitch formulism.

If 1, heat feedback from the gas-phase is neglected.

AS Pre-exponential factor in solid propellant surface regression law. If NZCBC = 0, units are in/sec. If NZCBC = 1, units are psi.

ES Activation energy (NZCBC = 0) or heat of vaporization (NZCBC = 1) in solid propellant surface regression law (lbf-in/lbmol).

TSEN Temperature sensitivity of propellant steady state burn rate (1/R).

TTRANS

Time interval over which external stimulus drops to zero following ignition of the surface of the propellant (sec).

PTRANS Pressure above which thermal analysis is discontinued and steady state combustion is assumed to occur (psi).

| File [C | "Parameters to Define Mesh in Invariant Embedding Analysis" (F10.0,315) One Card |
|---------|---|
| N.B. F | ile required if and only if KMODE = 2. (See File [M2].) |
| DELX* | Mesh spacing in group closest to heated surface ($\sec^{1/2}$) DELX > 0. |
| N** | Number of intervals per group. |
| MDELX | Integer multiple by which mesh spacing increases from group to group as we move away from heated surface. |
| NGRP | Number of groups. 1 ≤ NGRP ≤ 10. |

Refers to computational coordinate $x\sqrt{\alpha}$ where x is the distance from heated surface and α is thermal diffusivity.

^{**} N*NGRP \leq 200.

| File [C25] | "Tank Gun | Option | Control | Data" | (16I5) | One Card |
|------------|-----------|--------|---------|-------|--------|----------|
|------------|-----------|--------|---------|-------|--------|----------|

N.B. File required if and only if MODET = 1. (See File [M2].)

NAFT Number of pairs of data to describe projectile afterbody. NAFT may be zero. Otherwise $2 \le NAFT \le 10$.

JIS(1) Switch to define level of modeling of surface source term attributed to tube wall.

| <u>JIS(1)</u> | WodeT |
|---------------|--|
| 0 | No source term |
| 1 | Tabular source term |
| 2 | Rate of source determined according to ignition and combustion submodels. |
| JIS(2) | Switch to define level of modeling of surface source term attributed to centerline of tube. |
| JIS(3) | Switch to define level of modeling of surface source term attributed to afterbody of projectile. |
| NENDL | Number of endwalls defined by packaging of charge. $0 \le NENDL \le 21$. |

| NPRM | Number of permeability data sets. $0 \le NPRM \le 10$. |
|------------|---|
| NRCT | Number of reactivity data sets. $0 \le NRCT \le 9$. |
| NSEGS (1) | Number of segments having different properties in tube wall surface source. $0 \le NSEGS(1) \le 3$. Default value is 1. |
| NSEGS (2) | Number of segments in centerline surface source. |
| NSEGS (3) | Number of segments in afterbody surface source. |
| KCTRL | If 0, control charge not present. If 1, control charge is present. Files [C28] - [C28.7] required. |
| NZCRE | Number of data to describe external geometry of ballistic control tube. |
| INHBCR (1) | If 0, control charge not deterred. If 1, control charge is deterred. |
| NABDIS . | If 0, discontinuity in area at base of afterbody is represented implicitly. If 1, discontinuity in area at base of afterbody is represented explicitly as a discontinuity. File [C25.11] is required. |

| File [C25.1] | "Geometry of Projectile Afterbody" | (8F10.0) | One to Three | |
|--------------|------------------------------------|----------|--------------|--|
| | | | Cards | |

N.B. File required if and only if MODET = 1 and NAFT \geq 2. (See Files [M2] and [C25].)

ZAFT (NAFT) Last axial position.

RAFT(NAFT) Corresponding radius of afterbody.

ZAFT(1) * First axial position on afterbody (in).

RAFT(1) Corresponding radius of afterbody (in).

The origin of the coordinate ZAFT is independent of that used to describe the gun tube. XKTC internally reconciles the coordinate frames by assuming that ZAFT(NAFT) coincides with ZBPR. (See File [M13].)

- File [C25.11] "Spatial Resolution Factor for Analysis of Base of Afterbody as Surface of Area Discontinuity" (F10.0) One Card
- N.B. This file is required if and only if MODET = 1 and NABDIS = 1. (See File ([C25].)
- RZOLV2 Spatial resolution factor (-). Recommended value is < 0.01. It should be noted that this datum is completely independent of RZOLV (File [M3]). RZOLV2 is used to determine the maximum proximity of a mixture boundary to the base of the projectile.
- N.B. The following Files, [C25.2] through [C26.3] are repeated, as needed, as a group for each of the three types of reactive layers whose presence is indicated by a non-zero value of JIS(I).
 (See File [C25].)
- File [C25.2] "Thickness and Density Counters for Reactive Layer I" (415)
 One Card
- N.B. File required if and only if MODET = 1 and JIS(I) \neq 0. (See Files [M2] and [C25].)
- NSTAC(I) Number of data to describe thickness of reactive layer I. $2 \le NSTAC(I) \le 10$.
- NRHOS(I,1) Number of data to describe density of first segment of reactive layer I as a function of pressure. $1 \le NRHOS(I) \le 10$.
- NRHOS(I,2) Number of data for second segment of reactive layer I.
- NRHOS(I,3) Number of data for third segment.

File [C25.3] "Thickness of Reactive Layer I" (8F10.0) One to Three Cards

- N.B. File required if and only if MODET = 1 and JIS(I) \neq 0. (See Files [M2] and [C25].)
- ZAC(1,I) * First axial position (in).
- THC(1,1) Corresponding thickness of reactive layer (in).
- ZAC(NSTAC(I),I) Last axial position.
- THC(NSTAC(I),I) Corresponding thickness.

When I = 1 or 2, ZAC is assumed to refer to the coordinate system used to define the tube geometry. When I = 3, ZAC is assumed to correspond to the coordinate system used to define the afterbody of the projectile. The thickness of layer I is taken to be zero outside the table range.

File [C25.31] "Segment Pointers for Reactive Layer I" (815) One Card

N.B. File required if and only if MODET = 1, JIS(I) \star 0 and NEGS(I) > 1. (See Files [M2] and [C25].)

NSG(1,I) Segment property type for axial positions between ZAC(1,I) and ZAC(2,1).

NSG(NSTAC(I)-1,I) Segment property type for axial positions between ZAC(NSTAC(I)-1,I) and ZAC(NSTAC(I),I).

NSG(NSTAC(I),I) Not used.

N.B. If Reactive Layer I consists of more than one segment, the following Files [C25.4] through [C26.21] are repeated as a group for each of the segments of the layer. The subscript pertaining to the segment is suppressed in the following discussion.

File [C25.4] "Density of Reactive Layer I" (8F10.0) One to Three Cards

N.B. File required if and only if MODET = 1 and JIS(I) \neq 0. (See Files [M2] and [C25].)

RHOS(1,I) * Value of density at first pressure {lbm/in³).

PRHOS(1,I) First value of pressure (psi).

RHOS(NRHOS(I),I) Last value of density.

PRHOS (NRHOS (I), I) Last value of pressure.

Outside the table range, the first or the last value of RHOS applies. If a single value is specified, the density is taken to be constant and therefore independent of pressure. At present, case compressibility is only modeled if JIS(I) = 2. (See File [C25].)

```
File [C25.5]
              "Counter to Describe Discharge of Reactive Layer I" (215)
               One Card
      File required if and only if MODET = 1 and JIS(I) = 1.
      (See Files [M2] and [C25].)
                Number of axial positions in discharge table.
IIS(I)
                2 \le IIS(I) \le 10.
JJS(I)
                Number of times in discharge table. 2 \le JJS(I) \le 10.
File [C25.6]
              "Times to Describe Discharge of Reactive Layer I" (8F10.0)
               One to Two Cards
N.B. File required if and only if MODET = 1 and JIS(I) = 1.
      (See Files [M2] and [C25].)
                  First time (msec).
TPHIS(1,1)
TPHIS(JJS(I),I) Last time (msec).
File [C25.7] "Positions to Describe Discharge of Reactive Layer I"
               (8F10.0) One to Two Cards
N.B. File required if and only if MODET = 1 and JIS(I) = 1.
      (See Files [M2] and [C25].)
ZPHIS(1,I)*
                 First position (in).
```

Last position (in).

ZPHIS(IIS(I),I)

The coordinate frame for ZPHIS is assumed to accord with that for ZAC. (See File [C25.3].)

- File [C25.8] "Rate of Discharge of Reactive Layer I" (8F10.0) One to Thirteen Cards
- N.B. File required if and only if MODET = 1 and JIS(I) = 1.
 (See Files [M2] and [C25].)
- PHIS(1,1,I) Rate of discharge at first position and first time (lbm/in-sec).
- PHIS(2,1,I) Rate of discharge at second position and first time.
- PHIS(IIS(I),1,I) Rate of discharge at last position and first time.
- PHIS(1,2,I) Rate of discharge at first position and second time. Starts a new card.
- PHIS(IIS(I), JJS(I), I) Rate of discharge at last position and last time.

File [C25.9] "Burn Rate Counters for Reactive Layer I" (215) One Card

- N.B. File required if and only if MODET = 1 and JIS(I) = 2. (See Files [M2] and [C25].)
- KBRDS(I) Number of burn rate data. $1 \le KBRDS \le 10$.
- KNHIB(I) If 0, layer I is not deterred.

 If 1, layer I is deterred
- KFACSF(I) If 0, the nominal surface area is used. If $2 \le \text{KFACSF}(I) \le 10$, the surface area is multiplied by a value which depends on surface regression. File [C26.31] is required.

```
File [C26]
             "Burn Rate Data for Reactive Layer I"
                                                      (8F10.0)
              One to Three Cards
       File required if and only if MODET = 1 and JIS(I) = 2.
       (See Files [M2] and [C25].)
UPPRS(1,I)*
                 First pressure limit (psi).
                 Value of pre-exponent for pressures less than UPPRS(1,I)
B22S(1, I)
                 (in/sec-psi<sup>BNNS</sup>).
BNNS (1, I)
                 Value of exponent for pressures less than UPPRS(1,I) (-).
UPPRS(KBRDS(I),I)*
                      Last pressure limit (psi).
B22S (KBRDS (I), I)
                      Value of pre-exponent for pressures less than
                      UPPRS(KBRDS(I),I) but greater than UPPRS(KBRDS(I)-1,I).
BNNS (KBRDS (I), I)
                      Corresponding exponent (-).
   Outside the table range the first and last values are used.
File [C26.1]
               "Ignition Data for Reactive Layer I"
                                                      (5F10.0)
                                                                 One Card
N.B.
      File required if and only if MODET = 1 and JIS(I) = 2.
      (See Files [M2] and [C25].)
B1S(I)
                 Burn rate additive constant (in/sec).
TMPIGS(I)
                Ignition temperature (R).
KPS(I)
                 Thermal conductivity (lbf/sec-R).
ALPHAS(I)
                 Thermal diffusivity (in2/sec).
ALFCC(I)
                Emissivity factor (-).
File [C26.2]
               "Thermochemical Data for Reactive Layer I" (8F10.0)
                                                                       One Card
      File required if and only if MODET = 1 and JIS(I) = 1 or 2.
N.B.
      (See Files [M2] and [C25].)
EIGS(I)
                Chemical energy released during combustion (lbf-in/lbm).
                Molecular weight of products of combustion (lbm/lbmol).
GMS(I)
                Ratio of specific heats (-).
GAMAS(I)
```

```
File [C26.21] "Composition of Reactive Layer Near Field Combustion
                Products" (8F10.0)
                                      One Card
      File required if and only if MODET = 1, KMODE = 1 and JIS(I) = 1 or 2.
N.B.
      (See Files [M2] and [C25].)
                Mass fraction of species 1 (-).
               Mass fraction of species NSPEC (-).
YSO(I, NSPEC)
              "Properties of Deterred Layer of Reactive Layer I" (5F10.0)
File [C26.3]
               One Card
      File required if and only if MODET = 1, JIS(I) = 2 and KNHIB(I) = 1.
N.B.
      (See Files [M2], [C25] and [C25.9].)
ECHIS(I)
                Internal energy released in combustion at start of deterred
                layer (lbf-in/lbm).
                Internal energy released in combustion at end of deterred
ECHIS2(I)
                layer (lbf-in/lbm).
RGFAS(I)*
                Factor by which burn rate is multiplied at start of deterred
                layer (-).
                Factor by which burn rate is multiplied at end of deterred
RGFAS2(I)
              · layer (-).
HIBS(I)
                Depth of deterred layer (in).
   Values within deterred layer deduced by linear spacewise interpolation
   with an allowance for compression of the reactive layer. Final values
   need not be the same as those of the undeterred layer.
               "Surface Area Multiplier for Reactive Layer I"
                                                                 (2F10.0)
File [C26.31]
                KFACSF(I) Cards
```

DBITSF(1,I) First value of surface regression (in).

RFACSF(1,I) Corresponding surface area multiplier (-).

DBITSF(2,1) Second value of surface regression. Starts a new card.

RFACSF(KFACSF(I),I) Last value of multiplier.

N.B. This file is required if and only if MODET = 1 and JIS(I) = 2 and KFACSF(I) \geq 2. (See Files [M2], [C25] and [C25.9].)

| File [C26.4] | "Endwall Property Pointers" (615) NENDL Cards |
|--------------|---|
| | equired if and only if MODET = 1 and NENDL = 0. iles [M2] and [C25].) |
| NBAGL(I) | Pointer to propellant increment to which I-th endwall is attached. If NBAGL(I) = 0, the endwall is assumed to be attached to the breech of the gun. An increment may include several parallel packaged bundles of propellant. |
| NBAGE (I) | If 0, endwall is at rear of increment. If 1, endwall is at front of increment. |
| NREACT(I) | Pointer to reactivity models associated with endwall. NREACT is interpreted as a four digit number. Each digit points to a different model. A zero value implies no reactivity. The digits have the following meanings |
| | Digit Source of Reactivity |
| | 1 Internal attached component |
| | 2 Interior of endwall |
| | 3 Exterior of endwall |
| | 4 External attached component |
| NPERM(I) | Pointer to permeability model associated with endwall. |
| NPRAT(I) | <pre>If 0, force on endwall is transmitted to propellant. If 1, force on endwall is transmitted to projectile.</pre> |
| File [C26.5] | "Permeability Model Data" (8F10.0) NPRM Cards |
| | equired if and only if MODET = 1 and NPRM \neq 0. iles [M2] and [C25].) |
| PRM(I) | Initial flow resistance coefficient for I-th model (-). |
| RUPSTR(I) | Pressure differential at which rupture of endwall commences |

RUPINT(I)

(psi).

(msec).

Time interval over which rupture of endwall is completed

N.B. The following Files, [C26.6] through [C27], are repeated as a group for each of the NRCT reactivity models.

File [C26.6] "File Counters for I-th Reactivity Model" (315) One Card File required if and only if MODET = 1 and NRCT \neq 0. N.B. (See Files [M2] and [C25].) KBRDE (I) Number of data in modeled burn rate description (-). If KBRDE(I) = 0, it is assumed that tabular discharge data are specified. $0 \le KBRDE(I) \le 10$. Ignition criterion for modeled burn rate description. IGCRIT(I) Ignition is determined by reference to VALIG(I) (File [C26.8]) as follows. IGCRIT(I) VALIG(I) 1 Time Delay (msec) 2 Ambient gas temperature (R) Neighboring propellant temperature (R) 3 Number of data in tabular burn rate description (-). JRCT(I) $JRCT(I) = 0 \text{ or } 2 \le JRCT(I) \le 8.$ File [C26.7] "Thermochemical Data for I-th Reactivity Model" (4F10.0) One Card File required if and only if MODET = 1 and NRCT \neq 0. (See Files [M2] and [C25].) Density (lbm/in3). RHOE (I) Chemical energy released during combustion (lbf-in/lbm). EIGE(I) GME (I) Molecular weight of combustion products (lbm/lbmol). Ratio of specific heats of combustion products (-). GAMAE(I) File [C26.71] "Composition of Near Field Combustion Products of I-th Reactivity Model" (8F10.0) One Card File required if and only if MODET = 1, KMODE \neq 0 and NRCT \neq 0. N.B. (See Files [M2] and [C25].) Mass fraction of species 1 (-). YEE (I, 1)

Mass fraction of species NSPEC (-).

YEE (I, NSPEC)

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File [C26.81
               "Ignition Value for I-th Reactivity Model" (F10.0)
                                                                       One Card
N.B.
      File required if and only if MODET = 1, NCRT \neq 0 and KBRDE(I) \neq 0.
       (See Files [M2], [C25] and [C26.6].)
VALIG(I)
                 Value of time delay (msec), gas temperature (R) or
                 propellant temperature (R) in accordance with IGCRIT(I) as
                 defined above. (See File [C26.6].)
               "Burn Rate Data for I-th Reactivity Model"
File [C26.9]
                                                             (8F10.0)
                One to Three Cards
      File required if and only if MODET = 1, NRCT \neq 0 and KBRDE(I) \neq 0.
        (See Files [M2], [C25] and [C26.6].)
UPPRE (1, I) *
                 First pressure limit (psi).
B22E(1,I)
                 Value of pre-exponent for pressures less than UPPRE(1,1)
                 (in/sec-psi<sup>BNNE</sup>).
                 Value of exponent for pressures less than UPPRE(1,I) (-).
BNNE (1, I)
UPPRE (KBRDE (I), I)
                        Last pressure limit (psi).
B22E (KBRDE (I), I)
                        Value of pre-exponent for pressures less than
                        UPPRE(KBRDE(I),I), but greater than
UPPRE (KBRDE (I) -1, I).
BNNE (KBRDE(I), I)
                        Corresponding exponent (-).
   Outside the table range the first and last values are used.
File [C27]
            "Tabular Description of I-th Reactivity Model"
                                                               (8F10.0)
            One or Two Cards
      File required if and only if MODET = 1, NRCT # 0, KBRDE(I) = 0 and
N.B.
                     (See Files [M2], [C25] and [C26.6].)
      2 \le JRCT \le 8.
TRCT(1,I)
                 First value of time (msec).
                Corresponding rate of combustion (lbm/in2-sec).
FLORCT(1, I)
                   Last value of time.
```

FLORCT(JRCT(I),I) Corresponding rate of combustion.

TRCT(JRCT(I),I)

"Internal Properties of Control Charge Combustion Chamber" File [C28] (4F10.0) One Card File required if and only if MODET = 1 and KCTRL \neq 0. N.B. (See Files [M2] and [C25].) Discharge coefficient for venting to gun chamber (-). CDCR Internal radius of bore (in). RCRI Initial chamber volume corresponding to zero afterbody VCR0 offset (in3). Initial afterbody offset (in). ZCR0 "External Properties of Control Charge Combustion Chamber" File [C28.1] (3F10.0) NZCRE Cards N.B. File required if and only if MODET = 1 and KCTRL \neq 0. (See Files [M2] and [C25].) First axial position relative to breechface of gun (in). ZCRE(1) Corresponding external radius of chamber (in). RCRE(1) Total sidewall vent area exposed when base of afterbody is AVENT(1) at ZCRE(1) (in²). Second axial position. Starts a new card. ZCRE(2) Last axial position. ZCRE (NZCRE) RCRE (NZCRE) AVENT (NZCRE) One Card "Control Charge Type" (5A4,2F10.0) File [C28.2] File required if and only if MODET = 1 and KCTRL = 0. N.B. (See Files [M2] and [C25].)

GRNMCR Name of propellant. Up to 20 alphanumeric characters.

WGTCR Mass of control charge (lbm).

RHOPCR Density of propellant (lbm/in³).

File [C28.3] "Control Charge Form Function" (I5, 4F10.0) One Card

N.B. File required if and only if MODET = 1 and KCTRL # 0.
(See Files [M2] and [C25].)

NFRMCR Form function indicator. See discussion of File [M8].

Allowable values of NFRMCR are 1, 2, 5, 6 and 7.

ODCR Grain dimension (in). See File [M8].

DPRFCR Grain dimension (in). See File [M8].

GLENCR Grain length (in).

NPRFCR Number of perforations (-).

File [C28.4] "Control Charge Burn Rate Counter" (I5) One Card

N.B. File required if and only if MODET = 1 and KCTRL # 0. (See Files [M2] and [C25].)

NBRDCR Number of sets of values used to describe burn rate. $1 \le NBRDCR \le 10$.

File [C28.5] "Control Charge Burn Rate Description" (8F10.0)
One to Four Cards

N.B. File required if and only if MODET = 1 and KCTRL ≠ 0. (See Files [M2] and [C25].)

UPPCR(1) Maximum value of pressure for corresponding values of burn rate pre-exponential and exponential factors (psi).

B22CR(1) Burning rate pre-exponential factor (in/sec-psiⁿ).

BNNCR(1) Burning rate exponent (-).

UPPCR(NBRDCR) Maximum value for last set of burn rate data.

B22(NBRDCR) Corresponding pre-exponent.

BNN(NBRDCR) Corresponding exponent.

BlCR Burning rate additive constant (in/sec).

DELCR Ignition delay (msec).

File [C28.6] "Control Charge Thermochemistry" (3F10.0) One Card

N.B. File required if and only if MODET = 1 and KCTRL ≠ 0. (See Files [M2] and [C25].)

ECHCR Internal energy released in combustion (lbf-in/lbm).

GMCR Molecular weight of combustion products (lbm/lbmol).

GAMACR Ratio of specific heats (-).

File [C28.7] "Properties of Deterred Layer" (8F10.0) One Card

N.B. File required if and only if MODET = 1 and KCTRL # 0 and INHBCR = 1. (See Files [M2] and [C25].)

ECRIB* Internal energy released in combustion at start of deterred layer (lbf-in/lbm).

ECRIB2 Internal energy released in combustion at end of deterred layer (lbf-in/lbm).

RGFCR Factor by which burn rate is multiplied at start of deterred layer (-).

RGFCR2 Factor by which burn rate is multiplied at end of deterred layer (-).

Depth of inhibited layer (in).

Values within deterred layer deduced by linear spacewise interpolation.
Final values need not be the same as those of the undeterred propellant.

| File | [C29] | "Forward | Boundary | Discharge | Data" | (8F10.0) | One Card | ı i |
|------|-------|----------|----------|-----------|-------|----------|----------|-----|
|------|-------|----------|----------|-----------|-------|----------|----------|-----|

N.B. File required if and only if INBCX = 1. (See File [M2].)

FBAEX Discharge area (in²).

HIBXCR

FBCD Discharge coefficient (-).

FBPMIN Pressure required to open forward vent (psi). Discharge begins when the gas pressure exceeds FBPMIN and then continues as long as it exceeds the atmospheric value.

Backflow is not considered.

"Inbore Rocket Motor Data" File [C30] (8F10.0) Two Cards File required if and only if INBCX = 2. (See File [M2].) N.B. RMP0 Initial mass of rocket motor propellant (1bm). RECHEM Chemical energy of propellant (lbf-in/lbm). RPDEN Density of propellant (lbm/in3). RGAM Ratio of specific heats of motor combustion products (-). RMOLW Molecular weight of motor combustion products (lbm/lbmol). RPOP Operating pressure of motor (psi). RAP0 Initial port area (in2). RTIG1 Delay prior to first venting from motor (msec). RTIG2 Interval from onset of venting to operation at nominal pressure RPOP (msec). RCDEN Density of case material (lbm/in3). RCSTR Tensile yield strength of case material (psi). File [C30.1] "Composition of Rocket Motor Combustion Products" (8F10.0) One or Two Cards File required if and only if INBCX = 2 and KMODE # 0. [M2].) RCYEE (1) Mass fraction of motor combustion products corresponding to species 1 (-).

RCYEE (NSPEC)

species NSPEC (-).

Mass fraction of motor combustion products corresponding to

File [C31] "ETG Control Switches" (415)One Card File required if and only if NETG = 1. (See File [M2].) NETGS Number of plasma jet data sets (-). $1 \le NETGS \le 10$. If 1, propellant type 1 will have surface regression rate MODPET (1) described by usual exponential law in accordance with data of File [M10]. If 2, propellant type 1 will have surface regression rate described by Helmholtz Law with data as given in File [C31.1]. If 3, propellant type 1 will have surface regression rate described by table of values of linear regression versus time as given in Files [C31.2] and [C31.3]. If 4, propellant type 1 will have surface regression rate described by table of value of mass burning rate versus time as given in Files [C31.2] and [C31.3]. Like MODPET(1), but applying to propellant type 2. MODPET (2) Like MODPET(1), but applying to propellant type 3. MODPET (3) The following Files [C31.3] through [C31.3] are repeated as a group for each of the NPROP propellants for which MODPET # 1. (See File [C31].) "I-th Propellant Helmholtz Wiping Coefficient" (F10.0)File [C31.1] One Card File required if and only if NETG = 1 and MODPET(I) = 2. N.B. See Files [M2] and [C31].) Wiping coefficient for propellant type I (-). ETPR2(I) (I5) File [C31.2] "I-th Propellant Tabular Regression Rate Counter" One Card File required if and only if NETG = 1 and MODPET(I) = 3 or 4. N.B. (See Files [M2] and [C31].)

Number of pairs of data in File [C31.3] for propellant

type I (-). $1 \le NPDAT \le 100$.

NPDAT(1)

- File [C31.3] "I-th Propellant Tabular Regression Rate Data" (2F10.0)
 NPDAT(I) Cards
- N.B. File required if and only if NETG = 1 and MODPET(I) = 3 or 4. (See Files [M2] and [C31].)
- TDOTET(1,1) First value of time (msec).
- RDOTET(1,I) First value of regression rate. If MODPET(I) = 3, the value is understood to be the linear regression rate (in/sec). If MODPET(I) = 4, the value is understood to be the mass burning rate (lbm/sec).

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TDOTET(2,I) Second value of time. Starts a new card.

RDOTET (NPDAT (I), I)

- N.B. The data in this file are linearly interpolated within the table range. The first or last values are used outside the table range. If the rate is constant, one pair of data will suffice.
- N.B. The following Files [C31.4] through [C32] are repeated as a group for each of the NETGS plasma jets. (See File [C31].)

File [C31.4] "I-th Plasma Jet File Counters" (215) One Card

- N.B. File required if and only if NETG = 1. (See File [M2].)
- MODPLS(I) = 0, the plasma mixing length is assumed to be constant and the flux is described by the integrated data of Files [C31.7] and [C31.8].

 If MODPLS(I) = 1, the plasma mixing length is assumed to vary in time according to a Prandtl spreading rate criterion with detailed data given by Files [C31.9] and [C32].

 If MODPLS(I) = 2, the plasma mixing length is assumed to be constant and the flux is determined by the capillary model of Powell and Zielinsky.
- NETDAT(I) Number of sets of data in File [C31.8] or [C32] according as MODPLS(I) = 0 or 1 respectively. $2 \le NETDAT(I) \le 100$.

| File [C31.5] | "Global Properties of I-th Plasma Jet" (5F10.0) One Card |
|-----------------|--|
| N.B. File re | quired if and only if NETG = 1. (See File [M2].) |
| ETTOTE (I) | Total plasma energy (lbf-in). |
| ETTOTM(I) | Total plasma mass (lbf-in). |
| ETDIA(I) | Average capillary diameter (in). Only required if MODPLS(I) = 1. |
| ETAVGA(I) | Average ratio of specific heats of plasma (-). |
| ETAVMW(I) | Average molecular weight of plasma (lbm/lbmol). |
| File [C31.6] | "Composition of I-th Plasma Jet" (8F10.0) One Card |
| N.B. File re | quired if and only if NETG = 1 and KMODE \neq 0. (See File [M2].) |
| YET0(I,1) | Mass fraction of species 1 (-). |
| | |
| YETO (I, NSPEC) | Mass fraction of species NSPEC (-). |
| File [C31.7] | "I-th Plasma Jet Mixing Length Parameters in Integrated Format" (3F10.0) One Card. |
| | quired if and only if NETG = 1 and MODPLS(I) = 0 or 2. les [M2] and [C31.4].) |
| ETZO(I) | Distance of injection point from breech of tube (in). |
| ETMIXL(I) | Mixing length (in). |
| FRIN(I) | Fraction of plasma flux directed to internal voidage in cases involving dual-voidage representation of flow through propellant. $0 \le FRIN \le 1$. |

File [C31.71] "Plasma Capillary Data" Unformatted. One Card. N.B. This File is only required if NETG = 1 and MODPLS(I) = 2. (See Files [M2] and [C31.4].) XXRI Capillary radius (m). XXL Capillary length (m). NPTS Number of pairs of data in File [C31.73]. Must not exceed 1000. ITMAX Maximum number of iterations for determination of plasma flux. File [C31.72] "Stoichiometry Coefficients for Plasma Model" Unformatted. Eight Cards. This File is only required if NETG = 1 and MODPLS(I) = 2. (See Files [M2] and [C31.4].) First value (-). RRI(1) Second value. Starts a new card. RRI(2) Last value. RRI(8) "Current History" Unformatted. File [C31.73] NPTS Cards. This File is only required if NETG = 1 and MODPLS(I) = 2. (See Files [M2] and [C31.4].) TPLAS(1) First value of time (sec). Corresponding value of current (amp). XIPLAS(1) Second value of time. Starts a new card. TPLAS(2) XIPLAS (NPTS)

File [C31.8] "I-th Plasma Jet Integrated Data" (4F10.0) NETDAT(I) Cards

N.B. File required if and only if NETG = 1 and MODPLS(I) = 0. (See Files [M2] and [C31.4].)

- ETGT(1,I) First value of time (msec).
- ETGE(1,1) Fraction of total energy delivered by time ETGT(1,1) (-).
- ETGM(1,I) Fraction of total mass delivered by time ETGT(1,I) (-).
- ETGU(1,I) Axial velocity component of plasma jet at time ETGT(1,I) (in/sec).
- ETGT(2, I) Second value in time. Starts a new card.

ETGU (NETDAT (I), I).

N.B. Data in these tables are linearly interpolated within the table range.

The plasma flux is assumed to be zero outside the table range.

File [C31.9] "I-th Plasma Jet Mixing Length Parameters in Detailed Format" (3F10.0) One Card

N.B. File required if and only if NETG = 1 and MODPLS(I) = 1. (See Files [M2] and [C31.4].)

- ETZO(I) Distance of injection point from breech of tube (in).
- ETPR1(I) Dimensionless spreading rate coefficient (-).
- FRIN(I) Fraction of plasma flux directed to internal voidage in cases involving dual-voidage representation of flow through propellant. $0 \le FRIN \le 1$.

| File [C32] | "I-th Plasma Jet Detailed Data" (7F10.0) NETDAT(I) Cards |
|-------------|---|
| | required if and only if NETG = 1 and MODPLS(I) = 1. Tiles [M2] and [C31.4].) |
| ETGT (1, I) | First value of time (msec). |
| ETGE(1,I) | Fraction of total energy delivered by time $ETGT(1,I)$ (-). |
| ETGM(1,I) | Fraction of total mass delivered by time ETGM(1,1) (-). |
| ETGU(1,I) | Axial velocity component of plas ma jet at time ETGT(1,1) (in/sec). |
| ETGD (1, I) | Diameter of exit plane of capillary at time ETGT(1,I) (in). If ETGD is entered as zero, it defaults to ETDIA. (See File [31.5].) |
| ETGAM(1,I) | Ratio of specific heats of plasma jet at time ETGT(1,I) (-). If ETGAM is entered as zero, it defaults to ETAVGA. (See File [C31.5.) |
| ETMOL(1,I) | Molecular weight of jet at time ETGT(1,I) (lbm/lbmol). If ETMOL is entered as zero it defaults to ETAVMW. (See File [C31.5].) |
| ETGT(2,I) | Second value of time. Starts a new card. |

ETMOL (NETDAT (I), I)

N.B. Data in these tables are linearly interpolated within the table range.

The plasma flux is assumed to be zero outside the table range.

N.B. The following Files, [TC1] - [TC17] are required only if NTC = 1 or 2 (See File [M2]).

| File [TC1] | "Traveling Charge Control Data" (715) One Card TC-Mandatory |
|------------|---|
| IDEAL | Propellant burn rate indicator. 0 - Measured burn rate data. See Files [TC5] - [TC8]. 1 - Not Supported. 2 - Ideal burning with prespecified value of pressure on either side of gas/traveling charge interface or of projectile acceleration. Note the discussion of SIGMAX, MACH, APMAX in File [TC2]. |
| NPRC | 0 - Traveling charge treated as a rigid. 1 - Traveling charge treated as a continuum with analytical description of rheology. File [TC9] required. 2 - Traveling charge treated as continuum with tabular description of rheology. Files [TC10] and [TC11] required. |
| NPROP | Number of traveling charge increments (maximum of 20). |
| NWFR | Propellant Wall Friction Parameter. 0 - Friction between propellant and tube not considered. 1 - Friction due to gas film. File [TC12] required. >0 - Number of entries in velocity dependent coefficient of friction table (maximum of 10). File [TC13] required. |
| NBRES1 | 0 - Obturator resistance not given as table.>0 - Number of entries in table of resistive pressure versus travel (maximum of 10). File [TCl4] required. |
| NBRES2 | 0 - Resistance due to shocked air not considered.1 - Resistance due to shocked air considered. File [TC15] required. |
| NBRES3 | 0 - Obturator resistance not proportional to setback pressure. >0 - Number of entries in table of velocity dependent coefficient of friction of obturator (maximum of 10). Files [TC16] and [TC17] required. |

| File [TC2] | "Mesh Parameters" (I5,F10.0) One Card TC-Mandatory |
|------------|---|
| MAXDIM | Maximum number of mesh points to be used in continuum representation of traveling charge (\leq 100). |
| DXMIN | Minimum mesh size for continuum representation (in). |

| File [TC3] | "General Properties" (6F10.0) One Card TC-Mandatory |
|------------|---|
| DВ | Diameter of tube (in) if NTC = 1 and diameter of end burning charge if NTC = 2. (See File $[M2]$). |
| XIB | Initial length of gas column (in). |
| PRM | Mass of projectile (lbm). |
| SIGMAX | Maximum value of pressure at gas/propellant interface (psi). If SIGMAX = 0, no restriction is considered. SIGMAX pertains to the reacted or the unreacted side of the flame according as NPORS(KK) = 0 or 1 respectively. (See File [TC5].) |
| МАСН | Maximum value of Mach number of combustion products relative to regressing surface. If MACH = 0, no restriction is considered. |
| APMAX | Maximum value of acceleration of projectile (gravities). If APMAX = 0, no restriction is considered. |

N.B. Files [TC4] through [TC13] pertain to a specific type of propellant. The sequence [TC4] through [TC13], subject to relevant contingencies, is repeated for each type of traveling charge propellant in the problem. The index KK used in the following file descriptions runs through the values 1, 2, . . ., NPROP, where NPROP is defined in File [TC1].

| File [TC4] | "Propellant Thermochemical Properties" (8F10.0) One Card TC-Mandatory |
|-------------|--|
| XGAM (KK) | Ratio of specific heats of gas (-). |
| XBV (KK) | Covolume (in ³ /lbm). |
| XMOL (KK) | Molecular weight (lbm/lbmol). |
| XECHEM (KK) | Chemical energy of propellant (lbf-in/lbm). |
| XRHOP (KK) | Density of solid propellant at zero pressure (lbm/in3). |
| XCM(KK) | Mass of propellant (lbm). |
| XCRIT (KK) | Time delay following first exposure of increment base before combustion begins (msec). |
| XDEL (KK) | Time interval over which increment combustion rate increases to steady-state value (msec). |

| File [TC5] "B | ourn Rate Switches" (215) One Card TC-Mandatory |
|-------------------|---|
| MNBR1 (KK) | 0 - Exponential form for measured burn rate description of propellant KK. 1 - Tabular form for measured burn rate description of propellant KK. 2 - Propellant is endburning plasma guided design |
| npors (KK) | 0 - Measured burn rate data are given as function of pressure on reacted side of flame. Ideal burn rate value SIGMAX (see File [TC3]) pertains to reacted side. 1 - Measured burn rate data are given as function of pressure on unreacted side of flame. Ideal burn rate value SIGMAX pertains to unreacted side. |
| File [TC6] "T | abular Burn Rate Data" (215,F10.0) One Card TC-Contingent |
| | required if and only if IDEAL = 0 and MNBR1(KK) = 1. es [TC1] and [TC5].) |
| NBRP (KK) | Number of pairs of data in KK-th tabular description of burn rate (maximum of 20). |
| INTD | Number of table entries to use in divided difference interpolation. The same value is assumed for all propellants. |
| B1 (KK) | Burn rate additive constant for KK-th increment (in/sec). |
| File [TC7] "T | abular Burn Rate Data (cont'd) (2F10.0) NBRP(KK) Cards TC-Contingent |
| | required if and only if IDEAL = 0 and MNBR1(KK) = 1. es [TC1] and [TC5].) |
| PE (1, KK) | First value of pressure in tabular description of burn rate of propellant KK (psi). |
| RP(1, KK) | First value of burn rate of propellant KK corresponding to $PE(1,KK)$ (in/sec). |
| PE (NBP (KK), KK) | |
| RP (NBRP (KK), K | () |

| File [TC7.1] | "Plasma Guided End Burner" | (15, F15.0) | 1 card | , |
|--------------|---|-------------|--------|---|
| NBRM(I) | Number of sets of data to sponsor NBRM(I) must not be less that | | | |

EPLAS(I) Total energy of plasma to be added to surface of increment.

N.B. The subscript I indicates that as many as 20 separate increments may be defined for the endburning grain, each with distinct properties.

| File [TC7.2] | "Plasma Guided End Burner (Cont'd) (3F10.0) NBRM(I) cards |
|--------------|---|
| TBRM(1,1) | First time (msec). |
| FBRM(1,I) | Fraction of mass consumed at TBRM(1, I). |
| PLAS (1,I) | Fraction of plasma energy delivered at TBRM(1,I). |
| • | |

TBRM(NBRM(I), I)

N.B. A cubic spline is fitted to these data and is then explicitly differentiated to determine a continuously varying rate as required by the code. Smooth data should be provided since the spline can give problems with data containing high order structure. The rates are taken to be zero for times less than TBRM(1,I) and are set equal to the boundary value for times greater than TBRM(NBRM(I),I) in order to allow for complete consumption of the increment in the event of imperfect integration.

It is assumed that the plasma mass can be neglected. Also, it is assumed that there is no net delivery of plasma across the surface of the grain if the rate of regression is zero.

| File | [TC8] | "Exponential Burn Rate Data" (3F10.0) One Card TC-Contingent |
|--------|------------|--|
| N.B. | | required if and only if IDEAL = 0 and MNBR1(KK) = 0. Files [TC1] and [TC5].) |
| B1 (K | () | Burn rate additive constant for KK-th propellant (in/sec). |
| B2 (Ki | () | Burn rate pre-exponential coefficient for KK-th propellant $(in/sec-psi^{BN})$. |
| BN (K | ۲) | Burn rate exponent for KK-th propellant (-). |

File [TC9] "Propellant Analytical Rheology Data" (2F10.0) One Card TC-Contingent (See File [TC1].) File required if and only if NPRC = 1. N.B. Compressive wave speed at zero pressure in analytical XAUP (KK) description of propellant rheology (in/sec). Expansion wave speed in analytical description of propellant XADWN (KK) rheology (in/sec). If XADWN(KK) is entered so that it is less than the nominal compressive wave speed, the loading value is used. By entering XADWN(KK) = 0, a reversible law is defined. File [TC10] "Propellant Tabular Rheology Data" One Card (I5) TC-Contingent (See File [TC1].) File required if and only if NPRC = 2. N.B. Number of pairs of entries in tabular description of MNSS (KK) propellant rheology (maximum of 20). (3F10.0)"Propellant Tabular Rheology Data" (cont'd) File [TC11] MNSS(KK) Cards TC-Contingent File required if and only if NPRC = 2. (See File [TC1].) First value of percent strain in tabular description of PSTA(1,KK) propellant rheology (-). Corresponding value of pressure on nominal loading STRL(1,KK) (compression curve (psi)). Corresponding value of pressure on nominal unloading STRU(1,KK) (expansion curve (psi)). PSTA (MNSS (KK), KK) STRL (MNSS (KK), KK) STRU (MNSS (KK), KK) "Ablative Film Data" One Card TC-Contingent (2F10.0) File [TC12] File required if and only if NWFR < 0. (See File [TC1].) Viscosity of gas film used to lubricate propellant VISLYR (KK)

(lbm/in-sec).

DELYR (KK)

Thickness of film.

File [TC13] "Propellant Friction Data" (8F10.0) One to Three Cards TC-Contingent N.B. File required if and only if NWFR > 0. (See File [TC1].) All propellants are assumed to have the same number of data NWFR. AMUV(1,KK) First value of velocity of propellant (in/sec). Corresponding coefficient of friction on tube (-). AMU(1,KK) AMUV (NWFR, KK) Last value of velocity (in/sec). AMU (NWFR, KK) Corresponding coefficient of friction (-). File [TC14] "Tabular Bore Resistance Data" (8F10.0) One to Three Cards TC-Contingent File required if and only if NBRES1 # 0. (See File [TC1].) First value of projectile travel (in). BRX(1) BR (1) Corresponding value of resistive pressure due to obturator (psi). BRX (NBRES1) Last value of projectile travel (in). Corresponding value of resistive pressure (psi). BR (NBRES1) File [TC15] "Barrel Shock Resistance Data" (4F10.0) One Card TC-Contingent File required if and only if NBRES2 # 0. (See File [TC1].) N.B. Ratio of specific heats of air (-). AIRGAM Pressure of air in barrel (psi). AIRP0 AIRT0 Temperature of air in barrel (R). Molecular weight of air in barrel (lbm/lbmol). AIRMW

One Card File [TC16] "Obturator Setback Resistance Data" (3F10.0) TC-Contingent File required if and only if NBRES3 # 0. (See File [TC1].) N.B. Mass of projectile ahead of midpoint of obturating band PRMB (1bm). Length of bearing section of obturating band (in). ELB Poisson's ratio of obturating band (-). ANU One to Three Cards (8F10.0) "Obturator Friction Data" File [TC17] TC-Contingent N.B. File required if and only if NBRES3 # 0. (See File [TC1].) First value of velocity of projectile (in/sec). BMUV(1) Corresponding value of coefficient of friction between BMU(1) obturator and tube (-). Last value of velocity of projectile (in/sec). BMUV (NBRES3) BMU (NBRES3) Corresponding coefficient of friction (-). The following Files [TLC2] - [TLC22.7] are required if and only if N.B. NTLC = 1 (See File [M2]). One Card TLC-Mandatory File [TLC2] "Option Switches" (315) If 0, traveling liquid propellant is assumed to convert to KIN1 droplets instantaneously upon discharge into region where cavity is not mechanically stabilized. If 1, propellant converts to droplet form according to finite kinetic law which depends on slip velocity at propellant/cavity interface in region where cavity is not mechanically stabilized. File [TLC9.1] is required. If 0, droplets are assumed to burn instantaneously upon KIN2 formation. If 1, droplets are assumed to burn according to finite rate kinetic law which depends on pressure. File [TLC9.2] is required. Solutions based on KIN2 will only be valid if the ratio of specific heats and the molecular weight are not expected to vary, and provided that droplets are not swept back into the booster region. If 0, a TC expulsion charge is not located in the projectile NXPEL base.

base and Files [TLC22.1] - [TLC22.7] are required.

If 1, a TC expulsion charge is located in the projectile

| File [TLC5] | "Integration Parameters" (I5,2F10.0) One Card TLC-Mandatory |
|-------------|--|
| NMSHLC | Number of mesh points assigned to traveling liquid charge. Must be at least 6 unless NCAV = 0 (See File [TLC11]). Suggested value is 11. |
| DZMNLC | Minimum mesh spacing in traveling liquid charge (in). |
| TOLP | Convergence tolerance for iterative determination of fluxes between lumped parameter regions $(10^{-6} \text{ lbm}^2/\text{sec}^2)$. Default value is 1.0. Suggested value is 0.01. |

N.B. The value of 2 * NMSHLC must not exceed 95.

| File [TLC6] | "Tube Properties" (215,F10.0) One Card TLC-Mandatory |
|-------------|--|
| nbres1 | If 0, obturator resistance is neglected. If > 0, NBRES1 is the number of tabular entries used to define the obturator resistance as a function of travel. NBRES1 must not be greater than 8. File [TLC6.1] is required in this case. |
| nbres2 | If 0, resistance due to shocked air in front of projectile is neglected. If 1, resistance due to shocked air is considered. File [TLC6.2] is required in this case. |
| DB | Diameter of gun tube (in). |

| File [TLC6.1] | "Obturator Resistance" | (8F10.0) | One or Two Cards |
|---------------|------------------------|----------|------------------|
| | | | TLC-Mandatory |

N.B. File required if and only if NBRES1 > 0.

BRZ(1) First value of projectile travel (in).

BR(1) Corresponding value of obturator resistance (psi).

BRZ(NBRES1) Last value of projectile travel (in).

BR(NBRES1) Corresponding value of bore resistance (psi).

File [TLC6.2] "Air Shock Resistance Data" (8F10.0) One Card TLC-Mandatory

N.B. File required if and only if NBRES2 = 1.

AIRPO Initial pressure of gas in barrel (psi).

AIRTO Initial temperature of gas in barrel (R).

AIRGAM Ratio of specific heats of gas in barrel (-).

AIRMW Molecular weight of gas in barrel (lbm/lbmol).

File [TLC7] "Projectile Properties" (8F10.0) One Card TLC-Mandatory

PRM Projectile mass (lbm).

ZPRO Initial location of projectile base with respect to entrance of gun tube (in).

N.B. This datum does not take into account the possible presence of an afterbody used to stabilize the traveling liquid charge. The base of the afterbody is located a distance ZCAV(NCAV) - ZCAV(1) behind the projectile base. (See File [TLC11.1].) Accordingly, even if ZPRO is positive, it is possible that the data base may represent the afterbody as intruding into the booster combustion chamber. The analysis of the combustion chamber by XKTC is only performed to the base of the afterbody. Errors will occur if the afterbody intrudes into the chamber and the chamber diameter differs from that of the tube.

ZVENT Projectile travel after which traveling liquid charge begins

to vent rearwards from mechanically stabilized region.

RHOCAV Density of afterbody material (lbm/in³).

PCAV Pressure at which traveling liquid charge separates from

base of projectile (psi).

File [TLC7.1] "Chamber Length" (F10.0) One Card TLC-Mandatory

CHAMIN Distance from breech to entrance of tube (in).

| File | [TLC9] "Properties of Liquid Propellant" (8F10.0) One Card TLC-Mandato |
|------|--|
| RHOL | Density of liquid propellant at one atmosphere (lbm/in3). |
| BUL1 | Bulk modulus of liquid propellant at one atmosphere (psi). |
| BUL2 | Derivative of bulk modulus with respect to pressure at one atmosphere (-). |
| EFL | Chemical energy released in combustion (lbf-in/lbm). |
| GAML | Ratio of specific heats of products of combustion (-). |
| GML | Molecular weight of products of combustion (lbm/lbmol). |
| BVL | Covolume of products of combustion (in3/lbm). |
| | |
| File | [TLC9.1] "Propellant Droplet Formation Data" (8F10.0) One Card TLC-Continger |
| N.B. | This file is required if and only if KIN1 = 1. |
| DROP | Diameter of propellant droplets (in). This datum applies to both the traveling and the booster increments. |
| WIPE | Coefficient of proportionality between rate of droplet formation and slip velocity for traveling liquid charge in mechanically unstabilized region (lbm/in). |
| File | TLC9.2] "Droplet Burn Rate Data" (8F10.0) One Card TLC-Contingent |
| N.B. | This file is required if and only if KIN2 = 1. |
| B1 | Additive burn rate constant (in/sec). |
| B2 | Burn rate pre-exponential factor (in/sec/psi ^{BN}). |
| BN | Burn rate exponent (-). |
| | 4 |

| Initial pressure of gas (psi). |
|---|
| Initial pressure of traveling charge (psi). |
| Initial temperature (R). |
| Ratio of specific heats of initial ambient in TLC (-). |
| Molecular weight of initial ambient in TLC (lbm/lbmol). |
| nd GMOLST are not required by RLPTC. |
| |

| File [TLC11] | "Initial Cavity Parameters" (215) One Card TLC-Mandatory |
|--------------|---|
| NCAV | Number of tabular data used to describe initial configuration of cavity. Maximum of 50. If NCAV = 0, it is understood that there is no traveling liquid charge present. The subsequent data of this file are not required. |
| месн | If 0, cavity is not mechanically stabilized and its behavior is governed by the Taylor principle. If 1, cavity is stabilized and its geometry is taken to be frozen directly behind the projectile into the configuration defined by the initial data. |

| File [TLC11.1] | "Initial Cavity Geometry" | (3F10.0) | NCAV Cards |
|----------------|---------------------------|----------|----------------|
| | • | | TLC-Contingent |

N.B. This file is required if and only if NCAV > 0.

ZCAV(1)

First axial location for definition of initial cavity geometry (in). Starts a new card. The cavity defined by these data must formally extend to the projectile base. Zero values of RCAV may be used to represent sections of the traveling liquid charge which fill the cross-section of the tube. It is always understood that ZCAV(NCAV) corresponds to the base of the projectile. This latter assumption is always enforced internally to the code by adding a suitable value to the values of ZCAV(I), I = 1, ..., NCAV.

RCAV(1)

Corresponding radius of cavity (in).

THKV(1)

Thickness of mechanically stabilizing layer (in). Only used if MECH = 1. If THKV > 0, it is understood that RCAV refers to the exterior of the surface. The thickness is measured in the radial direction rather than normal to the surface of the stabilizing layer.

ZCAV (2)

Second axial location. Starts a new card.

THKV (NCAV)

| File [TLC22.1] | "Properties of | TLC E | xpulsion Charge | Combustion | Chamber" |
|----------------|----------------|-------|-----------------|------------|----------|
| • | (8F10.0) One | Card | TLC-Contingent | | |

N.B. This file is required if and only if NXPEL = 1.

CDCR(2) Discharge coefficient for venting to traveling charge region (-).

ACRI(2) Venting area (in²).

VCRO(2) TC expulsion charge chamber volume (in3).

PSTCR(2) Initial Pressure (psi).

TSTCR(2) Initial Temperature (R).

DELPST(2) Pressure differential between expulsion charge combustion chamber and forward end of TC to initiate venting (psi).

Once ventholes open, they stay open.

| File [TLC22.2] | "TLC Expulsion Charge Type" (5A4,2F10.0) One Card TLC-Contingent | | | |
|----------------|---|--|--|--|
| N.B. This file | is required if and only if NXPEL = 1. | | | |
| GRNMCR (2) | Name of propellant. Up to 20 alphanumeric characters. | | | |
| WGTCR (2) | Mass of TC expulsion charge (lbm). | | | |
| RHOPCR (2) | Density of propellant (lbm/in ³). | | | |
| File [TLC22.3] | "TLC Expulsion Charge Form Function" (I5,4F10.0) One Card TLC-Contingent | | | |
| N.B. This file | is required if and only if NXPEL = 1. | | | |
| NFRMCR (2) | Form function indicator. See discussion of File [M8]. Allowable values of NFRMCR are 1, 2, 5, 6, and 7. | | | |
| ODCR (2) | Grain dimension (in). | | | |
| DPRFCR(2) | Grain dimension (in). | | | |
| GLENCR (2) | Grain dimension (in). | | | |
| NPRFCR(2) | Number of perforations (-). | | | |
| File [TLC22.4] | "TLC Expulsion Charge Burn Rate Counter" (215) One Card TLC-Contingent | | | |
| N.B. This file | is required if and only if NXPEL = 1. | | | |
| NBRDCR (2) | Number of sets of values used to describe burn rate. 1 ≤ NBRDCR ≤ 10. | | | |
| INHBCR (2) | If 0, propellant is not deterred. If 1, propellant is deterred and File [TLC22.7] is required. | | | |
| | | | | |

File [TLC22.5] "TLC Expulsion Charge Burn Rate Description" (8F10.0) One to Four Cards TLC-Contingent N.B. This file is required if and only if NXPEL = 1. UPPCR (1, 2) Maximum value of pressure for corresponding values of burn rate pre-exponential and exponential factors (psi). B22CR(1,2) Burning rate pre-exponential factor (in/sec-psi*). BNNCR (1, 2) Burning rate exponent (-). Maximum value for last set of burn rate data. UPPCR (NBRDCR (2), 2) B22 (NBRDCR (2), 2) Corresponding pre-exponent. BNN (NBRDCR (2), 2) Corresponding exponent. B1CR(2) Burning rate additive constant (in/sec). Ignition delay (msec). DELCR(2) File [TLC22.6] "TLC Expulsion Charge Thermochemistry" (8F10.0) One Card TLC-Contingent This file is required if and only if NXPEL = 1. N.B. Internal energy released in combustion (lbf-in/lbm.) ECHCR(2) Molecular weight of combustion products (lbm/lbmol). GMCR(2) Ratio of specific heats (-). GAMACR (2)

| File [TLC22.7] | "Properties of Deterred Layer" (8F10.0) One Card TLC-Contingent |
|----------------|---|
| N.B. This file | is required if and only if $NXPEL = 1$ and $INHBCR(2) = 1$. |
| ECRIB(2)* | Internal energy released in combustion at start of deterred layer (lbf-in/lbm). |
| ECRIB2(2) | Internal energy released in combustion at end of deterred layer (lbf-in/lbm). |
| RGFCR (2) | Factor by which burn rate is multiplied at start of deterred layer (-). |
| RGFCR2(2) | Factor by which burn rate is multiplied at end of deterred layer (-). |
| HIBXCR(2) | Depth of inhibited layer (in). |

Values within deterred layer deduced by linear spacewise interpolation Final values need not be the same as those of the undeterred propellant.

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13. ABSTRACT(Maximum 200 words)

We describe a number of extensions to the XNOVAKTC (XKTC) code, a model of interior ballistics phenomena based on a numerical solution of the governing equations for one-dimensional, multi-phase flow. We also present some analytical formulations for the pressure gradient in a gun in a form suitable for incorporation into a lumped parameter interior ballistics model.

In XKTC, the flow resistance formula for stacked-granular propellant is extended to account for the increase in drag due to tumbling of the grains as the bed expands. The code is also extended to permit the analysis of the consequences of propellant fracture, with fracture taken to be dependent on the local maximum intergranular stress. An explicit representation of the impact induced granular compaction wave as a surface of discontinuity is encoded to support the fracture analysis.

The analytical formulas for the pressure gradient include the effects of tube geometry and several aspects of the structure of the two-phase flow. The results are in a closed form with the breech and base pressure explicitly related to the spacemean pressure. Results are presented for both granular and stick propelling charges.

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